

### Statistical inference

Draw conclusions from a set of data

Put a probability on whether a conclusion is correct 'beyond reasonable doubt'

The major question to answer is whether a difference between samples, or between a sample and a population, has occurred simply as a result of natural variation or because of a real difference between the two

### Two-tailed or one-tailed

The alternative hypothesis may be classified as two-tailed or one-tailed

#### Two-tailed test

- is a two-sided alternative
- we do the test with no preconceived notion that the true value of  $\mu$  is either above or below the hypothesised value of  $\mu_0$
- the alternative hypothesis is written:  $H_1: \mu \neq \mu_0$

#### One-tailed test

- one-sided alternative
- do the test with a strong conviction that, if  $H_0$  is not true, it is clear that  $\mu$  is either greater than  $\mu_0$  or less than  $\mu_0$
- E.g. the alternative hypothesis is written as:  $H_1: \mu > \mu_0$

### Decision-making process steps

1. Collecting the data
2. Summarising the data
3. Setting up a hypothesis (i.e. a claim or theory), which is to be tested
4. Calculating the probability of obtaining a sample such as the one we have if the hypothesis is true
5. Either accepting or rejecting the hypothesis

### Significance level

After the appropriate hypotheses have been formulated, we must decide upon the significance level (or  $\alpha$ -level) of the test

most common significance level used is 0.05, commonly written as  $\alpha = 0.05$

A 5% significance level says in effect that an event has occurred that occurs less than 5% of the time is considered unusual

### One-sample z-test

Deals with the case of a single sample being chosen from a population and the question of whether that particular sample might be consistent with the rest of the population

Construct a test statistic according to a particular formula

Information required in calculation

- the size (n) of the sample
- the mean of the sample
- the standard deviation (s) of the sample

Other information of interest might include:

- Does the population have a normal distribution?
- Is the population's standard deviation known?
- Is the sample size (n) large? (25+)

There are different cases for the one-sample z-test statistic

#### Case I

the population has a normal distribution and the population standard deviation,  $\sigma$ , is known

#### Case II

the population has any distribution  
the sample size, n, is large (i.e. at least 25), and  
the value of population standard deviation is known

*In both these cases we can use a z-test statistic formula (a)*

#### Case III

the population has any distribution  
the sample size, n, is large (i.e. at least 25), and

### One-sample z-test (cont)

the value of population standard deviation is unknown (however, since n is large, the value of population standard deviation is approximated by the sample standard deviation, s)

*In this case we can use a z-test statistic formula (b)*

### Set up your Hypothesis

#### Null Hypothesis

Part of formulation of an hypothesis

Statement that nothing unusual has occurred

The notation is  $H_0$

#### Alternative hypothesis

States that something unusual has occurred

The notation is  $H_1$  or  $H_A$

**Together** they may be written in the form:  
 $H_0$ : (statement) v.  $H_1$ (alternative statement)

### Conclusion errors

Two possible errors in making a conclusion about a null hypothesis

Type I errors occur when you reject  $H_0$  (i.e. conclude that it is false) when  $H_0$  is really true.

Type II errors occur when you accept  $H_0$  (i.e. conclude that it is true) when  $H_0$  is really false.

### z-test statistic formula (a)

$$Z = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$$

### z-test statistic formula (b)



By **Natalie Moore**  
(NatalieMoore)

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