

Statistics

the branch of mathematics in which data are used descriptively or inferentially to find or support answers for scientific and other quantifiable questions.

It encompasses various techniques and procedures for recording, organizing, analyzing, and reporting quantitative information.

Difference - parametric test & non-parametric test					
PROPERTIES	PARAMETRIC	NON-PARAMETRIC			
assumptions	YES	NO			
value for central tendency	mean median/mode				
probability distribution	normally distri- buted	user specific			
population knowledge	required	not required			
used for	interval data	nominal, ordinal data			
correlation	pearson	spearman			
tests	t test, z test, f test, ANOVA	Kruskal Wallis H test, Mann-w- hitney U, Chi-square			

Correlation Coefficient

a statistical measure of the strength of the relationship between the relative movements of two variables

value ranges from -1 to +1

- -1 = perfect negative or inverse correlation
- +1 = perfect positive correlation or direct relationship
- 0 = no linear relationship

Alternatives	
PARAMETRIC	NON-PARAMETRIC
one sample z test, one sample t test	one sample sign test
one sample z test, one sample t test	one sample Wilcoxon signed rank test
two way ANOVA	Friedman test
one way ANOVA	Kruskal wallis test
independent sample t test	mann-whitney U test
one way ANOVA	mood's median test
pearson correlation	spearman correlation

Paired t-test

to compare means of two related groups

ex. compare weight of 20 mice before and after treatment *two conditions:*

- pre post treatment
- two diff conditions ex two drugs

ASSUMPTIONS

- random selection
- normally distributed
- no extreme outliers

FORMULA

t= m / s/√n

m= sample mean of differences

df= n-1

t-distribution

aka Student's t-distribution = probability distribution similar to normal distribution but **has heavier tails**

used to estimate pop parameters for small samples

Tail heaviness is determined by degrees of freedom = gives lower probability to centre, higher to tails than normal distribution, also have higher kurtosis, symmetrical, unimodal, centred at 0, larger spread around 0

df = n - 1

above 30df, use z-distribution

t-score = no of SD from mean in a t-distribution

we find:

- upper and lower boundaries
- p value

TO BE USED WHEN:

- small sample
- SD is unknown

ASSUMPTIONS

- cont or ordinal scale
- random selection
- NPC
- equal SD for indep two-sample t-test



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Two-sample z-test

to determine if means of two independent populations are equal or different

to find out if there is significant diff bet two pop by comparing sample mean

knowledge of:

SD and sample >30 in each group

eg. compare performance of 2 students, average salaries, employee performance, compare IQ, etc

FORMULA:

 $z = \bar{x}_1 - \bar{x}_2 / \sqrt{s_1^2/n_1} + s_2^2/n_2$

s= SD

formula:

 $z = (\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2) / \sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}$

 $(\mu_1 - \mu_2)$ = hypothesized difference bet pop means

Point Biserial correlation

measures relationship between two variables

rpbi = correlation coefficient

one continuous variable (ratio/interval scale)

one naturally binary variable

FORMULA:

rpb= M1-M0/Sn * √ pq

Sn= SD

Two-sample z-test

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eg. compare performance of 2 students, average salaries, employee performance, compare IQ, etc

FORMULA:

7= x̄

z-test

for hypothesis testing

to check whether means of two populations are equal to each other when pop variance is known

we have knowledge of:

- SD/population variance and/or sample n=30 or more

if both unknown -> t-test

left-tailed

right-tailed

two-tailed

z-test (cont)

REJECT NULL HYPOTHESIS IF Z STATISTIC IS STATISTICALLY SIGNIFICANT WHEN COMPARED WITH CRITICAL VALUE

z-statistic/ z-score = no representing result from z-test

z critical value divides graph into acceptance and rejection regions

if z stat falls in rejection region-> H0 can be rejected

TYPES

One-sample z-test

Two-sample z-test

ANOVA

Analysis of Variance

comparing several sets of scores

to test if means of 3 or more groups are equal

comparison of variance between and within groups

to check if sample groups are affected by same factors and to same degree

compare differences in means and variance of distribution

ONE-WAY ANOVA=no of IVs

single IV with different (2) levels/variations have measurable effect

compare means of 2 or more indep groups

aka:

- one-factor ANOVA
- one-way analysis of variance
- between subjects ANOVA

Assumptions

- independent samples
- equal sample sizes in groups/levels
- normally distributed
- equal variance

