### Maths and Tech Cheat Sheet by Jonathan\_Walsh1999 via cheatography.com/81859/cs/22389/

### Quaternions

A quaternion is a 4 element vector that can used to encode any rotation in a 3D coordinate system.

<b>q</b> = ( <i>w</i> , <i>x</i> , <i>y</i> , <i>z</i> ) or <b>q</b> = (w, v) where v = (x, y, z)				
<b>q</b> = (w, v) = (cos(t- heta/2), sing(thet- a/2)r)	r and theta form an axis-angle rotation.			
Normalise Quater-	$w^2 + x^2 + y^2 + z^2 = 1$			

Ν nions:

#### Pros

Quaternions can easily be combined together, used to transform points/vectors and can be interpolated very easily. Interpolation is vital for animation, which is far more difficult with matrices.

Quaternions only use 4 floats, 12 less then 4x4 matrices.

#### Cons

They lack hardware support, therefore they need to be converted from matrices to them and back to matrices again.

#### Formulae 1

Quaternion can be converted to a matrix

If  $\mathbf{q} = (w, x, y, z)$ , then

1st row - Mg =  $[1-2y^2 - 2z^2 2xy+2wz 2xz -$ 2wy 0]

2nd row - Mq =  $[2xy - 2wz - 1 - 2x^2 - 2z^2 - 2yz +$ 2wx 0]

 $3rd row - Mq = [2xz + 2wy 2yz - 2wx 1-2x^2 - 2wx 1-2wx 1-2w^2 - 2wx 1-2w^2 - 2w^2 - 2$  $2y^2 0$ ]

4th row - Mg = [0 0 0 1]

Multiply result by  $1/w^2 + x^2 + y^2 + z^2$  if **q** is not normalised

Can be expensive but can be simplified in code. Refer to Van Verth for more details.

#### Formulae 2

Quaternions can be added and scaled

```
Addition: (w1, x1, y1, z1) + (w2, x2, y2, z2)
= (w1 + w2, x1 + x2, y1 + y2, z1 + z2)
```



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### Quaternions (cont)

Multiplication: q1, q2 = (w, v) = (w1w2 - v1). v2,  $w1v2 + w2v1 + v2 \times v1$ )

Note that X means cross product and . means dot product

Same effect as multiplying matrices, order important

This is potentially much faster than matrix multiplication

#### Formulae 3

Inverse of quaternion where rotation is in the opposite direction.

 $a^{-1} = (w, -v)$ 

Quaternion must be normalised before formula is used

Much faster than matrix equivalent

Vector can be represented as quaternions. Set w to 0

i.e. Vector p = (x, y, z) = (0, x, y, z) as a quaternion

#### Formulae 4

Rotate a vertex or vector p by a quaternion  $\mathbf{q} = (\mathbf{w}, \mathbf{v})$ 

Rotate q (**p**) =  $q^{-1}pq = (2w^2 - 1)p + 2(v \cdot p)v$ + 2w(v X p)

Note that X means cross product and . means dot product

Slower than matrix equivalent

#### Summary

Quaternions can perfrom similar operations to matrices with comparable performance although you need to convert to/from matrices and they can't store positioning/scaling

Therefore, there is no compelling reason to use them yet.

#### **Emerging Tech for games**

	echilor games
Hardware Capabi- lities	Screen res/refresh rates
	Depth and Stencil buffer formats
	Anti-aliasing
	Texture Capabilities
Testing Capabi- lities	DX 10+ define min spec
	Still need some testing to check for advance features
	Consoles are largely unaffected by such matters as specs are fixed unlike PCs
	Still need to check for storage size, peripherals etc.
Shader Capabi- lities	Shaders complied to machine code
	Shader version defines instru- ction set available
	Higher shader versions have more instructions like for and if
	Have more registers
	Should provide alternate shaders for high and low spec machines
Multiple Passes	Complex material may need several passes in the shaders

