

Quadratic Equation

$$\text{Roots of } ax^2 + bx + c = 0 \text{ are } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\text{Sum of roots } x_1 + x_2 = -\frac{b}{a};$$

$$\text{Product of roots } x_1 x_2 = \frac{c}{a}$$

For real roots, $b^2 - 4ac \geq 0$

For imaginary roots, $b^2 - 4ac < 0$

Logarithm

$$\log_{10} N = x \Rightarrow 10^x = N$$

$$\log_a N = \log_a b * \log_b N$$

$$\log_1 1 = 0, \log_a a = 1$$

$$\log mn = \log m + \log n \quad \log \frac{m}{n} = \log m - \log n$$

$$\log m^n = n \log m \quad \log_m n = 2.303 \log_{10} m$$

$$\log 2 = 0.3010 \quad \log 3 = 0.4771$$

Arithmetic Progression

a, a+d, a+2d, a+3d,a+(n-1)d
here d = common difference

$$\text{Sum of n terms } S_n = \frac{n}{2} [2a + (n-1)d]$$

$$n^{\text{th}} \text{ term, } a_n = a + (n-1)d$$

Geometric Progression

a, ar, ar², ar³, here, r = common ratio

$$n^{\text{th}} \text{ term, } a_n = a \cdot r^{n-1}$$

$$\text{Sum of n terms } S_n = \frac{a(1-r^n)}{1-r}$$

$$\text{Sum of } \infty \text{ terms } S_\infty = \frac{a}{1-r} \quad [\text{where } |r| < 1]$$

Cosine Rule

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}, \cos B = \frac{c^2 + a^2 - b^2}{2ca}, \cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

Sine Rule

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

Binomial Theorem

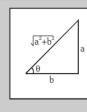
$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2} x^2 + \frac{n(n-1)(n-2)}{6} x^3 + \dots$$

$$(1-x)^n = 1 - nx + \frac{n(n-1)}{2} x^2 - \frac{n(n-1)(n-2)}{6} x^3 + \dots$$

If $x \ll 1$ then $(1+x)^n \approx 1 + nx$ & $(1-x)^n \approx 1 - nx$

Trigonometry I

$\sin \theta = \frac{\text{perpendicular}}{\text{hypotenuse}}$	$\cos \theta = \frac{\text{base}}{\text{hypotenuse}}$	$\tan \theta = \frac{\text{perpendicular}}{\text{base}}$
$\cot \theta = \frac{\text{base}}{\text{perpendicular}}$	$\sec \theta = \frac{\text{hypotenuse}}{\text{base}}$	$\cosec \theta = \frac{\text{hypotenuse}}{\text{perpendicular}}$
$\sin \theta = \frac{a}{\sqrt{a^2 + b^2}}$	$\cos \theta = \frac{b}{\sqrt{a^2 + b^2}}$	$\tan \theta = \frac{a}{b}$
$\cosec \theta = \frac{1}{\sin \theta}$	$\sec \theta = \frac{1}{\cos \theta}$	$\cot \theta = \frac{1}{\tan \theta}$



Trigonometry II

$$\begin{aligned} \sin^2 \theta + \cos^2 \theta &= 1 & 1 + \tan^2 \theta &= \sec^2 \theta & 1 + \cot^2 \theta &= \cosec^2 \theta \\ \sin(A+B) &= \sin A \cos B + \cos A \sin B & \tan(A \pm B) &= \frac{\tan A \pm \tan B}{1 - \tan A \tan B} & \cos(A+B) &= \cos A \cos B - \sin A \sin B \\ \tan(A+B) &= \frac{\tan A + \tan B}{1 - \tan A \tan B} & \sin 2A &= 2 \sin A \cos A & & \\ \cos 2A &= \cos^2 A - \sin^2 A = 1 - 2 \sin^2 A = 2 \cos^2 A - 1 & \cos 2A &= \frac{1 - \tan^2 A}{1 + \tan^2 A} & & \\ 2 \sin 2A &= 2 \sin A \cos A & \sin 3A &= 3 \sin A - 4 \sin^3 A & & \\ \cos 3A &= 4 \cos^3 A - 3 \cos A & 2 \sin A \sin B &= \cos(A-B) - \cos(A+B) & & \\ 2 \cos A \cos B &= \cos(A-B) + \cos(A+B) & 2 \sin A \cos B &= \sin(A+B) + \sin(A-B) & & \end{aligned}$$

