

Basic Concepts (H1)

| | |
|---------|------------------------------|
| Current | $I[A]=Q[C]/t[s]$ |
| Voltage | $U[V]=W[J]/Q[C]$ |
| Power | $P[W]= W / t = U * I$ |
| Energy | $W = P * t$ |
| Coulomb | $1C = 6,241 * 10^{18}$ elek. |

Resistance (H2)

| | |
|-------------------|----------------------------|
| Ohm's Law | $I[A] = U[V] / R[Ohm]$ |
| Resistivity | $R = \rho * (l[m]/A[m^2])$ |
| Power Absorbition | $P = V^2/R = I^2R$ |

DC Circuits (H3)

Voltage Law (KVL):

The sum of all voltage drops equals the sum of all voltage rises in a mesh.

Current Law (KCL):

The sum of all currents entering a closed surface equals the sum of all leaving one.

Equivalent Resistor:

$R_t = (R_1 * R_2) / (R_1 + R_2)$
(in case of 2 resistors parallel)

DC Circuits Analysis (H4)

Source Transformation:

Current and Voltage source with 1 resistor are interchangeable.

$I = V / R$ and $U = I * R$

Mesh Analysis:

Applying KVL to a mesh.

Nodal Analysis:

Applying KCL to a node.

Equivalent Circuits (H5)

Thevenin Circuit:

Circuits can be reduced to voltage source with resistor in serie.

$R_t = R_{th}$ (open circuit and independent sources deactivated)

V_{th} = open circuit voltage

I_{sc} = current in short-circuit between a and b

Norton Circuit:

Found by source transformation of Thevenin

I_{sc} equals I_n

Maximum Power Transfer:

$V_{th}^2 / 4R_{th}$

Milliman's Theorem:

Multiple voltage sources with resistors can be combined into one by transformations giving one voltage source.

$V_m = (G_1V_1 + \dots + G_nV_n) / (G_1 + \dots + G_n)$

$R_m = 1 / (G_1 + \dots + G_n)$

Delta-Y Transformation:

$R_a = (R_1 * R_2) / (R_1 + R_2 + R_3)$

$R_b = (R_2 * R_3) / (R_1 + R_2 + R_3)$

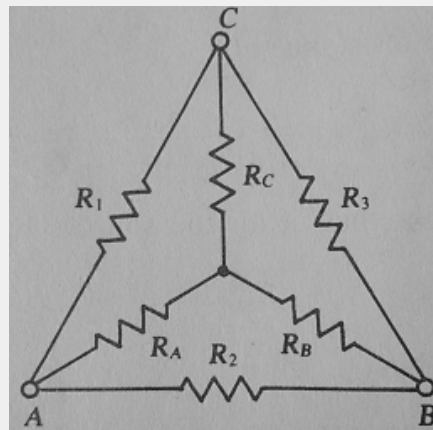
$R_c = (R_1 * R_3) / (R_1 + R_2 + R_3)$

$R_1 = (R_aR_b + R_aR_c + R_bR_c) / R_b$

$R_2 = (R_aR_b + R_aR_c + R_bR_c) / R_c$

$R_3 = (R_aR_b + R_aR_c + R_bR_c) / R_a$

Y-Delta Transformation



Operational Amplifier (H6)

$U_+ = U_-$ and $I_+ = I_- = 0$

inverter:

$V_o = -(R_f/R_i) * V_i$

summer:

$V_o = -(R_f/R_a)V_a + (R_f/R_b)V_b + (R_f/R_c)V_c$

Capacitors (H8)

Capacitance $C = Q / U$

Capacitance $C = \epsilon * (A/d)$

Capacitance parallel $C_t = C_1 + C_2 + \dots$

Capacitance series $1 / C_t = (1/C_1) + (1/C_2)$ etc.

Energy Storage $W_c = 0.5CV^2$

Time-varying Current $i = dq/dt = C * dv/dt$

RC time constant $\tau = R_{th} * C$

RC expression voltage $v(t) = v(\infty) + [v(0+) - v(0)]e^{-t/\tau}$

RC expression current $i(t) = i(\infty) + [i(0+) - i(0)]e^{-t/\tau}$

Inductors (H9)

Flux $\psi = N * d\phi/dt$

Inductance $L \psi = N \phi$

Coil inductance $L = (N^2 * \mu * A) / l$

Inductor series $L_t = L_1 + L_2 + L_n$

Inductor parallel $1 / L_t = (1/L_1) + (1/L_2)$ etc.

