

### First order Differential Equations

Linear  $a(t)y' + b(t)y = f(t)$  Normal form  $y' + p(t)y = q(t)$

Separable  $dy/dt = g(y)h(t)$

Bernoulli  $a(t)y' + b(t)y = f(t)y^m$   $m \neq 0, 1$

Homogeneous  $y' = g(y/t)$

Exact  $M(x,y)dx + N(x,y)dy = 0$  Exact if and only if the partials  $M_y$  and  $N_x$  are equal

Non-Exact  $M(x,y)dx + N(x,y)dy = 0$  When  $M_y \neq N_x$

### First order DE's and their form

### Solving first order linear

1. Make sure its in normal form  $y' + p(t)y = q(t)$

2. Find an integrating factor  $\mu(t) = e^{\int p(t)dt}$

3. Multiply both sides of the normal form by  $\mu(t)$  to get  $(\mu(t)y)' = \mu(t)q(t)$

4. Integrate both sides of  $(\mu(t)y)' = \mu(t)q(t)$  and solve for  $y$

Dont Forget constants of integration

### Solving FO Separable DE

1. Rewrite  $y'$  and  $dy/dt$  and separate the variable  $y$  from the variable  $t$  to get  $d$   $dy/dt = g(y)h(t)$  where we get...  $(1/g(y)) dy = h(t)dt$

2. Integrate both sides to obtain

### Second and Higher Order DE's

2<sup>ND</sup> Order Linear  $a(t)y'' + b(t)y' + c(t)y = f(t)$  Normal form  $y'' + p(t)y' + q(t)y = r(t)$

Homogeneous (H)  $a(t)y'' + b(t)y' + c(t)y = 0$  Gen. Soltn.  $y_H(t, c_1, c_2)$

Non-Homogeneous (NH)  $a(t)y'' + b(t)y' + c(t)y = f(t)$  Gen. Soltn.  $y_H(t, c_1, c_2) + y_P(t)$

(H) const. coeff.  $ay'' + by' + cy = 0$   $a \neq 0, b, c$  are const.

Cauchy-Euler  $at^2y'' + bty' + cy = 0$   $a \neq 0, b, c$  are const.

$y_H(t)$  = general solution of (H)

$y_P(t)$  = particular solution of (NH)



By **katalyst**

[cheatography.com/katalyst/](http://cheatography.com/katalyst/)

Not published yet.

Last updated 14th October, 2022.

Page 1 of 1.

Sponsored by **CrosswordCheats.com**

Learn to solve cryptic crosswords!

<http://crosswordcheats.com>