

### Basic Concepts (H1)

Current	$I[A]=Q[C]/t[s]$
Voltage	$U[V]=W[J]/Q[C]$
Power	$P[W]= W / t = U * I$
Energy	$W = P * t$
Coulomb	$1C = 6,241 * 10^{18}$ elek.

### Resistance (H2)

Ohm's Law	$I[A] = U[V] / R[\text{Ohm}]$
Resistivity	$R = \rho * (l[m]/A[m^2])$
Power Absorbtion	$P = V^2/R = I^2R$

### DC Circuits (H3)

#### Voltage Law (KVL):

The sum of all voltage drops equals the sum of all voltage rises in a mesh.

#### Current Law (KCL):

The sum of all currents entering a closed surface equals the sum of all leaving one.

#### Equivalent Resistor:

$R_t = (R_1 * R_2) / (R_1 + R_2)$   
(in case of 2 resistors parallel)

### DC Circuits Analysis (H4)

#### Source Transformation:

Current and Voltage source with 1 resistor are interchangeable.

$I = V / R$  and  $U = I * R$

#### Mesh Analysis:

Applying KVL to a mesh.

#### Nodal Analysis:

Applying KCL to a node.

### Equivalent Circuits (H5)

#### Thevenin Circuit:

Circuits can be reduced to voltage source with resistor in serie.

$R_t = R_{th}$  (open circuit and independent sources deactivated)

$V_{th} =$  open circuit voltage

$I_{sc} =$  current in short-circuit between a and b

#### Norton Circuit:

Found by source transformation of Thevenin

$I_{sc}$  equals  $I_n$

#### Maximum Power Transfer:

$V_{th}^2 / 4R_{th}$

#### Milliman's Theorem:

Multiple voltage sources with resistors can be combined into one by transformations giving one voltage source.

