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Semantics

¬, ∃x, \forall y (Highest, do first)

٨

V

→ (Lowest, do last)

Basic Equivalences	Proof Rules			Proof Rule	s (cont)	CS 310 Lect	ure 5 (cont)
Negation	Conjun-	$A, B / A \wedge b$	В	Contra-	A, ¬ A / False	Terms to	o Element - Each
AL	ction (Conj)			diction		understand	item stored in an
	Simplific-	$A \land B /$	$A \land B /$	(Contr)		the	array is called an
Basic Equivalences	ation	A	В	Indirect	From $\neg A$, derive	Array	element.
Some Conversions	(Simp)	and		Proof (IP)	False / A	Andy.	a laday - Fash
$A \rightarrow B \equiv \neg A \lor B$	Addition	A / \square	B / \square	These are	all fractions with the		o index - Each
$\neg (A \rightarrow B) \equiv A \land \neg B$	(Add)	$\Box VB$	$\Box \lor B$	first term a the second	ppearing on top and d one on the bottom.		element in an
<i>A</i> → <i>B</i> ≡ <i>A</i> ∧¬ <i>B</i> →False	Disjunctive						array has a
∧ and ∨ are associative	Syllogism	$\Box, \neg A/$	$\Box, \neg A /$	/ this slash	denotes where a		numerical index.
$(A \land B) \land C \equiv A \land (B \land C)$	(DS)	В	В	fraction wil	l be located	CS 310 Lect	uro 5
$(A \lor B) \lor C \equiv A \lor (B \lor C)$	Modus	$A, A \rightarrow B /$	В	00.0401	. -		
∧ and ∨ are commutativity	Ponens			CS 310 Le	cture 5	Array Update	Operation
$A \land B \equiv B \land A$	(MP)			Array	A linear data	1. Start	
A∨B≡B∨A	Conditional	FromA, d	erive 🗆	Data Structure	structure defined as a collection of	2. Set LA[K-1] = ITEM	
\wedge and \vee are Distributivity	Proof (CP)	$\Box / A \rightarrow B$				3. Stop	
$A \land (B \lor C) \equiv (A \land B) \lor (A \land C)$	Double	Aרר A / A רר A			same or different	CS 310 Locture 5	
$A \lor (B \land C) \equiv (A \lor B) \land (A \lor C)$	(DN)				data types.		
	()				They exist in both single and multiple dimensions	Common Fea	

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CS 310 Le	ecture 5 (cont)		CS 310 Lecture 5 (cont)	CS 310 Lecture 5	Basic Equ	livalences	
Node: Each element in a I I	>Data: The actual data or value	 >Next Pointer: A reference 	>Various DSs can be implem- ented using an LL, such as stack, queue, graphs, hash, etc.		$A \wedge (A \vee B) =$ $A \vee (A \wedge B) =$	n Laws # A # A	
is repres- ented	associated with the element.	or pointer or	nodes. Last node points to null(address 0)	Doubly-linked list: Inserting at the beginning	$A \wedge (\neg A \lor B)$ $A \lor (\neg A \wedge B)$	$\equiv A \land B$ $\equiv A \lor B$	
by a node, contains two compon		address to the next node in the LL.	CS 310 Lecture 5 Linked List: Traversing all Nodes > Visit each node in a LL: display contents, validate data, etc. Unit for the state of the sta	>The task can be performed by using the following 5 steps: static	Program AA (Assig- nment axiom)	Correctness $\{Q(x/t)\} x = \{Q\}$	5 = t
ents: >Head: T called the starting po >Tail: The	he first node in "head." It serv pint. e last node in a	n a LL is res as the a linked	LIST-Traversal (L) 1. Curr = L.head 2. While Curr.next != NULL 3. PRINT Curr	 >Make the next of new_node point to the current head of the DLL. 	Conseq uence rules (A & B)	$P \rightarrow R$ and {R} $S \{Q\}$ $/ \{P\} \square$ $\square \{Q\}$	$P S$ $T and \square$ $Q /$ $P S$ Q
 Data stru or remove execution. 	d the tail. uctures can be d from the LL	e added to during	CS 310 Lecture 5 Linked List: Searching a Node LIST-Searching (L,k)	>Make the previous of the current head point to new_node.	Loop inva is a condi change a executed	riants: A lo tion that do fter a loop h I.e. P	op invariant es not nas
>Unlike a cally alloca and shrink	n array, LL is ated DS that c 	a dynami- an grow	1. Curr = L.head 2. While Curr != NULL and Curr.key != k	>Lastly, point head to new_node.			
≫No elem after inser	ents need to l tion and deleti	oe shifted on.	3. Curr = Curr.next 4. return Curr	Basic Equivalences Disjunction A v True ≣ True A v False ≣ A			
				$A \lor A \equiv A$			

