

### Periodic Functions

Periodic Function: repeats a pattern of y-values (outputs) at regular intervals  
 Cycle: may begin at any point in a graph  
 Period: is the horizontal length of one cycle.

### Special Right Angles

#### 45-45-90

$h = \text{sqrt } 2 \text{ times } /$

#### 30-60-90

$h = 2 \text{ times } s$

$l = \text{sqrt } 3 \text{ times } s$

$s = \text{short leg}$

$l = \text{long leg}$

### Properties Of Sine Functions

$y = a \sin b \theta$

period =  $2\pi/b$

$|a| = \text{amplitude}$

$b = \text{number of cycles (0 to } 2\pi)$

### Quadratic Functions

#### Standard Form

$f(x) = ax^2 + bx + c$

$ax^2$

Quadratic term

$bx$

Linear term

$c$

constant term

### Exponential Growth & Exponential Decay

$b = 1 + r$

$b > 1 = \text{epon. growth}$

When  $b < 1$ ,  $b$  is a decay factor

x-axis = asymptote

$0 < b < 1$

$b = 1 + (-r)$

### Exponential Growth & Exponential Decay (cont)

$y = ab^x$

$b = \text{growth factor}$

$r = \text{increase in rate}$

### e & Its Importance

$A = Pe^{rt}$

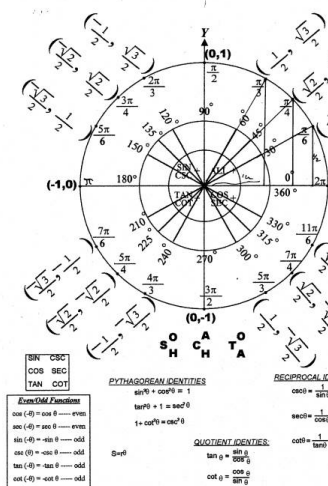
$A = \text{amount in account}$

$P = \text{principal (what you start with)}$

$r = \text{rate in interest (annually)}$

$t = \text{time (in years)}$

### Unit Circle



radian  $2\pi$ , tangent 0  
 radian  $\pi/6$ , tangent  $\text{sqrt } 3/3$   
 radian  $\pi/4$ , tangent 1  
 radian  $\pi/3$ , tangent  $\text{sqrt } 3$   
 radian  $\pi/2$ , tangent undefined  
 radian  $2\pi/3$ , tangent  $-\text{sqrt } 3$   
 radian  $3\pi/4$ , tangent -1  
 radian  $5\pi/6$ , tangent  $-\text{sqrt } 3/3$   
 radian  $\pi$ , tangent 0  
 radian  $7\pi/6$ , tangent  $\text{sqrt } 3/3$   
 radian  $5\pi/4$ , tangent 1  
 radian  $4\pi/3$ , tangent  $\text{sqrt } 3$   
 radian  $3\pi/2$ , tangent undefined  
 radian  $5\pi/3$ , tangent  $-\text{sqrt } 3$   
 radian  $7\pi/4$ , tangent -1  
 radian  $11\pi/6$ , tangent  $\text{sqrt } 3/3$

### Sine, Cosine, Tangent

Sine = opp./adj.

Cosine = Adj./Hypo.

Tangent = Opp./Adj.

### Mazimun & Minimum

$y = ax^2 + bx + c$

AOS:  $x = -b/2a$

1. vertex

2. c

3. another point

Area = length times width

### Trigonometric Identities

#### Reciprocal Identities

$\csc \theta = 1/\sin \theta$

$\sec \theta = 1/\cos \theta$

$\cot \theta = 1/\tan \theta$

#### Tangent & Cotangent Identities

$\tan \theta = \sin \theta / \cos \theta$

$\cot \theta = \cos \theta / \sin \theta$

#### Pythagorean Identities

$\cos^2 \theta + \sin^2 \theta = 1$

$1 + \tan^2 \theta = \sec^2 \theta$

$1 + \cot^2 \theta = \csc^2 \theta$

### Angle Identities

#### Angle Difference Identities

$\sin(A-B) = \sin A \cos B - \cos A \sin B$

### Angle Identities (cont)

$\cos(A-B) = \cos A \cos B + \sin A \sin B$

$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$

$\tan B$

$\tan B$

#### Angle Sum Identities

$\sin(A+B) = \sin A \cos B + \cos A \sin B$

$\sin B$

$\cos(A+B) = \cos A \cos B - \sin A \sin B$

$\sin B$

$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$

$\tan B$

### Identities

#### Double-Angle Identities

$\cos 2x = \cos^2 x - \sin^2 x$

$\cos 2x = 2\cos^2 x - 1$

$\cos 2x = 1 - 2\sin^2 x$

$\sin 2x = 2\sin x \cos x$

$\tan 2x = \frac{2\tan x}{1 - \tan^2 x}$

#### Half Angle Identities

$\sin A/2 = \pm \sqrt{1 - \cos A/2}$

$\cos A/2 = \pm \sqrt{1 + \cos A/2}$

$\tan A/2 = \pm \sqrt{1 - \cos A / 1 + \cos A}$

### Logarithms

- to base  $b$  of a positive number  $y$  is defined as...

If  $y = ab^x$ , then  $\log_b y = x$

#### Log In Life

$\text{pH} = -\log[\text{H}^+]$

**$b$  is not equal to 1**

**$b$  must be positive**

**log of 0 or negative number = undefined**

$\log = \log \text{ base } 10$

### Log Are Inverses Of Exponentials

1. Graph exponential function
2. Graph  $y = x$
3. Reflect exponential function over  $y = x$  (reverse coordinates)

### Solving Log Equations (cont)

Solve  $2\log x - \log 3 = 2$   
 $\log(x^2/3) = 2$   
 $x^2/3 = 10^2$   
 $x^2 = 2(100)$   
 $x = 10\sqrt{2}$  or 17.32

### Properties Of Log

$\log_b MN = \log_b M + \log_b N$  <----  
product property  
 $\log_b M/N = \log_b M - \log_b N$  <----  
Quotient property  
 $\log_b M^x = x \log_b M$  <----Power  
property

### WATCH OUT FOR ERRORS

$\log_b a/\log_b c$  does not equal  
 $\log_b a/c$

$\log_b a$  times  $c$  does not equal  
 $\log_b a$  times  $\log_b c$

### Pairs Of Relations are Inverse Of Each Other

$y = x - 7/2$   
 $y = 2x + 7$   
 $y = 3x - 1$   
 $y = x + 1/3$   
 $y = -x + 4$   
 $y = -x + 4/-1$   
 $y = x + 4/5$   
 $y = 5x - 4$

### Expanding Log

$$\log_2 7b = \log_2 7 + \log_2 b$$

left to right = expand

right to left = simplify

### Natural Log

Write  $3\ln 6 - \ln 8$  as a single  
natural log  
 $\ln 6^3/8 \rightarrow \ln 216/8 \rightarrow \ln 27$

### Solving Log Equations

Pt 1  
solve  $\log(3x+1) = 5$   
 $3x+1 = 10^5$   
 $3x+1 = 100000$   
 $3x = 99,999$   
 $x = 33,333$   
Pt 2