$V_m = (G_1V_1 + \dots + G_nV_n) / (G_1 + \dots + G_n)$

$R_m = 1 / (G_1 + \dots + G_n)$

#### Delta-Y Transformation:

$R_a = (R_1 * R_2) / (R_1 + R_2 + R_3)$

$R_b = (R_2 * R_3) / (R_1 + R_2 + R_3)$

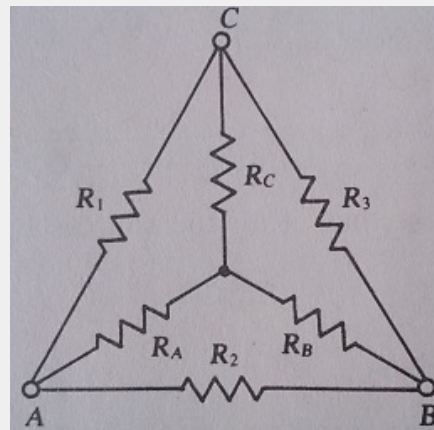
$R_c = (R_1 * R_3) / (R_1 + R_2 + R_3)$

$R_1 = (R_aR_b + R_aR_c + R_bR_c) / R_b$

$R_2 = (R_aR_b + R_aR_c + R_bR_c) / R_c$

$R_3 = (R_aR_b + R_aR_c + R_bR_c) / R_a$

### Y-Delta Transformation



### Operational Amplifier (H6)

$U_+ = U_-$  and  $I_+ = I_- = 0$

#### inverter:

$V_o = -(R_f/R_i) * V_i$

#### summer:

$V_o = -(R_f/R_a)V_a + (R_f/R_b)V_b + (R_f/R_c)V_c$

### Capacitors (H8)

Capacitance  $C = Q / U$

Capacitance  $C = \epsilon * (A/d)$

Capacitance parallel  $C_t = C_1 + C_2 + \dots$

Capacitance series  $1 / C_t = (1/C_1) + (1/C_2) \text{ etc.}$

Energy Storage  $W_c = 0.5CV^2$

Time-varying Current  $i = dq/dt = C * dv/dt$

RC time constant  $\tau = R_{th} * C$

RC expression voltage  $v(t) = v(\infty) + [v(0+) - v(0)]e^{-t/\tau}$

RC expression current  $i(t) = i(\infty) + [i(0+) - i(0)]e^{-t/\tau}$

### Inductors (H9)

Flux  $v = N * d\phi/dt$

Inductance  $L i = N \phi$

Coil inductance  $L = (N^2 * \mu * A) / l$

Inductor series  $L_t = L_1 + L_2 + L_n$

Inductor parallel  $1 / L_t = (1/L_1) + (1/L_2) \text{ etc.}$

Energy Storage  $W_l = 0.5Li^2$

RC time constant  $\tau = L / R_{th}$

### Alternating Current (H10)

Frequency	$f \text{ [Hz]} = 1 / T \text{ [s]}$
Angular Velocity	$\omega \text{ [rad/s]} = 2\pi f$
Average Value factor	$2 / \pi = 0.637$
Resistor Power	$P_{\text{av}} = V_{\text{m}}^2 / 2R = I_{\text{m}}^2 R / 2$
Effective Value (RMS)	$V_{\text{eff}} = V_{\text{m}} / \sqrt{2}$
Inductor Law	$X_L = \omega L$ and $I_{\text{m}} = V_{\text{m}} / X_L$
Capacitor Law	$X_C = -1/(\omega C)$

### Component Behavior (H10)

#### Resistor:

Current and Voltage in phase.

$$v = V_{\text{m}} \sin(\omega t + \phi)$$

$$i = I_{\text{m}} \sin(\omega t + \phi)$$

#### Inductor:

Voltage leads Current by 90 deg.

$$v = X_L I_{\text{m}} \cos(\omega t + \phi)$$

$$i = I_{\text{m}} \sin(\omega t + \phi)$$

#### Capacitor:

Current leads Voltage by 90 deg.

$$v = V_{\text{m}} \sin(\omega t + \phi)$$

$$i = \omega C V_{\text{m}} \cos(\omega t + \phi)$$

### AC Circuit Analysis (H12)

Impedantie	$Z = V/I$
Impedantie (2)	$Z = R + jX$
Admittantie	$Y = 1/Z$
AC Current	$I = (I_{\text{m}} / \sqrt{2}) \angle \theta$
AC Voltage	$V = ((R + jX) I_{\text{m}} / \sqrt{2}) \angle \theta$

### AC Circuit Analysis (H13)

#### Mesh Analysis:

Transform current to voltage source

Use of KVL

#### Nodal Analysis:

Transform voltage to current source

Use of KCL

### AC Y-Delta transformation (H14)

#### Delta-Y Transformation:

$$Z_a = (Z_1 * Z_2) / (Z_1 + Z_2 + Z_3)$$

$$Z_b = (Z_2 * Z_3) / (Z_1 + Z_2 + Z_3)$$

$$Z_c = (Z_1 * Z_3) / (Z_1 + Z_2 + Z_3)$$

$$Z_1 = (Z_a Z_b + Z_a Z_c + Z_b Z_c) / Z_b$$

$$Z_2 = (Z_a Z_b + Z_a Z_c + Z_b Z_c) / Z_c$$

$$Z_3 = (Z_a Z_b + Z_a Z_c + Z_b Z_c) / Z_a$$

### Maximum Power Absorbed (H14)

The load is the  $Z_{\text{th}}$  conjugate  $Z_L = Z_{\text{th}}^*$

Max. Power Absorbed  $V_{\text{th}}^2 / (4R_{\text{th}})$  ( $V_{\text{th}}$  is RMS of  $V_{\text{th}}$ )

### Power in AC circuits (H15)

#### Instantaneous Power:

$$p = V * I \cos(\theta)$$

$\cos(\theta)$  = Power Factor (PF)

$\theta$  = fase spanning - fase stroom

#### Reactive Power:

$$Q = V * I * \sin(\theta)$$

#### Complex Power:

$$S = P + jQ$$

#### Apparent Power:

$$S = VI$$

$$1 \text{ hp} = 745,7 \text{ W}$$

### Transformers (H16)

Ratio	$v_1/v_2 = N_1/N_2 = i_2/i_1$
Reflected Impedance	$Z_r = V_1/I_1 = a^2 Z_2$
Current rating	kVA transformer / voltage rating
PhiMax	$\Phi_{\text{M}} = (\sqrt{2} * V_{\text{rms}}) / (\omega N)$
coupling coefficient	$k = M / \sqrt{L_1 * L_2}$

### tijd-fase formules

	weerstand	spoel	condensator
Z	R	$j\omega L$	$1/(j\omega C)$
R	R	0	0
X	0	$\omega L$	$-1/(\omega C)$
Y	$1/R$	$1/(j\omega L)$	$j\omega C$
G	$1/R$	0	0
B	0	$-1/(\omega L)$	$\omega C$

### 3-Phase (H17)

$$V_{\text{line}} = \sqrt{3} * V_{\text{phase}}$$

$$I_{\text{line}} = \sqrt{3} * I_{\text{phase}}$$

### Dot rule transformer

Primary I into dot and secondary I out of dot:  
I1 and I2 both positive or negative.