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Emerging T	ech for games (cont)	Emerging 1	Fech for games (cont)	Emerging T	ech for games (cont)
	So that one texture can be rendered through different shaders adding multiple postprocessing effects for example		Input: Array of vertices Output: Stream of primitives - Must be specified as a triangle strip for example. Can output any number of primitives.	Stream output Considera- tions	Cannot ouput to same buffer that is being input from Work around this by using
Effect	Use .fx files we can collect		Example shown on lecture		double buffering
files for capabi- lities	together shader passes and their render states into techniques	Geometry Shader	slides Distorting, animating geometry		Often need multiple passes to render/update geometry
	Provide a range of techniques	uses			
	for different hardware specif- ications		Silhouettes	Instancing /	Stream-out for Particles
	If any one pass in a technique		Creating extra view-dependent gemetry	Instancing Overview	Instancing is a method to render many models or sprites
	fails capability testing then degrade to simpler technique		Particle systems without		in a single API draw call
	The DX effects files system	0	instancing		Previosuly we have rendered each model one at a time
	makes this quite simple. Example shown in lecture	Geometry shader consid-	Not needed for traditional geometry rendering methods so set gs shader to NULL		Send a list of instances with the vertex and index data
Quantation	slides	erations			List contains what is required
Geometry Shaders	This shader processes primitives e.g. triangle, lines		Performance of geomtry		to render each model
	Like vertex shader but works		shaders may be an issue for older GPUs		Removes per-model state changes
	with multiple vertices at the same time	Stream Output	Data ouput from gs can be written back into GPU memory		Allows for massively increased batch sizes
	Operates on the output of vertex shader	stage		Instance	Instance data stored on GPU
	Can also create or delete		Very powerful DX 11 feature	Buffers /	is instance buffer
	primitives ie output can be		Particle system can be done in	State	
	different to input		2 passes on the GPU. Pass1 - render with GPU as normal. Pass2 - Update particle		Smplest instance buffer might contain a list of instance positions
			positions on GPU, writing back to memory. There ios no CPU		Model defines by verterx/index data rendered once at each

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inttervention - efficent

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psoition in this buffer

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Instancing / Stream-out for Particles (cont) Instancing / Stream-out for Particles (cont) Instancing / Stream-out for Particles (cont) State requirement for Space is reserved forr Particles are spawned from instancing can be an issue instance data in both CPU and emitters GPU memory Particles have a life time after Vertex VS often unusual when instan-Shaders cing, depending on what is Constant copying of instance which they die for stored in the instance buffer buffer between GPU and CPU There may be attractors, means performance is lower instancing repulsors and other features than normal Very common to store some added for system complexity/fper-instance data and lexibility This is why we might not want randomise other elements to store a world matrix for each Approach: Store render data in instance. Instead the data is Instance instance buffer, store update Can store more than just often compressed Buffer position in an instance buffer data, update particles using Data to give each instance a Implies VS may have to do CPU and then copy entire different look: Rotation, scale additional work to derive the buffer to GPU, render particles or store entire world matrix full instance data in one vatch using instancing, per-instance much faster but still requires Using Instancing suits the rendering CPU/GPU copy Can also store mroe unusal Instancing of large numbers of similar data: Seed value to randomise models. ie trees, armies Sprite-Smart approach for camera each isntance or entity/paticle based facing sprite particles however Example: Particles are all similar, often particle data to allow the model to be this method can't be used if Particle camera-facing sprites updated on the GPU using systems the particles are models Systems stream-out Instancing can look poor due Advanced Particle systems are an ideal CPU / Simple instancing is processes Instancing to lack of variety condidate for instancing GPU using both CPU and GPU. Complex instancing Each particle system stores Instancing GPU render instances and techniques store more states rendering data such as UPU update instances e,g, animation data, texture position, rotation, sclae, Instance buffer must be made offsets, material settings colour, alpha available to both CPU and Each particle requires data to GPU update its position/rotation each frame

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Instancing /	Stream-out for Particles (cont)	Instancin	g / Stream-out for Particles (cont)	DX 11 - I	New Features (cont)
	Able to render models in different poses, with different- textures and material tweaks. Good for vegetation, crowds etc.		Typically we render the models twice. Pass1: Render models using instancing or similar. Pass2: Update models with stream-out - no actual rendering		Device pointer has been split in two. Device pointer for overall control and context pointer for each thread .fx not in the provided libraries
	More complex shaders can help here	Stream output	Reads from GPU buffer and writes back to one but can't		DX maths libraries not in 11 No font support
Particles	LAtest GPUs deal well with this kind of shader Instancing can be slow due to	consid era- tions	output to same buffer that is being input from. Work around this by double buffering	Pipeline	Few other minor changes Get two programmable stage:
without CPU/GPU copy	the CPU update/copy		Stream-out allows GPU only entities which is especially effective for particles.		hull and domain shaders One fixed stage in between: Tessellation
	One simple workaround is to avoid updates.		Works expecially well with the sprite-based particles technique		All three must be used to gether for tessellation otherwise disabled
	Drawback is that it is inflexible as paths are alwas the same. e.g. fountain can't be affected by wind	DX 11 - New Features	New Features DX 11 was introduced with Win7	Tessel- lation	Input geometry made of patches and control points. Vertex shader processes each
GPU stream- out for particle update	DX 10 supports stream output. Allows GPU to output vertex data back into a vertex buffer instead of sending it on for rendering.		Featres include multithreading, tessellation, compute shaders, shader Model 5.0 and high quality texture compression formats.		control pointHull shader also processes each control point but can access all points for a patch. Used for specific transforms.
	Using stream output hte GPU can be used to update particles for entities position,	DX10 DX11 Differ-	Nearly everything DX10 works with minimal change in DX11		Hull shader has an associated patch constant function which is called once per patch
	rotation etc Both render and update data is stored GPU only	ences			Tessellation stage tessellates the patch as required

