Cheatography

Linear Algebra Cheat Sheet by spoopyy via cheatography.com/28376/cs/8341/

Rasis

A set S is a basis for V if

1. S spans V

2. S is LI.

If S is a basis for V then every vector in V can be written in one and only one way as a linear combo of vectors in S and every set containing more than n vectors is I.D.

Basis Test

1. If S is a LI set of vectors in V, then S is a basis for V

2. If S spans V, then S is a basis for V

Change of Basis

 $P[x]_B' = [x]_B$

 $[x] B' = P^{-1} [x] B$

 $[B B'] \rightarrow [I P^{-1}]$

[B'B]->[IP]

Cross Product

if u = u1i + u2j + u3k

AND

v = v1i + v2j + v3k

THEN

 $u \times v = (u2v3 - u3v2)i - (u1v3 - u3v1)j + (u1v2 - u2v1)k$

Definition of a Vector Space

u + v is within V

u+v = v+u

u+(v+w) = (u+v)+w

u+0 = u

u-u=0

cu is within V

c(u+v) = cu+cv

(c+d)u = cu+du

c(du) = (cd)u

 $1^*u = u$

Diagonalizable Matrices

A is diagonalizable when A is similar to a diagonal matrix.

That is, A is diagonalizable when there exists an invertible matrix P such that P-1AP is a diagonal matrix

Dot Products Etc.

length/norm $||v|| = \operatorname{sqrt}(v_1^2 + ... + v_n^2)$

||cv|| = |c| ||v||

v / ||v|| is the unit vector

distance d(u,v) = ||u-v||

Dot product $u \cdot v = (u_1v_1 + ... + u_nv_n)$

 $n \cos(theta) = u \cdot v / (||u|| ||v||)$

u&v are orthagonal when dot(u,v) = 0

Eigenshit

The scalar lambda(Y) is called an **Eigenvalue** of A when there is a nonzero vector x such that Ax = Yx.

Vector x is an **Eigenvector** of A corresponding to Y.

The set of all eigenvectors with the zero vector is a subspace of Rⁿ called the **Eigenspace** of Y.

- 1. Find Eigenvalues: det(YI A) = 0
- 2. Find Eigenvectors: (YI A)x = 0

If A is a triangular matrix then its eigenvalues are on its main diagonal

Gram-Schmidt Orthonormalization

1. B = {v1, v2, ..., vn}

2. B' = {w1, w2, ..., wn}:

w1 = v1

w2 = v2 - projw1v2

w3 = v3 - projw1v3 - projw2v3

wn = vn - ...

3. B" = {u1, u2, ..., un}:

ui = wi/||wi||

B" is an orthonormal basis for V span(B) = span(B")

Important Vector Spaces

Вn

C(-inf, +inf)

C[a, b]

Р

 M_m,n

Inner Products

 $||u|| = sqrt \langle u, u \rangle$

d(u,v) = ||u-v||

 $cos(theta) = \langle u, v \rangle / (||u|| ||v||)$

u&v are orthagonal when $\langle u,v \rangle = 0$

proj_v u = <u,v>/<v,v> * v

Kernal

For T:V->W The set of all vectors v in V that satisfies T(v)=0 is the kernal of T. ker(T) is a subspace of v.

For T:Rⁿ ->R^m by T(x)=Ax ker(T) = solution space of Ax=0 & Cspace(A) = range(T)

Linear Combo

v is a linear combo of u_1 ... u_n

.

Linear Independence

a set of vectors S is LI if c1v1 +...+ ckvk = 0 has only the trivial solution.

If there are other solutions S is LD.

A set S is LI iff one of its vectors

can

be written as a combo of other S vectors.

Linear Transformation

V & W are Vspaces. T:V->W is a linear transformation of V into W if:

- 1. T(u+v) = T(u) = T(v)
- 2. T(cu) = cT(u)

Non-Homogeny

If xp is a solution to Ax = b then every solution to the system can be written as x = xp

Nullity

Nullspace(A) = $\{x \in R^n : Ax = 0\}$ Nullity(A) = dim(Nullspace(A)) = n - rank(A)

Orthogonal Sets

Set S in V is orthogonal when every pair of vectors in S is orthogonal. If each vector is a unit vector, then S is orthonormal





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One-to-One and Onto

T is one-to-one **iff** $ker(T) = \{0\}$

T is onto **iff** rank(T) = dim(W)

If dim(T) = dim(W) then T is one-to-one **iff** it is onto

Rank and Nullity of 1

nullity(T) = dim(kernal)

rank(T) = dim(range)

 $range(T) + nullity(T) = n (in m_x n)$

dim(domain) = dim(range) + dim(kernal)

Bank of a Matrix

Rank(A) = dim(Rspace) = dim(Cspace)

Similar Matrices

For square matrices A and A' of order n, A' is similar to A when there exits an invertible matrix P such that $A' = P^{-1}AP$

Spanning Sets

 $S = \{v1...vk\}$ is a subset of vector space V. S spans V if every vector in v can be written as a linear combo of vectors in S.

Test for Subspace

1. u+v are in W

2. cu is in w



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