## Reliability

## Rseries $=R^{n}$

Rparallel = $1-(1-R)^{n}$
2 Parallel Components in Series $=\left(1-(1-R)^{2}\right)^{2}$
2 Series Components in Parallel $=1-\left(1-R^{2}\right)^{2}$
Legitimate Values of $R 0<=R<=1$
Consider $f(R)=R(2-R)$ where does $f(R)$ achieve it's max and what' the max value?
$g(R)=R\left(2-R 0=2 R-R^{2}\right.$ taking it's derivative and setting equal to 0 we get
$d g(R) / d R=2-2 R=0$ Its max is achieved when $R=1$
Plugging this in for $R$ in $g(R)$ yields $2-1=1>0$
k out of $\mathbf{N}$ Redundancy - system that operates if at least $k$ out of $N$ components function properly.
$R=$ Sum(l=k to $n$ ) of $R^{I}(1-R)^{n-i}$ (ex Sum(l=2 to 3(for ito 3)(.0.9) $)^{i}(-$ $0.1)^{\wedge} 3$-i)

## Economic Analysis

How much would you need to invest on September 27th, 2019 to have \$10,000 on September 27th, 2027 given an interest rate of 5\%?
$P V=F V(P / F, i, n)=10 k(P / F, 5,7)$
How much would you need to deposit on January 1, 2020 in a fund that yields $5 \%$ annually in order to draw out $\$ 250.00$ at the end of each year starting December 31, 2020 for 7 years, leaving nothing in the fund at the end?
PV=250(P/A,5\%,7)
Dominate - when one of the outcome paths is clearly the better choice for every case

## Review Session Material

P34 = P[In State 4|Current State] - Take Pmatrix to the 4th power and look at position 34.
$\operatorname{EMV}(\mathrm{i})=\operatorname{SUM}(\mathrm{j}=1$ to N$) \mathrm{Pj}^{\star}$ rij
How much does P have to change before another alternative is best.
Add $a z$ to one state and subtract $z$ from another state, then set the equations $=$ to each other and solve for $z$. If $z$ is $(-)$ then it's not better.
EV of Perfect information means you take the largest value at each state and multiply it by it's probability.
Expected Loss of Sales cost (When D exceeds inventory)
E[lost sales cost | Demand=d,Inv=I]
MAX(d-i,0)
To remove a condition
E[lost sales] = SUM(d=0 to nd)SUM(I=0 to ni)max(d-i, 0 ) $\operatorname{Pd}(\mathrm{d})^{*} \mathrm{Pi}(\mathrm{i})$
Can also use PMF (PI)

## Markov Case

Markov Case Stochastic process where we only take into account the present to predict the future. That is the probability of going to state $j$ (future) from state I(present)
-If there is one (and only one) closed, aperiodic communicating class, the process is ergodic.
$\mathrm{Pi}(\mathrm{n})=\mathrm{P}[$ In state after transitions $]$
$\operatorname{Pi}(1)=\operatorname{Pi1}(0) p 11+\operatorname{Pi} 2(0) P 21+\ldots+\operatorname{Pin}(0)^{*} \operatorname{Pn1}$

## Floyd's Barbershop

Haircuts take exactly 15 min , we have
r.v. $\mathrm{Y}=$ \# customers who arrive during a 15 m interval

Haircuts cost 10; each customer consumes $\$ 1$ of snacks every
15min
$\mathrm{Pi}(\mathrm{n})=\mathrm{Pi}(\mathrm{n}-1)^{*} \mathrm{P}$
$=P i(0) * p^{n}$
Q1 - We have 3 customers in the shop, what's the Probability there will be 4 customers in the shop 4 periods from now? A - $\mathrm{P}^{4} 34$
What is the probability in the long run, a customer comes to the shop but leaves because there is no seat available?
P[A]=SUM(I=0 to 4]P(A|Statei)*P(Statei)
What is the Long run expected number of customers that come to the shop but leaves? $\mathrm{E}[\mathrm{A}]=\mathrm{SUM}(\mathrm{I}=1$ to n$) \mathrm{E}[\mathrm{A} \mid \mathrm{B}]^{*} \mathrm{P}[\mathrm{Bi}]$
$\mathrm{E}[\mathrm{a}$ |state $=0]=0(.2)+0(.7) \ldots \ldots$

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