

# Integral Calculus (Various) Cheat Sheet by Lipsum via cheatography.com/151963/cs/42793/

### Derivatives

- Power Rule:  $\frac{d}{dx}(x^n) = nx^{n-1}$
- Product Rule: (uv)' = u'v + uv'
- Quotient Rule:  $\left(\frac{u}{v}\right)' = \frac{u'v uv'}{v^2}$
- Chain Rule:  $\frac{d}{dx}(f(g(x))) = f'(g(x)) \cdot g'(x)$

### Trigonometric Identities

- Pythagorean Identities:  $\sin^2(x) + \cos^2(x) = 1$
- Sum and Difference Identities:  $\sin(x\pm y)=\sin(x)\cos(y)\pm\cos(x)\sin(y)$
- \* Double Angle Identities:  $\sin(2x) = 2\sin(x)\cos(x)$

### Logarithmic Properties

- - Product Rule:  $\log_1(xy) = \log_1(x) + \log_1(y)$
  - Quotient Rule:  $\log_b\left(\frac{x}{y}\right) = \log_b(x) \log_b(y)$
  - Power Rule:  $\log_b(x^n) = n \log_b(x)$

### Approximating Area Under a Curve

- The region is expression to the state of th Trapezoidal Rule:
- Trapezoidal Rule =  $\frac{\Delta x}{2}[f(a) + 2f(x_1) + 2f(x_2) + ... + 2f(x_{n-1}) + f(b)]$
- Simpson's Rule =  $\frac{\Delta x}{3}[f(a)+4f(x_1)+2f(x_2)+4f(x_3)+\ldots+2f(x_{n-2})+$

## **Power Sum Rules**

 $\sum_{i=1}^{n} i^3 = \left(\frac{n(n+1)}{2}\right)^2$ 

### Definite Integrals

- Definition:  $\int_a^b f(x)dx = \lim_{n \to \infty} \sum_{i=1}^n f(x_{i-1})\Delta x$ .
   Properties: Flip bounds (negate), break into smaller into
- ntal understanding of integration and its geometric interpre

### u-substitution

- Replace x with u(x), convert bounds,  $dx = \frac{du}{u(x)}$
- Calc 1 Technique: Use when an integral's integrand is a composite function, res application in reverse.

## Integration by Parts

- · LIATE Rule: Choo use u as the algebraic function that appears first in the list of functions Logarithmic, Inverse trigonometric, Algebraic, Trigonometric, Exp

# Integrals of Trigonometric Functions

- $$\begin{split} &\int \tan(x)\,dx = -\ln|\cos(x)| + C \\ &\operatorname{thergrain} \operatorname{involving Secant} \operatorname{and} \operatorname{cosecant} \\ &\cdot \int \sec(x)\,dx = \ln|\sec(x) + \tan(x)| + C \\ &\cdot \int \csc(x)\,dx = -\ln|\csc(x) + \cot(x)| + C \\ &\operatorname{thergrain} \operatorname{involving Products} \operatorname{of Trigonometric Functions} \\ &\cdot \int \sin^n(x)\cos^m(x)\,dx \text{ can often be solved using trig} \end{split}$$

#### reduction formulas for powers of sine and cosine

- trigonometric functions for variables. For example, if  $\int \sqrt{a^2-x^2}\,dx$  appears, you could let  $x=a\sin(\theta)$  or  $x=a\cos(\theta)$  to

## Hyperbolic Trig Functions

- hyperbolas instead of circles. The primary hyperbolic functions are:
- Hyperbolic Sine:  $\sinh(x) = \frac{e^e e^x}{2}$  Hyperbolic Cosine:  $\cosh(x) = \frac{e^e + e^{-x}}{2}$  Hyperbolic Tangent:  $\tanh(x) = \frac{\sinh(x)}{\cosh(x)}$
- Hyperbolic functions have properties similar to trigonometric functions, such as even/odd symmetry and relationships between their derivatives and themselves

#### **Power Series**

•  $\sum_{n=0}^{\infty} a_n (x-a)^n$  with a radius of convergence F

### Order of Convergence

•  $\lim_{n \to \infty} \frac{|z_{n+1} - L|}{|z_n - L|^p} = C$  , where C is a constant and p is the order of p in the order of p is the order of p in th