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A ∨ ¬A ≣ True

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Derived Proo	f Rules	CS 310 Lecture 5	CS 310 Lecture 5	CS 310 Lecture 5
Modus	$A \rightarrow B, \neg B / \neg A$	Operations in Arrays	$\begin{array}{c} & \text{if } \\ & & \\ $	
(MT)		o Traverse – print all the array elements one by one.	Singly Linked List: Every node	>Doubly Linked Lists: Each
Hypoth- etical	$A \to B, B \to$ $C / A \to C$	o Insertion – Adds an element at the given index.	stores the address of the next node in the list and the last node	node has two pointers: one pointing to the next node and
Syllogism (HS)		o Deletion – Deletes an element at the given index.	has the next address NULL.	one pointing to the previous node.
Proof by Cases	$A \lor B, A \to C, \square$ $\square \to C / C$	o Search – Searches an element using the index or value.	CS 310 Lecture 5 Linked List: Operations	both directions.
Cases) Constr-	$A \lor B, A \to C \land B \to D \land$	o Update - Updates an element at the given index.	>Accessing Elements/Traver- sing: Accessing a specific	CS 310 Lecture 5
Dilemma (CD)	C VD	o Display – Displays the contents of the array.	element in a linked list takes O(n) time since nodes are stored in non-contiguous	To insert a note the beginning of a LL
Destructive Dilemma	$A \to B, C \to D,$ $\neg B \lor \neg D / \neg A \lor \neg C$	CS 310 Lecture 5	locations, so random access is not possible.	• To insert a node after a given node in a LL,
(DD)		Array Search Operation	Searching: Searching a node	
		1. Start	in an LL takes O(n) time, as the	LIST-Insert (L,x,k)
CS 310 Lectu	ire 5	2. Set J = 0	whole list needs to be traversed	1. if L.Head == NULL
	Data	3. Repeat steps 4 and 5 while J	in the worst case.	2. L.Head = x and Exit
	Structures	< N	>Insertion: If we are at the	3. While Curr.key !=k and Curr
Linear Da Structur	ata es Data Structures	4. IF LA[J] == ITEM THEN GOTO STEP 6	position where we insert the element, insertion takes O (1)	!=NULL 4. prevN = Curr 5. Curr = Curr Novt
Array	Stack Trees	5. Set $J = J + 1$	time.	6 If PrevN == NULL
List	Queue Graph	6. PRINT J, ITEM	>Deletion a/Destroy the list:	7. x.next = L.Head
		7. Stop	know the element's position to	8. Head = x and exit
			be deleted.	9. PrevN = Curr and Curr =
				Curr.Next
				10. x.Next = Curr

