

MVE137 - Chalmers University Cheat Sheet

by Delegado FM (Learningbizz) via cheatography.com/73767/cs/34116/

Basic Probability Definitions		Basic Probability Definitions (cont)		Basic Probability Definitions (cont)	
Sample Space (Ω)	Set of all possible outcomes of a random experiment.	Sampling strategy	Choose repeatedly a random number in Ω	Mutually indepe- ndent (events)	More than two events (i.e. A,B,C) are mutually independent if: 1. They are pairwise independent 2. They meet the condition: P(A ∩ B ∩ C) = P(A) × P(B) × P(C) In plain english, events are mutually independent if any event is independent to the other events
Event	Outcome of a random experiment (inside Ω)	Sampling with	Select random numbers in Ω , without taking into account		
σ-field	The allowable events constitute a family of sets F, usually referred to as σ-field. Each set in F is a subset of	replac- ement	which ones you've already tested. Therefore, there will be some numbers tested multiple times		
Probability measure (P)	the sample space Ω . A probability measure on (Ω, F) is a function $P: F \to [0, 1]$ that satisfies the following two properties: 1. $P[\Omega] = 1$ 2. The probability of the union of a collection of disjoint members is the sum of its probabilities	Sampling without replac- ement	Select random numbers in Ω taking into account which ones you've already used. Therefore, you won't run the algorithm with the same number more than once		
				Condit- ional Probab- ility	If P[B] > 0, the conditional probability that A occurs give that B occurs is: P[A B]=P[-AnB]/P[B]
		Independent (events or family)	Two events are independent if: $P[A \cap B] = P[A] P[B]$ It also applies to families $\{Ai, i \in I\}$		
				Condit- ional Probab- ility (indep-	If A and B are independent events, then: $P[A B] = P[A \cap B]/P[B] = (P[A]*P[B])/P[B] = P[A]$
Probability space	(Ω, F, P)	Pairwise	To form all possible pairs (two items at a time) from a set		
Basic properties	$P[\varnothing] = 0$ $P[A^{-}] = 1 - P[A]$	Pairwise indepe-	A family or events are pairwise independent if:	endent events)	
of probab- ility measures	If $A \subseteq B$, then $P[B] = P[A] + P[B \setminus A] \ge P[A]$ $P[A \cup B] = P[A] + P[B] - P[A \cap B]$ Given sets A1, A2 $P[union(Ai)] \le sum(P[Ai])$ When the two events are disjoint, the inequality is = as they don't share any common space: $P[A \cap B] = 0$	ndent (family or events)	P[Ai n Aj] = P[Ai] P[Aj] for all i != j In english terms, a family or events is pairwise independent if any of its possible pairs is independent of each other. For example: P(AnB)=P(A)P(B) P(AnC)=P(A)P(C) P(BnC)=P(B)P(C)	Law of Total Probab- ility	Let e1en be partitions of Ω (a collection of ALL the sets in Ω which are independent of each other). Also assuming P[ei] > 0 for all i. The probability of A can be written as: P[A] = sum(i=1,n)(P[A ei]*P[ei]) In english, it's the sum of all the possible scenarios in which A can occur
Inclusion Exclusion Principle (comes from last basic					
property of probability measures)					



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Basic Probability Definitions (cont)

Bayes Assuming e1...en be partitions

Theorem of Ω

 $P[ej|B] = P[Ej \cap B]/P[B] = (P[B|Ej]/[Ej])/(sum(i=1,n)(P[-$

B/ei]P[ei])

It's basically using conditional theory and then applying conditional theory again for the top part and law of total probability

in the lower part

Discrete Random Variables and Expectation

Random A random variable X on a $\mbox{Variable} \quad \mbox{sample space } \Omega \mbox{ is a real-valued}$ $\mbox{(measurable) function on } \Omega; \mbox{ that}$ $\mbox{is } X:\Omega \to R.$

Denoted as upper case in this course and real numbers as

lower case

Discrete A discrete random variable is a
Random random variable that outputs
Variable only a finite or countably infinite
number of values

(i.e. number of kids in a family, range between 1 and x)

Probability that Sum of all the events w in Ω

which X(w) = x

X=a

Discrete Random Variables and Expectation (cont)

Indepe- Two random variables X and Y ndence are independent if and only if: of P[(X = x)n(Y = y)] = P[X=x]-

random *P[Y=y]

variables for all values x and y

Mutually Like mutually independent independent events

variables
Expectation

(mean)

random

It is a weighted average of the values assumed by the random variable, taking into account the probability of getting that value. The expectation of a discrete random variable X, denoted by

E[X] is given by

 $\mathsf{E}[\mathsf{X}] = \mathsf{sum}(\mathsf{i} \texttt{=} \mathsf{x}, \mathsf{X})(\mathsf{x}^*\mathsf{P}[\mathsf{X} \texttt{=} \mathsf{x}])$



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