### Convergence

### Convergence and Divergence:

- number of terms increases indefinitely. If the limit exists, it is called the sum of the series
- Conversely, a series diverges if the sequence of partial sums does not approach a finite limit. In this case, the series does not have a sum.
- Example of convergent series:  $\sum_{n=1}^{\infty}\frac{1}{2^n}=1$ , known as the geometric series Example of divergent series:  $\sum_{n=1}^{\infty}n$  diverges, as the partial sums increase v

- common convergence tests include:

- immon convergence tests include:  $0 \text{ Nevergence Test} = 1 \text{ If } m_n a_0 \ a_0 + b \text{ then the series } \sum_{n=1}^\infty a_n \text{ diverges.}$  Geometric Series Test  $\sum_{n=1}^\infty a_n^n \text{ converges to } \frac{1}{n^n} |r| < 1$ . In integral Test  $\Gamma(x)$  is positive, continuous, and decreasing for  $x \ge 1$  and  $a_n = f(n)$ , then  $\sum_{n=1}^\infty a_n$  and  $\int_1^\infty f(x) \, dx$  either both converge or both diverge.

- Absolute Convergence: A series  $\sum_{n=1}^\infty |a_n|$  converges. Conditional Convergence: A series  $\sum_{n=1}^\infty a_n$  converges, but  $\sum_{n=1}^\infty |a_n|$  diverges.

## Sequences and Series

- A sequence is an ordered list of numbers written in a specific order. It can be finite or  $\hbox{Formally, a sequence is denoted as } (a_n) \hbox{ or } \{a_n\}, \hbox{ where } a_n \hbox{ represents the $n$th term of sequence.}$

- Example:  $1,1/2,1/3,1/4,\ldots$  is a sequence with the formula  $a_n=\frac{1}{n}$
- Formally, a series is denoted as  $\sum_{n=1}^\infty a_n$  or  $a_1+a_2+a_3+\ldots$  Example:  $1+\frac12+\frac13+\frac14+\ldots$  represents the series of the sequence materials.

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## **Partial Fractions**

- osition is a technique used to break down a rational function into
- simpler fractions.
- simper inactions.

  The general process involves:

  2.1. Factorizing the denominator into linear and irreducible quadratic factors.

  2.2. Writing the partial fraction decomposition with undetermined coefficients for ea
- Example:  $\frac{3x^2+5x+7}{x^3-2x^2+x}$  can be decomposed into partial fractions as  $\frac{A}{x}+\frac{B}{x-1}+\frac{C}{(x-1)^2}$

## **Logistical Growth Function**

•  $P(t) = \frac{K}{1+\alpha e^{-kt}}$ 

r = growth rate, K = carrying capacity

### Improper Integrals

• Example:  $\int_1^\infty \frac{1}{x^p} \, dx$  converges if p>1 and diverges if  $p\leq 1$ .

Integrals where the limits of integration are infinite or where the function being integrated is undefined at certain points within the interval.

### **Taylor Polynomials**

- A Taylor polynomial of degree n for a function f(x) centered at a point x=a is a polynomial that approximates f(x) near x=a.
- The general form of a Taylor polynomial is
- $P_n(x)=f(a)+f'(a)(x-a)+\frac{f''(a)}{2!}(x-a)^2+\cdots+\frac{f^{(a)}(a)}{n!}(x-a)^n$  Here,  $f^{(n)}(a)$  denotes the nth derivative of f(x) evaluated at x=a, and n! n

# Taylor's Theorem

- polynomial approximation  $P_n(x)$ . It states that if f(x) is (n+1)-times differentiable on an interval cexists a number c between a and x such that the error  $R_n(x) = f(x) - P_n(x)$  can be
- This error term is known as the remainder or residual term of the Taylor polynomial

# **Maclaurin Series**

- (e., a=0). The Maclaurin series expansion of a function f(x) is given by:  $f(x)=f(0)+f'(0)x+\frac{f''(0)}{2}x^2+\cdots+\frac{f''(0)}{2}x^2+\cdots$  Essentially, the Maclaurin series represents the Taylor series expansion of a function around the

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