Energy Storage $W_l = 0.5Li^2$

RC time constant $\tau = L / R_{th}$

Alternating Current (H10)

| | |
|-----------------------|--|
| Frequency | $f \text{ [Hz]} = 1 / T \text{ [s]}$ |
| Angular Velocity | $\omega \text{ [rad/s]} = 2\pi f$ |
| Average Value factor | $2 / \pi = 0.637$ |
| Resistor Power | $P_{\text{av}} = V_{\text{m}}^2 / 2R = I_{\text{m}}^2 R / 2$ |
| Effective Value (RMS) | $V_{\text{eff}} = V_{\text{m}} / \sqrt{2}$ |
| Inductor Law | $X_L = \omega L$ and $I_{\text{m}} = V_{\text{m}} / X_L$ |
| Capacitor Law | $X_C = -1/(\omega C)$ |

Component Behavior (H10)

Resistor:

Current and Voltage in phase.

$$v = V_{\text{m}} \sin(\omega t + \phi)$$

$$i = I_{\text{m}} \sin(\omega t + \phi)$$

Inductor:

Voltage leads Current by 90 deg.

$$v = X_L I_{\text{m}} \cos(\omega t + \phi)$$

$$i = I_{\text{m}} \sin(\omega t + \phi)$$

Capacitor:

Current leads Voltage by 90 deg.

$$v = V_{\text{m}} \sin(\omega t + \phi)$$

$$i = \omega C V_{\text{m}} \cos(\omega t + \phi)$$

AC Circuit Analysis (H12)

| | |
|----------------|--|
| Impedantie | $Z = V/I$ |
| Impedantie (2) | $Z = R + jX$ |
| Admittantie | $Y = 1/Z$ |
| AC Current | $I = (I_{\text{m}} / \sqrt{2}) \angle \theta$ |
| AC Voltage | $V = ((R + jX) I_{\text{m}} / \sqrt{2}) \angle \theta$ |

AC Circuit Analysis (H13)

Mesh Analysis:

Transform current to voltage source

Use of KVL

Nodal Analysis:

Transform voltage to current source

Use of KCL

AC Y-Delta transformation (H14)

Delta-Y Transformation:

$$Z_a = (Z_1 * Z_2) / (Z_1 + Z_2 + Z_3)$$

$$Z_b = (Z_2 * Z_3) / (Z_1 + Z_2 + Z_3)$$

$$Z_c = (Z_1 * Z_3) / (Z_1 + Z_2 + Z_3)$$

$$Z_1 = (Z_a Z_b + Z_a Z_c + Z_b Z_c) / Z_b$$

$$Z_2 = (Z_a Z_b + Z_a Z_c + Z_b Z_c) / Z_c$$

$$Z_3 = (Z_a Z_b + Z_a Z_c + Z_b Z_c) / Z_a$$

Maximum Power Absorbed (H14)

The load is the Z_{th} conjugate $Z_L = Z_{\text{th}}^*$

Max. Power Absorbed $V_{\text{th}}^2 / (4R_{\text{th}})$ (V_{th} is RMS of V_{th})

Power in AC circuits (H15)

Instantaneous Power:

$$p = V * I \cos(\theta)$$

$\cos(\theta)$ = Power Factor (PF)

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Reactive Power:

$$Q = V * I * \sin(\theta)$$

Complex Power:

$$S = P + jQ$$

Apparent Power:

$$S = VI$$

$$1 \text{ hp} = 745,7 \text{ W}$$

Transformers (H16)

| | |
|----------------------|--|
| Ratio | $v_1/v_2 = N_1/N_2 = i_2/i_1$ |
| Reflected Impedance | $Z_r = V_1/I_1 = a^2 Z_2$ |
| Current rating | kVA transformer / voltage rating |
| PhiMax | $\Phi_{\text{M}} = (\sqrt{2} * V_{\text{rms}}) / (\omega N)$ |
| coupling coefficient | $k = M / \sqrt{L_1 * L_2}$ |

tijd-fase formules

| | weerstand | spoel | condensator |
|---|-----------|-----------------|-----------------|
| Z | R | $j\omega L$ | $1/(j\omega C)$ |
| R | R | 0 | 0 |
| X | 0 | ωL | $-1/(\omega C)$ |
| Y | $1/R$ | $1/(j\omega L)$ | $j\omega C$ |
| G | $1/R$ | 0 | 0 |
| B | 0 | $-1/(\omega L)$ | ωC |

3-Phase (H17)

$$V_{\text{line}} = \sqrt{3} * V_{\text{phase}}$$

$$I_{\text{line}} = \sqrt{3} * I_{\text{phase}}$$

Dot rule transformer

Primary I into dot and secondary I out of dot:

I1 and I2 both positive or negative.

