Cheatography

UWI Comp2211 - Analysis of Algorithms Cheat Sheet

by Keto via cheatography.com/183106/cs/38117/

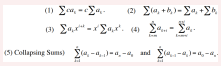
Summations - Closed Forms

(1) $\sum_{k=m}^{n} c = (n-m+1)c.$ (2) $\sum_{k=1}^{n} k = \frac{n(n+1)}{2}.$

(3) $\sum_{k=1}^{n} k^2 = \frac{n(n+1)(2n+1)}{6}.$ (4) $\sum_{k=0}^{n} a^k = \frac{a^{n+1}-1}{a-1}$ (where $a \neq 1$)

(5) $\sum_{k=1}^{n} ka^k = \frac{a-(n+1)a^{n+1}+na^{n+2}}{(a-1)^2}$ (where $a \neq 1$).

Summations - Rules



Logarithm Rules

$$\log_b b^x = x$$

$$b^{\log_b x} = x$$

$$\log_b(xy) = \log_b(x) + \log_b(y)$$

$$\log_b(x^a) = a \cdot \log_b(x)$$

$$\log_k(x) = \frac{\ln(x)}{\ln(k)} = \frac{\log_{10}(x)}{\log_{10}(k)}$$

$$a^{\log_b k} = k^{\log_b a}$$

Note: for AoA, $lg = \log_2$

$$e.g.\ lg\ 3 = \frac{\log_{10}(3)}{\log_{10}(2)}$$

Asymptotic Analysis - Common Orders of Growth

Slowest Growth → Fastest Growth

- $\Theta(1)$: constant
- $\Theta(\log n)$: logarithmic
- $\Theta(n)$: linear
- $\Theta(n \log n)$:
- $\Theta(n^2)$: quadratic
- $\Theta(n^k)$ (for constant k) : polynomial
- $\Theta(k^n)$ (for constant k) : exponential

Master Theorem Shortcut

Case	Condition	Result
1	k < E	n^E
2	k == E	$n^K \lg(n)$
3	k > E	n^K

Fermat's Little Theorem

For any prime p, for any x:

$x^p \equiv x \pmod p$

Alternatively, for any $x \neq 0$:

$x^{p-1} \equiv 1 \pmod p$

Mod Operations

(x + y) mod n = ((x mod n) + (y mod n)) mod n

(xy) mod n = ((x mod n) × (y mod n)) mod n

(x − y) mod n = ((x mod n) − (y mod n)) mod n

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