Trigonometry III



Trigonometry IV

θ	0°	30°	45°	60°	90°	120°	135°	150°	180°	270°	360°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	-1	0
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	0	$\frac{1}{2}$	- $\frac{1}{2}$	$-\frac{1}{\sqrt{2}}$	$-\frac{\sqrt{3}}{2}$	-1	0	1
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞	- $\sqrt{3}$	-1	$-\frac{1}{\sqrt{3}}$	0	∞	0

Trigonometry V

$$\begin{array}{llll} \sin(90^\circ + \theta) = \cos \theta & \sin(180^\circ - \theta) = \sin \theta & \sin(-\theta) = -\sin \theta & \sin(90^\circ - \theta) = \cos \theta \\ \cos(90^\circ + \theta) = -\sin \theta & \cos(180^\circ - \theta) = -\cos \theta & \cos(-\theta) = \cos \theta & \cos(90^\circ - \theta) = \sin \theta \\ \tan(90^\circ + \theta) = -\cot \theta & \tan(180^\circ - \theta) = -\tan \theta & \tan(-\theta) = -\tan \theta & \tan(90^\circ - \theta) = \cot \theta \\ \sin(180^\circ + \theta) = -\sin \theta & \sin(270^\circ - \theta) = -\cos \theta & \sin(270^\circ + \theta) = -\cos \theta & \sin(360^\circ - \theta) = -\sin \theta \\ \cos(180^\circ + \theta) = -\cos \theta & \cos(270^\circ - \theta) = \sin \theta & \cos(270^\circ + \theta) = -\sin \theta & \cos(360^\circ - \theta) = \cos \theta \\ \tan(180^\circ + \theta) = \tan \theta & \tan(270^\circ - \theta) = \cot \theta & \tan(270^\circ + \theta) = -\cot \theta & \tan(360^\circ - \theta) = -\tan \theta \end{array}$$

For Small Theta

$$\sin \theta \approx 0 \quad \cos \theta \approx 1 \quad \tan \theta \approx 0 \quad \sin \theta \approx \tan \theta$$

Average of a Varying Quantity

$$\text{If } y = f(x) \text{ then } \langle y \rangle = \bar{y} = \frac{\int_a^b y dx}{b-a} = \frac{\int_a^b f(x) dx}{b-a} = \frac{x_2 - x_1}{b-a}$$

Integration

- C = Arbitrary constant, k = constant
- $\int f(x) dx = g(x) + C$
- $\frac{d}{dx} (g(x)) = f(x)$
- $\int kf(x) dx = k \int f(x) dx$
- $\int (u+v+w) dx = \int u dx + \int v dx + \int w dx$
- $\int e^x dx = e^x + C$
- $\int x^n dx = \frac{x^{n+1}}{n+1} + C, n \neq -1$
- $\int \frac{1}{x} dx = \ln x + C$
- $\int \sin x dx = -\cos x + C$
- $\int \cos x dx = \sin x + C$
- $\int e^{ax+b} dx = \frac{e^{ax+b}}{a} + C$
- $\int (ax+b)^n dx = \frac{(ax+b)^{n+1}}{a(n+1)} + C$

Differentiation

- $y = x^n \rightarrow \frac{dy}{dx} = nx^{n-1} \quad \bullet y = mx \rightarrow \frac{dy}{dx} = \frac{1}{x}$
- $y = \sin x \rightarrow \frac{dy}{dx} = \cos x \quad \bullet y = \cos x \rightarrow \frac{dy}{dx} = -\sin x$
- $y = e^{ax+b} \rightarrow \frac{dy}{dx} = ae^{ax+b} \quad \bullet y = uv \rightarrow \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$
- $y = f(g(x)) \rightarrow \frac{dy}{dx} = \frac{df}{dg} \frac{dg}{dx} = \frac{df(g(x))}{dg(x)} \times \frac{dg(g(x))}{dx}$
- $y = k(\text{constant}) \rightarrow \frac{dy}{dx} = 0$
- $y = \frac{u}{v} \rightarrow \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$

Maxima and Minima

$$\begin{array}{l} \text{For maximum value } \frac{dy}{dx} = 0 \text{ & } \frac{d^2y}{dx^2} < 0 \\ \text{For minimum value } \frac{dy}{dx} = 0 \text{ & } \frac{d^2y}{dx^2} > 0 \end{array}$$

Componendo & Dividendo Theorem

$$\text{If } \frac{p}{q} = \frac{a}{b} \text{ then } \frac{p+q}{p-q} = \frac{a+b}{a-b}$$

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