## Probability and its notations

| Determ- | outcome can be predicted |
| :--- | :--- |
| inistic | exactly in advance |
| processes |  |

Random processes

Probability
outcome is not known exactly (can desc the probability distribution of possible outcomes)
of event A
Probability $\quad P(S)=1, P(A)+P(B)+P(C)=1$ of whole
sample space

Event $A$ will $\quad P(A)=0$
almost
definitely
not occur
Only small chance that event A will occur

| 50-50 <br> chance that event $A$ will occur | $P(A)=0.5$ |
| :---: | :---: |
| Strong chance that event A will occur | $P(A)=0.9$ |
| Event A will almost definitely occur | $P(A)=1$ |

Probability
successful
outcome (S)

Permutations

Combin- Order is not important
ations
Permutation $n^{\wedge} r$
with
repetition
Permutation $n!/(n-r)$ !
without
repetition

## Probability and its notations (cont)

Probability events $P(A \cap B)$
A and B both occur
Events $A$ and $B \quad P\{A \mid B\}=0, P\{A \cap B\}=0$
are mutually
exclusive or
disjoint cannot
occur at the same
time
Probability events $\quad P(A \cup B)$
A or B occur
Conditional $\quad \mathrm{P}(\mathrm{A} \mid \mathrm{B})$
probability (event
A occurs, given
that event $B$ has
occured)
Independent
$P\{A \mid B\}=P(A)$
(event A does not
change the
probability of event
B)

Complement
(event that not
occuring)
Rule of subtraction $\quad P(A)=1-P\left(A^{\prime}\right)$
(event A will occur)
Rule of multiplic-
$P(A \cap B)=P(A) x$
ation (probability of
$P(B \mid A)$
the intersection of
two events)
Rule of addition
(either event
occurs, not
mutually exclusive)
$P(A \cup B)=P(A)+P(B)$

- ( $\mathrm{P}(\mathrm{A}) \times \mathrm{P}(\mathrm{B} \mid \mathrm{A}))$

| Random variable | determined by a <br> chance event, <br> outcome of a random <br> experiment, <br> measurable real-v- <br> alued |
| :--- | :--- |
| Discrete random | range of $X$ is finite ot <br> countably infinite <br> (values $X$ can take <br> on, not the size of the <br> values) |


| Probability and its notations (cont) |  |
| :---: | :---: |
|  | of $X$ is uncountably (that makes a physical rement) |
| Bayes' Theorem |  |
| Mutually exclus- $\quad \mathrm{P}(\mathrm{A} u \mathrm{~B})=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})$ive/disjoint (if bothevents cannotoccur together) |  |
| Collectively $\quad$ AUB $=S$exhaustive (if atleast one of theevents must occur) |  |
| Events $A$ and $B$ are $P(A \cap B)=P(A) \times P(B)$independent |  |
| Events $A$ and $B$ are not independent | $\begin{aligned} & P(A \cap B)=P(A) x \\ & P(B \mid A) \end{aligned}$ |
| Conditional $P(A \mid B)=P(A, B) /$ <br> probability of $A$ $P(B)$ <br> given $B$  |  |
| If $A$ and $B$ are $P(A \mid B)=(P(A) x$ <br> statistically indepe-- $P(B)) / P(B)=P(A)$ <br> ndent  |  |
| if $A$ and $B$ are $\quad P(A \mid B)!=P(A)$statisticallydependent |  |
| Multiplication rule for conditional probabilities | $\begin{aligned} & P(A \cap B)=P(B) x \\ & P(A \mid B) \text { or } P(A \cap B)= \\ & P(A) \times P(B \mid A) \end{aligned}$ |
| Bayes Theorem | $\begin{aligned} & \mathrm{P}(\mathrm{~A} \mid \mathrm{B})=(\mathrm{P}(\mathrm{~B} \mid \mathrm{A}) \mathrm{x} \\ & \mathrm{P}(\mathrm{~A})) / \mathrm{P}(\mathrm{~B}) \end{aligned}$ |
|  | $\begin{aligned} & \mathrm{P}(\mathrm{~S} \mid \mathrm{F})=(\mathrm{P}(\mathrm{~F} \mid \mathrm{S}) \mathrm{x} \\ & \mathrm{P}(\mathrm{~S})) /(\mathrm{P}(\mathrm{~F} \mid \mathrm{S}) \mathrm{x} \\ & \mathrm{P}(\mathrm{~S}))+\left(\mathrm{P}\left(\mathrm{~F} \mid \mathrm{S}^{\prime}\right) \mathrm{x}\right. \\ & \left.\mathrm{P}\left(\mathrm{~S}^{\prime}\right)\right) \end{aligned}$ |
| Prior probability | originally obtained before any additional information is obtained |
| Posterior probability | has been revised by using additional information that is later obtained |

Combin-$(r+n-1)!/ r!(n-1)!$
ation with
repetition
Combin- $n!/(n-r)!$
ation
without
repetition
n : number of things to
choose from ; r: them are
chosen

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