

## Positional Number System

- **Radix** - number of unique symbols in a number system
- usually 0-9, then A-Z

## Number System Base conversion

**Base conversion between numeral systems**

- x numeral system to y numeral system (example: 32.2<sub>5</sub> to base-7)
- x numeral system → decimal → y numeral system
- 32.2<sub>5</sub> = 17.4<sub>10</sub> = 23.254<sub>7</sub>

32.2<sub>5</sub>

$2 \times 5^{-1} = 0.4$

$2 \times 5^0 = 2$

$3 \times 5^1 = 15$

summation: 17.4

7 | 17 3

2

0.4

-----

2.8

-----

0.8

-----

0.6

-----

0.254

-----

0.2

-----

1.4

we stop at 4 fractional places Slide 19

## 2x vs 10y

Decimal Name	Abbreviation	Value	Binary Term	Abbreviation	Value	% Largest	Value	Value
kilobits	kB	10 <sup>3</sup>	kibibits	KiB	2 <sup>10</sup>	1%	2 <sup>10</sup>	1 024
megabits	Mb	10 <sup>6</sup>	mebibits	MiB	2 <sup>20</sup>	1%	2 <sup>20</sup>	1 048 576
gigabits	Gb	10 <sup>9</sup>	gibibits	GiB	2 <sup>30</sup>	1%	2 <sup>30</sup>	1 073 741 824
terabits	Tb	10 <sup>12</sup>	tebibits	TiB	2 <sup>40</sup>	1%	2 <sup>40</sup>	1 099 511 627 776
petabits	Pb	10 <sup>15</sup>	pebibits	PiB	2 <sup>50</sup>	1%	2 <sup>50</sup>	1 125 899 906 842 624
exabits	Eb	10 <sup>18</sup>	exbibits	EiB	2 <sup>60</sup>	1%	2 <sup>60</sup>	1 152 921 504 606 846 976

- Binary prefix are mainly use in memory capacity
- SI prefix are usually use in data transfer rate or storage space
- abbreviation \* value = number of bits

## Binary Data Organization

Organization	Number of bits	Usage
Bit (binary digit)	2 cells - 0 or 1	Basic unit
Crumb	2 bits	*largely defunct term, rarely used
Nibble	4 bits	Hex digit, BCD digit
Byte	8 bits	Smallest addressable data unit
Half word	16 bits	Definition of word is architecture-dependent
Word	32 bits	A 32-bit architecture considers 1 word as 32-bit
Double word	64 bits	
Quad word	128 bits	

- a bit has 2 cells
- most significant (left) ----- least significant (right)
- bit(b), byte(B)
- little endian - **top** address to **bottom**
- big endian - **bottom** address to **top**

## Integer representation

### UNSIGNED

0 to (2<sup>n</sup>)-1

normal

fill the rest with 0 (MSb)

### SIGNED

-(2<sup>n-1</sup>) to +(2<sup>n-1</sup>)-1

sign and magnitude

sign bit | positive int

1's complement (n-1's)

flip for negative int

2's complement (n's)

flip then + 1, for negative int

- **unsigned** integers use **zero extension**
- **signed** integers use **sign extension**

*in short, extend the MSb until you have reached the sufficient num of bits*

## integer operation overflow

**SHOULD \_\_\_; otherwise, overflow**

*ADDITION*

**UNSIGNED** SHOULD NOT have carry

**SIGNED [same sign]** SHOULD remain the same sign

**SIGNED [different sign]** add using 2's complement representation (never overflow)

*SUBTRACTION*

**UNSIGNED** SHOULD HAVE carry

**SIGNED**  $A-B = A+B'$  (2's complement B)

addition of signed integers [same sign]

1. *first bit should never change*

2. *ignore carry if there is*



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Not published yet.

Last updated 18th September, 2023.

Page 1 of 3.

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## IEEE 754 Floating point for single precision

1 - sign bit	8 - exponent	23 - mantissa
0 for positive	$e' = e + 127$	f in 1.f notation

### Example:

Given:  $3.5_{10}$

1.  $3.5_{10} = 11.1_2$

2.  $1.11 \times 2^1$

3.  $e' = 128_{10} == 1000_0000_2$

Answer: 1\_1000000\_110 0000...00000

## IEEE 754 Floating point for single precision

1 - sign bit	8 - exponent	23 - mantissa
0 for positive		

## test

1 - sign bit	8 - exponent	23 - mantissa
0 for positive	$e' = e + 127$	f in 1.f notation

### Example:

Given:  $3.5_{10}$

1.  $3.5_{10} = 11.1_2$

2.  $1.11 \times 2^1$

3.  $e' = 128_{10} == 1000_0000_2$

Answer: 1\_1000000\_110 0000...00000

## Special cases floating single precision

Sign Bit	E'	Significand	Value
0	0000 0000	000 0000 0000 0000 0000	+0 (Positive Zero)
1	0000 0000	000 0000 0000 0000 0000	-0 (Negative Zero)
01	0000 0000	$\neq 0$	Denormalized
0	1111 1111	000 0000 0000 0000 0000	+ Infinity
1	1111 1111	000 0000 0000 0000 0000	- Infinity
x	1111 1111	01x xxxx xxxx xxxx xxxx	sNaN
x	1111 1111	1xx xxxx xxxx xxxx xxxx	qNaN



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Last updated 18th September, 2023.  
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