

### UNIT 4

#### PART A

**modeling transform-ations** Viewing transformations

world coordinate system. re-position the scene in front of a camera

**view orientation transf-ormation** DC to WC; camera at origin looking along -z axis

**parallel projection** perspective projection

preserves true measur-ements; less realistic realistic (depth); does not preserve true measur-ements

**Center of Projection (COP) or Projection Reference Point (PRP)** is the single point where all projectors converge

**Viewport Clipping** - after projection in standard viewing pipeline (before the perspective projection division; avoids division by zero)

**Back-Face Detection condition**  $V = N \cdot D$

**Scan-Line Method** determines the closest object along the line of sight (depth) and its corresponding color

### UNIT 4 (cont)

**Painter's Algorithm.** Primary criterion: sorted by minimum z-depth  
- Depth-- Ambiguity tests: Bounding rectangle overlap test, depth overlap test, surface inters-  
Sorting ection test, and final "complete  
Method behind" test.

composite transformation matrix is not commutative  
limitation of Back-Face  
Detection : multiple front faces overlap or obscure each other (hard to detect)

#### Parallel vs. Perspective projection

Parallel projection	Perspective projection
Orthographic: perpendicular rays	converge at a point (foreshortening)
Oblique: angled rays	
No depth cues, looks artificial, parallel lines stay parallel	Realistic, depth visible, lines converge (vanishing points)
Technical Drawings	Realistic Visual-ization

Parallel → accuracy & measurement  
Perspective → realism & depth

#### Back-Face Detection algorithm

Removes polygons whose normal faces away from viewer

$N \cdot V \leq 0 \rightarrow$  discard

**Sufficient for:** Single, convex, closed objects (e.g., cube)

#### Limitations

### Back-Face Detection algorithm (cont)

- 1. Concave Objects:** May remove faces that are actually visible
- 2. Multiple Objects:** Cannot decide visibility between different objects; No depth comparison
- 3. Transparent Surfaces:** Incorrectly removes visible back faces
- 4. Open Surfaces:** Back-face concept may not apply
5. Does not resolve cyclic overlap cases
6. Object-space only; doesn't compare between objects

It is a pre-processing culling step that reduces the polygon count sent to the rendering pipeline (by ~50%).  
followed by a true **Hidden Surface Removal (HSR)** algorithm (e.g., Depth-Buffer/Z--Buffer, Painter's, BSP Trees)

### 3D clipping

#### Steps

1. Transform vertices → Normalized Device Coordinates (NDC) using projection
2. Clip against 6 planes of canonical cube:  $x=\pm 1, y=\pm 1, z=0/1$
3. Test vertices (inside/outside)
4. Compute intersection points if edges cross planes
5. Discard outside parts, pass clipped primitives for viewport mapping

#### Standardized Cube

Uniform planes (inside/out and intersection math faster); hardware optimized; simplified depth (0 to 1)

**Clipping in normalized space:** consistency & simplicity (axis-aligned with plane equations than skewed, perspective dependent frustum); device independence; efficiency



By **racheleva**  
[cheatography.com/racheleva/](https://cheatography.com/racheleva/)

Not published yet.  
Last updated 28th April, 2026.  
Page 1 of 2.

Sponsored by **Readable.com**  
Measure your website readability!  
<https://readable.com>

### 3D projection

#### Perspective Projection

1. find parameter  $t$   $t = \frac{z_p - z_{CoP}}{z - z_{CoP}}$

2. projected  $x'$  and  $y'$   $x' = x_{CoP} + t(x - x_{CoP})$   
 $y' = y_{CoP} + t(y - y_{CoP})$

3. projected  $z'$   $z' = z_p$

#### Orthographic Projection

1. Keep  $x$  and  $y$  unchanged  $x' = x, y' = y$

2. Set  $z$  to projection plane  $z' = z_p$

### Multi-Viewport Viewing Pipeline for CAD

1. **Divergence of Single Modeling Stream** One modeling transformation pipeline (world/model matrix) feeds all viewports.

2. **Viewing & Projection Management** Each viewport has its own: **View Matrix** (camera orientation)  
**Projection Matrix** Orthographic (Top, Front, Side)  
Perspective (3D view)

3. **Clipping per Viewport** Clipping done independently for each viewport (frustum)

#### 4. Overall architecture

Model Transform → Stream Duplication → Parallel Per-Viewport (View+Proj Transform → Clipping → Viewport Transform).

### Multi-Viewport Viewing Pipeline for CAD

1. **Divergence of Single Modeling Stream** One modeling transformation pipeline (world/model matrix) feeds all viewports.

2. **Viewing & Projection Management** Each viewport has its own: **View Matrix** (camera orientation)  
**Projection Matrix** Orthographic (Top, Front, Side)  
Perspective (3D view)



By **racheleva**  
[cheatography.com/racheleva/](https://cheatography.com/racheleva/)

Not published yet.  
Last updated 28th April, 2026.  
Page 2 of 2.

Sponsored by **Readable.com**  
Measure your website readability!  
<https://readable.com>