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11. PrevN.Next = x

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CS 310 Lecture 5	Basic Eq	uivalences		Program	Correctness (cont)	Progra	m Correctness (cont)
	Absorptio	on Laws		Compos	$\{P\} S1 \{Q\}$ and	nd { <i>Q</i> }	lf-	$\{P \land C\} S1 \{Q\} and \{P\}$
	$A \land (A \lor B)$	$\equiv A$		ition rule	S2 {R} / {P} [then-	$\land \neg C$ } S2 {Q} / {P} if
	$A \lor (A \land B)$	$\equiv A$			$\Box 1;S2 \{R\}$		else	C then S1 else \Box
Doubly-linked list: Inserting at	$A \land (\neg A \lor B)$	$) \equiv A \wedge B$		lf-then	$\{P \land C\} S$	{ <i>P</i> } if	N/bilo	$\Box \ge \{Q\}$
the end	$A \lor (\neg A \land B)$)≡A∨B		Rule	$\{Q\}$ and \Box $\Box \land \neg C \rightarrow$	then	rule	{ <i>P</i> ∧ <i>C</i> } <i>S</i> { <i>P</i> } <i>I</i> { <i>P</i> } while <i>C</i> do <i>S</i> { <i>P</i>
\gg This can be done using the	Program	Correctnes	e		Q	S		$\land \neg C \}$
following 7 steps:	riogram					{ <i>Q</i> }	Loop ir	nvariants: A loop invariant
>Create a new node (say new_node).	AA (Assig- nment axiom)	$\{Q(xh)\} x =$ $\{Q\}$	= 1				is a con change execute	ndition that does not e after a loop has ed I.e. P
>Put the value in the new node.	Conseq uence	$P \rightarrow R$ and $\{R\}$	$\{P\} S$ $\{T\}$ and \Box					
>Make the next pointer of	rules (A	S {Q}	$\Box \rightarrow Q/$					
new_node as null.	& B)	$/ \{P\} \square$ $\square \{Q\}$	$\{P\} S$ $\{Q\}$					
≫If the list is empty, make		,						
new_node as the head.								

>>Otherwise, travel to the end of the linked list.

>>Now make the next pointer of last node point to new_node.

>Change the previous pointer of new_node to the last node of the list.

Basic Equivalences
Conjunction
A ∧ True ≣ A
A ∧ False ≣ False
$A \land A \equiv A$
A ∧ ¬A ≣ False

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CS 310 Lecture 5	CS 310 Lecture 5 (cont)	CS 310 Lecture 5	Basic Equivalences
Single Dimensional Array See: 9 2 4 5 6 11 2 2 2 2 2 2 2	7. Stop	Linked List: Deleting a Node	Implication
Multi Dimensional Array		previousNode nodePtr IIST-Delete (L, k 1. ifL.Head == NULL 2. Exit 3. Walks Curr key let a	A → True ≡ True
	CS 310 Lecture 5	ist head before the second sec	A → False ≣ ¬A
	$\overset{\text{Not} \rightarrow}{\longrightarrow} 2 \xrightarrow{\rightarrow} 5 \xrightarrow{\rightarrow} 7 \xrightarrow{\rightarrow} 8 \xrightarrow{\rightarrow} 10$	8. delete Head and 9. PrevN Next = Curr.N 10. Delete Curr 10. Delete Curr	^{xxit} True → A ≡ A
CS 310 Lecture 5		list the pards to be delated	False → A ≣ True
Array Deletion Operation	➢Circular Linked Lists: A sircular linked list is a type of		$A \rightarrow A \equiv True$
1. Start	linked list in which the first and	Adjusting pointer around the	
2. Set J = K-1	the last	node to be deleted	Basic Equivalences
3. Repeat steps 4 and 5 while J	nodes are also connected to	LIST-Delete (L_k)	De Morgan's Laws
< N	form a circle. There is no NULL	1. if L.Head == NULL	$\neg (A \land B) \equiv \neg A \lor \neg B$
4. Set LA[J] = LA[J + 1]	at the end.	2. Exit	$\neg(A \lor B) \equiv \neg A \land \neg B$
5. Set J = J+1	CS 310 Lecture 5	3. While Curr.key !=k and Curr	Quantifiore
6. Set N = N-1		!=NULL	Quantiners
7. Stop	head	4. Previv = Curr 5. Curr = Curr Next	"An equivalence to be careful with"
N - is the size of the array		6. If PrevN == NULL	$\exists r(n(r) \Rightarrow q(r)) \equiv \forall rn(r) \Rightarrow$
	Linked List: Empty List	7. Curr = Head.Next	$\exists xq(x) \neq q(x) = \forall xp(x) \neq$ $\exists xq(x)$
CS 310 Lecture 5	>If a list currently contains 0	8. delete Head and exit	
Array Insertion Operation	 >In this case, the list head 	9. PrevN.Next = Curr.Next	Quantifiers
1. Start	points to null		Negations of quantifiers
2. Create an Array of a desired		CS 310 Lecture 5	$\neg(\forall xW) \equiv \exists x \neg W$
datatype and size.	CS 310 Lecture 5	kinde TLis	$\neg(\exists x W) \equiv \forall x \neg W$
3.Initialize a variable 'i' as 0.	Linked List: Appending a Node	Inserting at the beginning of the list	
4. Enter the element at the i-th	€ Curr • • • • • • • • • • • • •	Make T -> next = last -> next. last -> next = T	
index of the array.	list	Insertion at the beginning Is the same as inserting At the end	
5. Increment i by 1			
6. Repeat Steps 4 & 5 until the	list head 23 hull New node i	Circular-linked list operations:	
end of the array.	тенилога	>Insertion: Inserting At the	
	LIST-Append (L; x)	Beginning, at the end, and after	
	1. if L.head == NULL	 Deletion: Deleting from the 	
	 L.head = x and Exit Curr = L head 	Beginning, the end, and a	
	3. While Curr.next != NULL	Specific Node	
	Curr = Curr.next	➢Display: This process displays	
	4. Curr.next = x	the elements of a CLL.	

