

## Equations!

Deviation score:	$(x-\bar{x})$
Squared deviation score:	$(x-\bar{x})^2$
Sum of squares:	$SS = \sum(x-\bar{x})^2$
Variance:	$SD^2 = SS \div N$
Standard deviation:	$\sqrt{\text{variance}}$ $\sqrt{SD^2}$
Covariance	$cov = SP \div N$
Pearson correlation:	$r = cov \div (SD_x)(SD_y)$
Slope:	$b_y = r(SD_y \div SD_x)$
intercept:	$a_y = \bar{y} - b_y(\bar{x})$
Total variability:	$SST = \sum(Y-\bar{y})^2$
explained variability:	$SSR = \sum(Y'-\bar{y}')^2$
unexplained variability	$SSE = \sum(Y-Y')^2$
Standard error of prediction:	$SD_{y-y'} = SD_y \sqrt{1-r^2}$
Predicting X':	$X' = ax + bxY$
Predicting Y':	$Y' = ay + byX$

## General guidelines for test reliability

>.85	very desirable
.70 to .85	desirable aka moderately acceptable
<.70	not desirable aka poor reliability

## describe relationship between two variables?

### 1.) Direction of the relationship:

Positive (+) or negative (-)

*Positive correlation* = As the values of x increase or decrease, so do the values of y  
*No relationship* = no consistent relationship between variables

*Negative correlation* = As the values of x increases, the value of y decreases, and vice versa

### 2.) shape of the relationship

## describe relationship between two variables? (cont)

Linear relationship = straight line relationships  
– All dots clustered around straight line  
Curvilinear relationship = consistent, predictable relationship, but not linear  
– As the values of x increase, the values of y increases but at some point the pattern reverses

### 3.) Strength of the relationship

Subjective measure of relationship between two scores (e.g., weak, moderate, strong, no relationship)  
how closely the data points cluster together  
The more spread out they are from a line of some sort, the weaker the correlation between variables

### 4.) Magnitude of the relationship

Objective measure of relationship based on computed r value: ranges from -1 to 1

## biserial correlation

### When to use it:

– when one of the variables is nominal (with only two groups) and the other variable is interval/ratio

*How to calculate:*

– use the same formula as pearson r

## Curvilinear relationships:

Linear:  $Y' = a + bX$

Quadratic:  $Y' = a + bX + cX^2$

Cubic:  $Y' = a + bX + cX^2 + dX^3$

Quartic:  $Y' = a + bX + cX^2 + dX^3 + eX^4$

## Comparing SD<sub>y-y'</sub> and SD<sub>y</sub>

When R does not equal Zero, SD<sub>y-y'</sub> will be smaller than SD<sub>y</sub>

When R=0 (no correlation/relationship), SD<sub>y-y'</sub> = SD<sub>y</sub>

When R=+/- 1 (perfect correlation), SD<sub>y-y'</sub>=0

## How do we describe our data?

- 1.) plotting a scatter plot, linearity, Shape strength, direction, magnitude
- 2.) defining the regression line Central (mean of bivariate data) tendency
- 3.) standard error or estimates Variability (SD<sub>y-y'</sub>)

## Factors affecting R

- 1.) Relationship is real and strong or weak contributes to a bigger/smaller r
- 2.) Sampling error Sampling error = naturally occurring discrepancy, or error, that exists between a sample statistic and the corresponding parameter
- 3.) Unmeasured third variable contributes to a bigger/smaller r, Correlation tells us if a relationship between two variables exists but does not tell us about causation
- 4.) Heterogeneous sample Data in which the sample of observations could be subdivided into two distinct sets on the basis of some other variable
- 5.) Sampling from a restricted (truncated) range The correlation coefficient will be affected by the range of score in the data

## Factors affecting R (cont)

- 6.) Non-linear- Reminder: r underesti-  
rity: relati- mates a curvilinear relati-  
onship is onship, contributes to a  
curvilinear smaller r
- 7.) Hetero- contributes to a smaller r  
scedasticity  
in the data

## PHI

### When to use it:

- when both variables are nominal (with only two groups per variable, i.e., dichotomous)

### Calculating Phi:

- use the same formula as pearson r

## How to calculate Pearson r:

- 1.) Plot the data (scatterplot)
- 2.) Compute (e.g., deviation scores, bivariate statistics SP, COV)
- 3.) Compute (number beyond +/-1 correlation coeffi- means you did it  
cient r wrong)

## Interpreting Pearson Correlation

- |                 |                       |
|-----------------|-----------------------|
| <  .10          | no relationship       |
| .10  to  .30    | weak relationship     |
| >  .30  to  .50 | moderate relationship |
| >  .50          | strong relationship   |

## Reporting in APA format

- 1.) Give variables, R = ?, Mean =  
describes ?, Standard deviation = ?, Give  
relati- sample size, Mention strength  
onship in and if its positive for negative  
statistical terms
- 2.) Results in plain language

## extra stuff

Homoscedasticity (a good thing): Variability in Y scores remains constant across increasing values of X

Heteroscedasticity (not a good thing): variability in y scores changes across increasing values of x,  
Caused by a skew in one or both variables

$$SST = SSy \quad SSe = SSy - y'$$

(error)

$$SSr = SST - SSe \quad \Sigma(Y - Y') = 0$$

For Y': if r=0, by=0 (i.e., regression line is parallel to the x-axis), and ay= $\bar{y}$

For X': if r=0, bx=0 (i.e., regression line is parallel to the x-axis), and ax= $\bar{x}$

As correlation (r) increases, the numerical value for b increases

Total variability =  $\Sigma(Y - \bar{y})$   
differences between  
observed data (Y)  
and the mean value  
of Y

Unexplained variab-  $\Sigma(Y - Y')$   
ility (i.e., residuals) =  
difference between  
the observed value  
for Y and the  
predicted value for  
Y(Y')

Explained variability =  $\Sigma(Y' - \bar{y})$   
the difference  
between total and  
unexplained variab-  
ility

Standardized test = interval

## Spearman rho

When to use it:

- one or both variables are on an ordinal scale of measurement
- there is a weak curvilinear relationship in interval/ratio data
- there is heteroscedasticity in interval/ratio data

### How to calculate:

Convert all scores into ranks

Lower scores get lower ranks

High scores get higher ranks

Use the pearson correlation formula to find how consistently increases in one variable are associated with increases in another variable

