### Cheatography

# Economic Statistics - Midterm 2.2 Cheat Sheet by lunarorbit via cheatography.com/216484/cs/47304/

## Probability basics (definitions & rules)

**Probability Basics** 

#### What probability actually means:

- Probability is a number that tells you how likely something is to happen.
- It's always between 0 and 1:
- ▶ 0 = impossible
- ▶ 1 = guaranteed
- ► 0.5 = 50% chance

You can think of probability as the **long-run frequency** of something happening if you repeated it a bunch of times.

Example: if you flip a fair coin 1,000 times, about half the flips will be heads → P(Heads)=0.5.

### Key probability symbols

 Event: any outcome or collection of outcomes you're interested in.

Example: "Rolling an even number" on a die  $\rightarrow$  that's the event A = {2, 4, 6}.

 Sample space (S): all possible outcomes.

Example: rolling a die  $\rightarrow$  S = {1, 2, 3, 4, 5, 6}.

• P(A): "The probability that event A happens."

Example: P(Even)=3/6=0.5.

### Types of events

- Disjoint / mutually exclusive: can't happen at the same time. Example: "Rolling a 3" and "Rolling a 4."
- Independent: one happening doesn't change the chance of the other.

Example: Coin toss and rolling a die — they don't affect each other.

#### Example: "At least one"

"If there's a 0.004 chance a test gives a false positive, what's the probability that at least one out of 200 tests is a false positive?" This uses the **complement rule**— it's easier to find the chance that none are false positives, then subtract from 1.

P(At least one)=1−P(None)
Each test has a 0.996 chance of being fine →
P(None)=0.996^200
So P(At least one)=1−0.996^200

### Random Variables (RVs)

What they are

A random variable is just a number that represents the outcome of something random. Example:

Toss a coin twice.

X = number of heads.

Possible X values: 0, 1, or 2. We can describe all the possible values of X and how likely they are. That list is called a **probability distribution**.

### Probability distribution

A table or formula showing: Every possible value of X The probability of each value Must satisfy:

- 1. All probabilities are between 0 and 1.
- 2. They add up to 1.

### Mean (Expected Value)

The expected value (E[X]) or mean ( $\mu$ x) tells you the average outcome in the *long run*.  $E[X] = \sum (x \times P(X=x))$  Example (from table above):

E[X]=0(0.25)+1(0.50)+2(0.25)=1  $\rightarrow$  On average, 1 head per 2 flips.

### Variance & Standard Deviation

 $Var(X) = \sum (x-\mu)^2 P(X=x) / SD(X) = \sqrt{Var(X)}$ 

Variance = average of squared distances from the mean.

Standard deviation = average distance.

If SD is small → values are close to the mean.

### **Useful shortcuts**

- *E*[*aX+b*]=*aE*[*X*]+*b* (Multiply and add constants outside the expectation.)
- Var(aX+b)=a² Var(X)
   (Adding doesn't affect spread, multiplying stretches it.)
- *E[X+Y]=E[X]+E[Y]*
- If X and Y independent:Var(X+Y)=Var(X)+Var(Y)
- If correlated: Var(X+Y) =
   Var(X)+Var(Y)+2ρσxσy
   (ρ = correlation between X and Y)

### **Example: Lottery**

You buy a \$1 ticket that pays \$500 if you win (probability = 1/1000). If you lose, you get \$0.

E[X]=(499)(0.001)+(-1)(0.99-9)=-0.5

You lose 50¢ on average each play → expected loss.

## Sampling & Sampling Distributions

### Population vs Sample

- Population: the entire group you care about (all students in a school).
- Sample: the smaller group you actually measure (30 students). We use samples to estimate the truth about populations.



By **lunarorbit** cheatography.com/lunarorbit/

Not published yet. Last updated 6th November, 2025. Page 1 of 2. Sponsored by Readable.com Measure your website readability! https://readable.com

### Cheatography

### Economic Statistics - Midterm 2.2 Cheat Sheet

by lunarorbit via cheatography.com/216484/cs/47304/

### Types of samples

- Simple Random Sample (SRS): every individual has an equal chance of being chosen.
- Stratified sample: population divided into groups (strata) → random sample from each.
- Cluster / multistage: randomly pick clusters, then pick within them.

△□ Voluntary response or convenience samples are biased! (not random → results unreliable).

### Sampling distribution

If you take many random samples and compute a statistic (like a mean or proportion) for each sample, the distribution of those statistics is the sampling distribution.