New Node is added to the end of the list

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Quantifiers	Inference Rules FOPC (cont)	Inference Rules FOPC (cont)	Inference Rules FOPC (cont)
Formalize English sentences and entire arguments into FOPC	EIExistential $W(t)$ /generalization $\exists x W(t)$	EG Existe- $W(t)$ / There ntial $\exists x W($ are	$U(G)$ / Universal $\exists x W(x)$ / $\exists x W$ (Generativer (ization $W(c)$)
$\forall x \text{ quantifies a conditional}$	requires that t x) is free to replace	genera- x) two lization specia	UI & EI Add A and E from
$\exists x$ quantifies a conjunction $\forall x$ with conditional for "all,""every," and "only." $\exists x$ with conjunction for "some,"	<i>x</i> in <i>W</i> (<i>x</i>)	requires cases that □ for □ is EG: free to	away A and E in the problem.
"there is," and "not all." $\forall x$ with conditional or $\neg \exists x$ with		replace <i>x</i> in	1. Start
conjunction for "no A is B." $\exists x \text{ with conjunction or } \forall x \text{ with}$		W(x):	2. Initialize an Array, LA. // 1. Initialize an array called LA
conditional for "not all A's are B."			3. Initialize, i = 0. // 2. Set i - 0
Inference Rules FOPC			4. Print the LA[i] and increment i. // 3. Repeat Steps 4-5 while i < N
UIUniversal $\forall x W($ Thereinstan- x) / \Box aretiation $\Box(t)$ tworequiresspecialthat t casesis free tofor UI:replace x in $W(x)$: $V(x)$	$\forall x W($ $\forall x W($ $x) / \square$ $x) / \square$ $\square (x)$ $\square (c)$		5. Repeat Step 4 until the end of the array. // 4. Print LA[i]

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CS 310 Le	ecture 5 (cor	nt)	CS 310 Lecture 5 (c	cont)	CS 310 Lecture 5
6. End // 5 of i by one // represen	5. Increment e. (Set i = i + nt possible n	the value 1) nodifi-	>Linked >Eac List: A LL node is a linear contai data a data	ch ≫A refere- ins nce(li-	
cations yo still be cou	ou can do tha unted as cor ecture 5	at would rrect	structure field constr- ucted like	add- ress/a- rray-l-	Doubly-linked list: Inserting after a given node
>An abstraction >> An abstraction >> An abstraction abstractio	ract data typ s a data typ me attribute	be (ADT) in c e defined wi s and some	a chain of data _{nodes} th the Where functions	ndices) to the next node	 Firstly create a new node (say
≫An abstract data	≫A list data structure	≫A stack data	≫A queue ^{data} l Inlike Arrays I in	in the list.	new_node). ≫Now insert the data in the new
type in the data structure can be		structure	structure elements are not sto contiguous location.	bred at a	 Node. >Point the next of new_node to the next of prev_node.
				19 null	➢Point the next of prev_node to new_node.
			Doubly-linked list: O ≫Insertion: Inserting	perations g At the	➢Point the previous of new_node to prev_node.
			Beginning, at the en given node, and bef given node.	id, after a fore a	>Change the pointer of the new node's previous pointer to new_node.
			>Deletion: Deleting Beginning, end, and node of the list	from the I a specific	
			>Display: This proc the elements of a do	ess displays bubly LL.	
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