

### Distance Formula

$$\text{distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

### Slope Formula

$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1} \text{ where } x_2 \neq x_1$$

### Midpoint Formula

$$\text{midpoint} = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

### Types of Triangles

Name	Example	Point of Concurrency	Special Property	Example
perpendicular bisector		circumcenter	The circumcenter P of $\triangle ABC$ is equidistant from each vertex.	
angle bisector		incenter	The incenter Q of $\triangle ABC$ is equidistant from each side of the triangle.	
median		centroid	The centroid R of $\triangle ABC$ is two thirds of the distance from each vertex to the midpoint of the opposite side.	
altitude		orthocenter	The lines containing the altitudes of $\triangle ABC$ are concurrent at the orthocenter S.	

### Proof

Using CPCTC in a Proof  
 Given:  $\overline{DE} \parallel \overline{AC}$ ,  $\overline{DF} \parallel \overline{BC}$   
 Prove:  $\overline{EF} \parallel \overline{AC}$

Statements	Reasons
1. $\overline{DE} \parallel \overline{AC}$	1. Given
2. $\overline{DF} \parallel \overline{BC}$	2. Given
3. $\angle DEB \cong \angle ACB$	3. Alt. Ang. $\angle$ Thm.
4. $\overline{DE} \parallel \overline{AC}$	4. Reflex Prop. of $\parallel$
5. $\angle DEF \cong \angle ACB$	5. Alt. Ang. $\angle$ Thm.
6. $\angle DEB \cong \angle ACB$	6. CPCTC
7. $\overline{EF} \parallel \overline{AC}$	7. Converse of Alt. Ang. $\angle$ Thm.

### Terms

Acute Angle	Less than $90^\circ$
Adjacent Angle	Two angles on the same plane
Collinear Points	Two points on the same line
Complementary Angle	Two angles whose sum is $90^\circ$
Midpoint	The point halfway between the endpoints of a segment.
Obtuse Angle	More than $180^\circ$
Ray	A point on a line and all points in one direction
Vertical Angles	Two nonadjacent angles formed by two intersecting lines

### Terms (cont)

Linear Pair	Adjacent angles whose non-common sides are opposite rays
Isoscles	At least two sides are congruent
Scalene	Nothing is congruent
Equilatera	Every side is the same length
Biconditional	A and B are bi conditionally related if A implies B and B implies A.
Counterexample	a number which disproves a proposition For example, the prime number 2 is a counterexample to the statement "All prime numbers are odd."
Isometry	A isometry is a transformation where distance (aka size) is preserved.
Preimage	Produced by reflection from a mirror, refraction by a lens, or the passage of luminous rays through a small aperture and their reception on a surface.
Translation	A transformation in which a graph or geometric figure is picked up and moved to another location without any change in size or orientation.

### Types of Angles

<u>Alternate Interior Angles</u>		Equal
<u>Same Side Interior Angles</u>		Supplementary
<u>Alternate Exterior Angles</u>		Equal
<u>Same Side Exterior Angles</u>		Supplementary
<u>Corresponding Angles</u>		Equal

### Pythagorean Theorem

$$a^2 + b^2 = c^2$$

### Congruent Angles



### Reflections

TYPE OF REFLECTION	Point of the pre-image (Before reflection)	Point of the image (After reflection)
Reflection about the x-axis	$(x, y)$	$(x, -y)$
Reflection about the y-axis	$(x, y)$	$(-x, y)$
Reflection about the line $y = x$	$(x, y)$	$(y, x)$
Reflection about the line $y = -x$	$(x, y)$	$(-y, -x)$
Reflection about the origin	$(x, y)$	$(-x, -y)$

### Proof

Given:  
P is the midpoint of  $\overline{LO}$  and  $\overline{MN}$ .  
Show that  $\overline{LM} \parallel \overline{NO}$ .

Statements	Reasons
1. P is the midpoint of both $\overline{LO}$ and $\overline{MN}$ .	1. Given
2. $\overline{LP} \cong \overline{PO}$ $\overline{MP} \cong \overline{PN}$	2. Definition of Midpoint
3. $\angle NPO \cong \angle LPM$	3. Vertical angles are congruent.
4. $\triangle LPM \cong \triangle OPN$	4. SAS Congruence Postulate
5. $\angle MLP \cong \angle NOP$	5. CPCTC
6. $\overline{LM} \parallel \overline{NO}$	6. Converse of Alternate Interior Angles Theorem
7. $\overline{LM} \parallel \overline{NO}$	7. Segments of parallel lines are parallel.

### Properties

Name	Property of Equality
Addition Property	<b>If <math>a = b</math>, then <math>a + c = b + c</math></b>
Subtraction Property	<b>If <math>a = b</math>, then <math>a - c = b - c</math></b>
Multiplication Property	<b>If <math>a = b</math>, then <math>ac = bc</math></b>
Division Property	<b>If <math>a = b</math>, then <math>a/c = b/c</math></b>
Reflexive Property	<b>For any real #, <math>a = a</math></b>
Symmetric Property	<b>If <math>a = b</math>, then <math>b = a</math></b>
Transitive Property	<b>If <math>a = b</math> and <math>b = c</math>, then <math>a = c</math></b>
Substitution Property	<b>If <math>a = b</math>, then <math>b</math> can be substituted in for <math>a</math></b>