We study its:

- Center: average (should equal population value if unbiased)
- **Spread**: how much sample results vary
- Shape: often becomes bell-shaped for large samples

### **Unbiased estimator**

A statistic is **unbiased** if its sampling distribution's center equals the true population parameter.

 $E[\bar{X}] = \mu$  and  $E[\hat{p}] = p$ Unbiased means, "on average, it hits the right answer."

### How sample size affects variability

Bigger sample  $\rightarrow$  smaller variability (less spread).  $SD(\bar{X}) = \sigma/\sqrt{n}$  As n increases, denominator gets bigger  $\rightarrow$  SD gets smaller.

## Law of Large Numbers & Central Limit Theorem

### Law of Large Numbers

When you take more and more samples, the sample mean  $\bar{X}$  will get closer and closer to the population mean  $\mu$ .

Example: the average of 10 coin flips might not be 0.5, but the average of 10,000 flips almost definitely will be close to 0.5.

### Central Limit Theorem (CLT)

This is *super important* for exams.

Even if the original population is not Normal, when you take a large enough sample, the distribution of sample means will look Normal (bell-shaped).

 $\bar{X} \sim N(\mu, \sigma/\sqrt{n})$  Meaning:

Centered at  $\mu$  (the true mean)

Spread =  $\sigma/\sqrt{n}$ 

### Why it matters

CLT lets you use **z-scores** and Normal tables to find probabilities for sample means. \*z = sample mean -  $\mu / \sigma / \sqrt{n}$ ) Then use the z-table (or calculator) to find probabilities.

### Example (CLT in action)

A machine fills cereal boxes.  $\mu = 500g, \ \sigma = 10g.$  Sample 25 boxes.  $SD(\bar{X}) = 10/\sqrt{25} = 2$   $P(\bar{X} < 496) = P(Z < 496\text{-}500/2) = P(Z < -2) = 0.0228$   $\rightarrow 2.28\% \text{ chance the sample}$ 

average weight is below 496g.

### Probability rules

RULE	MEANING	FORMULA	EX
1. Range	Probabilities go from 0 to 1	0sP(A)s1	A 70% chan not 1.3
2. Whole Sample	All outcomes together have probability 1		Somethin
3. Addition (Disjoint)	If A and B can't both happen, add them	P(A or B)=P(A)+P(B)	Rolling a 3 d → 1/6
4. Complement	Opposite events add to 1	P(A^c)=1-P(A)	If 30% rail
5. General Addition	If A and B can overlap	P(A or B)=P(A)+P(B) -P(A and B)	Subtract o doubl

### Probability Distribution Chart

x	P(X)

## Quick strategy for exam problems

	WHAT TO CHECK	
	Identify if question is about sin (probability), random variables (expectation/variance), or sam (means/proportions).	
	Draw or imagine the sample sp the possible outcomes?	
3.	If you see words like "at least," use probability rules (addition	
4.	If you see "average of samples of successes," use sampling for	
5.	Convert to z-score when findir of sample means or proportion	
6.	Watch for independence: if evi independent, you can't multiply probabilities.	

#### **Formula Summary**

		MEANING
Probability of A	P(A)	Likelihood that
Complement	P(A^c)=1-P(A)	Probability th happen
Addition (disjoint)	P(A or B)=P(A)+P(B)	If events can'
Addition (general)	P(A or B)=P(A)+P(B)-P(A and B)	Subtract over
Independence	P(A and B)=P(A)P(B)	Only if A, B in
Expected value	$E[X] = \sum xP(X = x)$	Long-run ave
Variance	$Var(X)=\sum (x-\mu)^2 P(X=x)$	Spread aroun
Standard deviation	$SD(X) = \sqrt{Var(X)}$	Average dista
Linear rules	E[aX+b]=aE[X]+b, Var(aX- +b)=a <sup>2</sup> Var(X)	Adjust for sca
Sample mean	$E[\bar{X}] = \mu,  SD(\bar{X}) = \sigma/\sqrt{n}$	Mean & spres means
Sample proportion		Mean & sprea proportions
Z-score (sampling)	z = sample mean - μ/sd	Converts to S for probability



By **lunarorbit** cheatography.com/lunarorbit/

Not published yet. Last updated 6th November, 2025. Page 2 of 2. Sponsored by **Readable.com**Measure your website readability!
https://readable.com