F test is used to check statistical significance

higher F value --> higher likelihood that difference observed is real and not due to chance

used in field studies, experiments, quasi-exp

CONDITIONS:

- min 6 subjects
- sample no of samples in each group

H0: μ1=μ2=μ3 ... μk i.e. all pop means are equal

Ha: at least one μ i is different i.e atleat one of the k pop means is not equal to the others

μi is the pop mean of group





Spearman Correlation

non-parametric version of Pearson correlation coefficient named after Charles Spearman denoted by $\rho(\text{rho})$

determine the strength and direction of monotonic variables bet two variables measured at ordinal, interval or ratio levels & whether they are correlated or not

monotonic function=one variable never increases or never decreases as its IV changes

- monotonically increasing= as X increases, Y never decreases
- monotonically decreasing= as X increases, Y never increases
- not monotonic= as X increases, Y sometimes dec and sometimes inc

for analysis with: ordinal data, continuous data uses ranks instead of assumptions of normality

aka Spearman Rank order test

FORMULA:

 $\rho = 1 - 6\Sigma d_i^2/n(n^2-1)$

di= difference between two ranks of each observation

- -1 to +1
- +1 = perfect association of ranks

0= no association

-1= perfect negative association of ranks

closer the value to 0, weaker the association

Value Ranges

0 to 0.3 = weak monotonic relationship

0.4 to 0.6 = moderate strength monotonic relationship

0.7 to 1 = strong monotonic relationship

Parametric and Non-parametric test

Fixed set of parameters, certain assumptions about **distribution of population**

PARAMETRIC - prior knowledge of pop distribution i.e NORMAL DISTRIBUTION

NON-PARAMETRIC - no assumptions, do not depend on population, DISTRIBUTION FREE tests, values found on nominal or ordinal level

easy to apply, understand, low complexity decision based on - distribution of population, size of sample parametric - mean & <30 sample

non-parametric - median/mode & >30 sample or regardless of size

Advantages & Disadvantages - NON-PARAMETRIC TESTS				
ADVANTAGES	DISADVANTAGES			
simple, easy to understand	less powerful than parametrics			
no assumptions	counterpart parametric if exists, is more powerful			
more versatile	not as efficient as parametric tests			
easier to calculate	may waste information			
hypothesis tested may be more accurate	requires larger sample to be as powerful as parametric test			
small sample sizes are okay	difficult to compute large samples by hand			
can be used for all types of data (nominal, ordinal, interval)	tabular format of data required that may not be readily available			
can be used with data having outliers				

Application	
PARAMETRIC TESTS	NON-PARAMETRIC TESTS
- quantitative & continuous data	- mixed data
- normally distributed	- unknown distribution of population
- data is estimated on ratio or interval scales	- different kinds of measur- ement scales

degrees of freedom

independent values in the data sample that have freedom to vary FORMULA:

no of values in a data set minus 1 df= N-1

t-test

statistical test to determine if significant difference between avg scores of two groups

1908-William Sealy Gosset-student t-test and t-distirbution for hypothesis testing

knowledge of:

distribution - normally distributed



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t-test (cont)

no knowledge of SD

TYPES:

one-sample t-test - single group

FORMULA:

t= m - μ / s/√n

SD FORMULA:

 $\sigma = \sqrt{\Sigma(X-\mu)^2} / N$

 $s=\sqrt{\Sigma(X-\mu)^2}/n-1$

independent two-sample t-test - two groups

paired/dependent samples t-test - sig diff in paired measurements, compares means from same group at diff times (test-retest sample)

H0: no effective difference = measured diff is due to chance

Ha: two-tailed/ one-tailed nonequivalent means/smaller or larger than hypothesized mean

PERFORM **two-tailed test**: to find out difference bet two populations **one-tailed**: one pop mean is > or < other

Independent two-sample t-test

aka unpaired t-test

to compare mean of two independent groups

ex. avg weight of males and females

two forms:

- student's t-test: assumes SD is equal
- welch's t-test: less restrictive, no assumption of equal SD

both provide more/less similar results

ASSUMPTIONS:

- normally distributed
- SD is same
- independent groups
- randomly selected
- independent observations
- measured on interval or ratio scale

FORMULA:

 $t = \bar{x}_1 - \bar{x}_2 / \sqrt{s_1 2/n_1 + s_2 2/n_2}$

df= n1 + n2 - 2

 $S = \sqrt{\Sigma (x1-\bar{x})^2 + (x2-\bar{x})^2} / n1+n2-2$

One-sample z-test

to check if difference between sample mean & population mean when SD is known

FORMULA:

z=x-µ/SE

SE=σ/√n

z score is compared to a **z table** (includes % under NPC bet mean and z score), tells us whether the z score is due to chance or not **conditions**:

knowledge of:

- pop mean
- SD
- simple random sample
- normal distribution

two approaches to reject H0:

- p-value approach - p-value is the smallest level of significance at which H0 can be rejected...smaller p-value, stronger evidence
 -critical value approach - comparing z stat to critical values... indicate boundary regions where stat is highly improbable to lie= critical regions/rejection regions

if z stat is in critical region-> reject H0

based on:

significance level (0.1, 0.05, 0.01), alpha level, Ha

Biserial correlation

to measure relationship between quantitative variables and binary variables

given by Pearson - 1909

biserial correlation coeff varies bet -1 and 1

0= no association

ex. IQ scores and pass/fail correlation

continuous variable and **binary variable** (dichotomised to create binary variable)

rbis or **rb** = correlation index estimating strength of relationship between artificially dichotomous variable and a true continuous variable

ASSUMPTIONS:

- data measured on continuous scale
- one variable to be made dichotomous
- no outliers
- approx normally distributed
- equal variances (SD)

FORMULA

rb= M1-M0/SDt * pq/y



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Biserial correlation (cont)

M1=mean of grp 1

M2= mean of grp 2

p= ratio of grp 1

q= ratio of grp 2

SDt= total SD

y= ordinate

Pearson Correlation

measures **strength and direction** of a linear relationship between two variables

how two data sets are correlated

gives us info about the slope of the line

aka:

- Pearson's r

- bivariate correlation
- Pearson product-moment correlation coefficient (PPMCC) cannot determine dependence of variables & cannot assess

nonlinear associations

r value variation:

-0.1 to -.03 / 0.1 to 0.3 = weak correlation

-0.3 to -0.5 / 0.3 to 0.5 = average/moderate correlation

-0.5 to -1.0 / 0.5 to 1.0 = strong correlation

FORMULA:

 $r=n(\Sigma xy)-(\Sigma x)(\Sigma y) / \sqrt{[n\Sigma x^2-(\Sigma x)^2][n\Sigma y^2-(\Sigma y)^2]}$

Mann-Whitney U test

non-parametric test to test the significance of difference two independently drawn groups OR compare outcomes between two independent groups

equi to unpaired t test

CONDITIONS:

No NPC assumption, small sample size >30 with min 5 in each group, continuous data (able to take any no in range), randomly selected samples,

aka:

Mann-Whitney Test

Wilcoxon Rank Sum test

H0: the two pop are equal

Ha: the two pop are not equal

denoted by U

FORMULA:

Mann-Whitney U test (cont)

U1=n1n2+ n1(n1+1)/2 - R1

U2=n1n2+ n2(n2+1)/2 - R2

R= sum of ranks of group

One-way ANOVA test

Source of Variation	Sums of Squares (SS)	Degrees of Freedom (df)	Mean Squares (MS)	F
Between Treatments	$SSB = \Sigma v_J \left(\bar{X}_J - \bar{X} \right)^2$	dfr= k-1	$MSB = \frac{SSB}{k-1}$	$F = \frac{MSB}{MSE}$
Error (or Residual)	$\mathbf{SSE} = \mathbf{\Sigma} \mathbf{\Sigma} \left(\mathbf{X} - \mathbf{\bar{X}}_{f} \right)^{2}$	dfe=N-k	MSE= SSE/N-k	
Total	SST= SSB+SSE	dft=N-1		

One-way ANOVA test

- . SSB/SSR = the regression sum of squares
- SSE = the error sum of squares
- SST = the total sum of squares (SST = SSR + SSE)
- dfr = the model degrees of freedom (equal to dfr = k 1)
- dfe = the error degrees of freedom (equal to dfe = n k)
- k = the total number of groups (levels of the independent variable)
- n = the total number of observations
- dft = the total degrees of freedom (equal to dft = dfr + dfe = n 1)

One-way ANOVA test

- MSR = SSR/dfr = the regression mean square
- MSE = SSE/dfe = the mean square error
- Then the F statistic itself is computed as:
- F=MSR/MSE
 p: The p-value that corresponds to Fdfr, dfe

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