

### Double Angle Identities

$$33. \sin\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 - \cos \theta}{2}} \quad \sin^2 \theta = \frac{1 - \cos 2\theta}{2}$$

$$34. \cos\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 + \cos \theta}{2}} \quad \cos^2 \theta = \frac{1 + \cos 2\theta}{2}$$

$$35. \tan\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 - \cos \theta}{1 + \cos \theta}} \quad \tan\left(\frac{\theta}{2}\right) = \frac{1 - \cos \theta}{\sin \theta} = \frac{\sin \theta}{1 + \cos \theta}$$

### Half-Angle Identities

$$\sin\left(\frac{a}{2}\right) = \pm \sqrt{\frac{1 - \cos a}{2}}$$

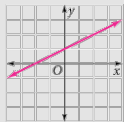
$$\cos\left(\frac{a}{2}\right) = \pm \sqrt{\frac{1 + \cos a}{2}}$$

$$\tan\left(\frac{a}{2}\right) = \frac{1 - \cos a}{\sin a} = \frac{\sin a}{1 + \cos a}$$

### Families of Function

#### Linear function

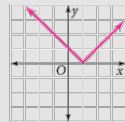
$$y = mx + b$$



slope =  $m$   
y-intercept =  $b$   
The greatest exponent is 1.

#### Absolute value function

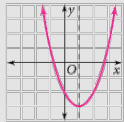
$$y = |x - a| + b$$



shift  $y = |x|$  horizontally  $a$  units  
shift  $y = |x|$  vertically  $b$  units  
vertex at  $(a, b)$   
The greatest exponent is 1.

#### Quadratic function

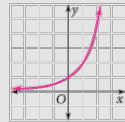
$$y = ax^2 + bx + c$$



parabola with axis of symmetry at  $x = -\frac{b}{2a}$   
The greatest exponent is 2.

#### Exponential function

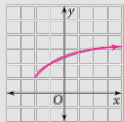
$$y = ab^x$$



growth for  $b > 1$   
decay for  $0 < b < 1$   
The variable is the exponent.

#### Radical function

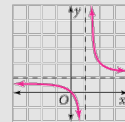
$$y = \sqrt{x - b} + c$$



shift  $y = \sqrt{x}$  horizontally  $b$  units  
shift  $y = \sqrt{x}$  vertically  $c$  units  
The variable is under the radical.

#### Rational function

$$y = \frac{a}{x - b} + c$$



vertical asymptote at  $x = b$   
horizontal asymptote at  $y = c$   
The variable is in the denominator.

### Identities

A. Reciprocal	B. Ratio	C. Pythagorean
$\csc = \frac{1}{\sin}$	$\tan = \frac{\sin}{\cos}$	$\sin^2 + \cos^2 = 1$
$\sin \csc = 1$	$\cot = \frac{\cos}{\sin}$	$\tan^2 + 1 = \sec^2$
$\sec = \frac{1}{\cos}$	$\cos = \frac{\sin}{\tan}$	$1 + \cot^2 = \csc^2$
$\cos \sec = 1$	$\sin = \frac{\cos}{\cot}$	$1 - \cos^2 = \sin^2$
$\cot = \frac{1}{\tan}$	$\sin = \cos \tan$	$1 - \sin^2 = \cos^2$
$\sin = \frac{1}{\csc}$	$\cos = \sin \cot$	$\sec^2 - 1 = \tan^2$
$\cos = \frac{1}{\sec}$		$\csc^2 - 1 = \cot^2$
$\tan = \frac{1}{\cot}$		$\sec^2 \cdot \tan^2 = 1$
		$\csc^2 \cdot \cot^2 = 1$

### Parent Functions

constant function

$f(x) = a$  graph is a horizontal line

identity function

$f(x) = x$  points on graph have coordinates  $(a, a)$

quadratic function

$f(x) = x^2$  graph is U-shaped

cubic function

$f(x) = x^3$  graph is symmetric about the origin

square root function

$f(x) = \sqrt{x}$  graph is in first quadrant

reciprocal function

$f(x) = 1/x$  graph has two branches

absolute value function

$f(x) = |x|$  graph is V-shaped

### Exponential & Logarithmic

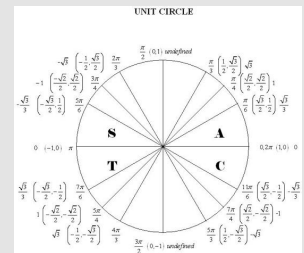
Logarithmic

$$y = \ln x$$

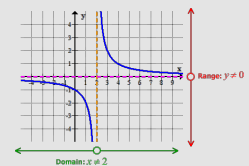
Exponential

$$y = b^x$$

### Unit Circle



### Domain & Range



**Domain:** The domain of a function is the set of all possible input values (often the "x" variable), which produce a valid output from a particular function. It is the set of all real numbers for which a function is mathematically defined.

**Range:** The range is the set of all possible output values (usually the variable  $y$ , or sometimes expressed as  $f(x)$ ), which result from using a particular function.