

SML Syntax

String

```
#"st r"
```

```
String.sub : string * int -> char
```

```
chr
```

```
ord : char -> int
```

```
^
```

```
String.tokens : (char -> bool) -> string -> string list
```

```
String.explode : string -> char list
```

List

```
@ : 'a list @ 'a list
```

```
List.partition : ('a -> bool) -> 'a list -> 'a list * 'a list
```

```
List.rev : 'a list -> 'a list
```

```
List.exists : ('a -> bool) -> 'a list -> bool
```

```
List.all : ('a -> bool) -> 'a list -> bool
```

```
String.concatWith : string -> string list -> string
```

Referential Transparency

Replace any expression with another expression of "equal" value does not affect the value of the expression

Equivalence

Two programs are equivalent iff

1. They both evaluate to the same value, or
2. They both raise the same exception, or
3. They both enter an infinite loop

Properties

1. Equivalence is an equivalence relation
2. Equivalence is a congruence (one program can be substituted for another)

Equivalence (cont)

3. If $e \rightarrow e'$ then e is equivalent to e'

Valuable & Total

Expression e is valuable iff there is some value v s.t. $e == v$

- If $e = (e1, e2)$

- If $e = e1 + e2$

- If $e = e1 :: e2$

then e is valuable iff $e1$ is valuable and $e2$ is valuable

A function $f : A \rightarrow B$ is total iff for all values $v : A$, $f(v)$ is valuable

Currying

=== Non-Curried ===

```
fun pow (x, y) : int * int -> int =
```

```
case y of
```

```
0 => 1
```

```
| _ => x * pow(x, y-1)
```

=== Curried ===

```
fun pow x y =
```

```
case y of
```

```
0 => 1
```

```
| _ => x * pow(x, y-1)
```

reverse

```
1)
```

```
fun pow x y =
```

```
any
```

```
case y of
```

```
0 => 1
```

```
| _ => x * pow(x, y-1)
```

=== Currying and Uncurrying ===

```
curry : (('a * 'b) -> 'c) -> ('a -> 'b -> 'c)
```

```
fun curry f x y = f (x, y)
```

```
fun uncurry f (x, y) = f x y
```

```
uncurry : ('a -> 'b -> 'c) -> (('a * 'b) -> 'c)
```



Composition

```
fun compose (f, g) = fn x => f(g x)

Using infix operator
val sqrt_o f_abs = Math.sqrt o Real.f romInt o abs

Pipelining and infix pipeline operator
`fun pipeline (f, g) = g f

infix !>
fun x !> f = f x

fun sqrt_o f_abs i =i !> Real.f romInt !> Math.sqrt
datatype 'a list = Nil | :: of 'a * 'a list
```

Mergesort

```
fun split (lst : int list) : int list * int list =
  case lst of
    [] => ([], [])
  | [x] => ([x], [])
  | x::y::xs => let val (pile1, pile2) =
    split xs
    in
      (x::pile1, y::pile2)
    end

fun merge(lst1 : int list, lst2 : int list) : int
list =
  case (lst1, lst2) of
    ([], lst2) => lst2
  | (lst1, []) => lst1
  | (x::xs, y::ys) =>
    (case x < y of
      true => x::mer ge( xs, lst2)
    | false => y::mer ge( -
lst1, ys)

fun mergesort (lst : int list) : int list =
  case lst of
    [] => []
  | [x] => [x]
  | _ => let val (pile1, pile2) = split lst
    in merge( mer gesort pile1,
mergesort pile2)
    end
```

Generalized math functions

```
fun sum (f, a, b, inc) :
  if (a > b) then 0
  else (f a) + sum(f, inc(a), b, inc)

fun piOver8 = sum(fn x => 1.0 / (x*(x+ 2.0)), a,
b, fn x => x + 4.0)

fun integral (f, a, b, dx) =
  dx * sum(f, a+dx/2.0, b, fn x => x+dx)

fun series (operator, f, lo, hi, inc, identity) =
  if (lo > hi) then identity
  else operat or((f lo), series (operator, f,
inc(lo), hi, inc, identity))

fun sumSeries (f, a, b, inc) = series (op +, f, a,
b, inc, 0)

fun prodSe ries(f, a, b, inc) = series(op *, f, a,
b, inc, 1)
```

Data types

User defined types

```
datatype tree = Empty | Node of tree * int * tree
datatype 'a option = NONE | SOME of 'a
```

Type synonym

```
type intPai rList = (int * int) list
```

Map

```
map : ('a -> 'b) * 'a list -> b' list

fun map (f lst) =
  case lst of
    [] => []
  | h::tail => (f h)::(map f tail)
```

Fold

```
fun foldl(f, acc, lst) =
  case lst of
    [] => acc
  | h::t => foldl(f, f(h, acc), t) (*tail
recursive*)

fun foldr(f, acc, lst) =
  case lst of
    [] => acc
  | h::t => f(h, foldr(f, acc, t)) (*not
tail recursive*)
```

Associativity

```
'a -> 'b -> 'c = 'a -> ('b -> 'c)
f a1 a2 = (f a1) a2
```

Filter

```
filter : ('a -> bool) * 'a list -> 'a list
fun filter (p : 'a -> bool, lst : 'a list) =
  case lst of
    [] => []
  | x::xs => if p x then x::(filter p xs)
              else filter p xs
```



By **kvp_**
cheatography.com/kvp/

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