

### Basic Cobb-Douglas Production Function

Key Properties	Marginal Product of Capital	Marginal Product of Labor
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-Constant Returns to Scale

MPK=Partial derivate of F(K,N)	MPN=Partial derivate of F(K,N)
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-If inputs are 0 outputs will be 0

$MPK = A\alpha(K/N)^{\alpha-1}$	$MPN = A(1-\alpha)(K/N)^{\alpha}$
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-The production function is increasing in each of the inputs

$\alpha(Y/K) > 0$	$(1-\alpha)(Y/K) > 0$
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-The production function exhibits diminishing returns

### Neg Impact of Aging Labor Force

- Rapid retirement decreases the firms overall knowledge, decreasing productivity.
- Productivity peaks at age 50

### Growth Rate of GDP

$$Y = (Y/N) * N$$

then take logs

$$\ln Y = \ln[Y/N] + \ln N$$

Differentiate for time

$$Y^{\circ}/Y = (Y^{\circ}/N)/(Y/N) + N^{\circ}/N$$

Growth rate of GDP equals the growth rate of labor productivity and the growth rate of labor stock

### Solow Growth Model Basics

**Aggregate Production Function**  $Y = AK^{\alpha}N^{1-\alpha}$

**Per Worker Production Function**  $y = Ak^{\alpha}$

**Capital Stock Accumulation**  $K^{\circ} = 1-\delta K$

**Capital Per Worker Accumulation**  $k^{\circ} = sf(k) - (n+\delta)k$

**Steady-State Equilibrium**  $k^{\circ} = 0 \rightarrow sf(k) = (n+\delta)k$