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DX 11 - Ne	ew Features (cont)	DX 11 - N
	Domain shader takes the generic tessellation and control points and creates the final vertices	Tessel-
Patche- s/control points	A Patch is a line, triangle or quad which is bent or shaped by some number of control points	lation Stage
	DX does not specify the available patch types	
	This is potentially a huge change for game asset creation	
Hull shader	Gets access to all control points for a single patch and can [rpcess them in any way	Domain Shader
	Output: Final control points used to shape the patch. MAy output greater or fewer points if	
	necessay Can be used for advanced purposes like approximating	
	complex input splines using simpler output splines. providing per control point info to help the patch constant	Distance / Density Variation
Patch Constant Function	Called once per patch - decides how much to tessellate each patch	
		Water

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DX 11 - New Features (cont)				
	Access input control points and the hull shader output control points as array to do its job			
Tessel- lation Stage	Uses factors specified in the patch			
	Divides up a unit square, triangle or line based on the factors			
	works in a generic 0->1 space			
	Several fixed algorithms are avaliable for the tessellation			
Domain Shader	Takes control points output from hull shader and the generic vertices output from the tessel- lation stage			
	Combine to create final tessel- lation for the scene			
	Exactly whatthis involves depends on the patch type.			
Distance / Density Variation	Common to vary amount of tessellation based on the geometry distance			
	Distance variation is simpler			
	Density variation needs pre-pr- ocessing			
Water tight patch seams	As as tessellation is varied there are problems with patch seams cracks in geometry appear			

### DX 11 - New Features (cont)

	That is why we can control the edge tessellation separately to ensure all edges have the same tessellation factor. Adjust height of vertices			
Displa- cement Mapping	Adjust height of vertices			
	Effectively this parallax mapping done properly			
	Result has correct silhouettes and no visual problems			
Technical Issues	Tessellation has performance implications			
	Displacement mapping brings more seam issues			
	Models must be designed with			
	displacement in mind			
_	displacement in mind			
Sterescopic				
Sterescopic Depth				
	Rendering Number of depth cues in a			
Depth Perception	Rendering Number of depth cues in a			
Depth Perception	Rendering Number of depth cues in a 2D image/video			
Depth Perception	Rendering Number of depth cues in a 2D image/video Pos and perspecive			
Depth Perception	Rendering Number of depth cues in a 2D image/video Pos and perspecive Known sizes of objects			
Depth Perception	Rendering Number of depth cues in a 2D image/video Pos and perspecive Known sizes of objects Visible detail			
Depth Perception	Rendering Number of depth cues in a 2D image/video Pos and perspecive Known sizes of objects Visible detail Motion Parallax			

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distance fog

just moncular vision

from having 2 eyes

We gain additional cues

None of these require 2 eyes

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Binocular

Vision

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### Sterescopic Rendering (cont)

Image in each eye is different

Brain resolves into one image with depth

Not sure if this will come up in exam so only covered briefly

### Animation: Interpolation

**Interpolation** is where a calculation is made to decipher a transform between 2 control transformations of a model

An animation is stored as a sequence of key frames (or transforms).

In order to get the frames in between the key frames, interpolation is used

Interpolation occurs in alpha blening and skinning

Linear Interpolation (Lerp)

Interpolation between two mathematical elements (could be points) P0 and P1

P(t) = P0(1-t) + P1t

Where t is typically in the range [0, 1] and the start and end elements are P0 and P1 respectively.

The interpolated point will be on a straight line in between P0 and P1, hence linear interpolation

### Normalised Lerp (Nlerp)

Can use Linear Interpolation for transformations including translations, scaling and rotations, however, the results for rotations is not correct, resulting in unwanted scaling. Therefore, Nlerp or normalised Lerp is required for rotation.

This works however, the angles can still be inaccurate. Can use Nlerp for rotations if the overall rotation is small enough.

### Spherical Linear Interpolation (Slerp)

Linear interpolation of angles is sameas linear interpolation of an arc on a sphere.

Forumla different from linear interpolation (Lerp)



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### Animation: Interpolation (cont)

 $slerp(P1, P2, t) = P1(P1^{-1}P2)^{t}$ 

More suited for larger rotation as it calculates the correct interpolated rotation

Slerp for Matrices: Substitute the matrices into the forumla. Required to raise the matrix to the power with t. This means that we need to convert the matrix to an axisangle format then calculate theta<sup>t</sup> then convert back.

#### This is very expensive

Slerp for Quaternions: The only thing that makes it make expensive is the sine function. There can be accuracy problems for small theta, but more useable than the matrix version

Quaternion formula: slerp(P1, P2, t) = (sin((1-5)theta)P1 + sin(t theta) P2) / sin(theta)

### Summary

Can use Lerp for positioning and scaling

For small rotations use nLerp

For larger rotations use Slerp

Rotations should be stored as quaternions if interpolation is involved as matrices are expensive

### Animation: Practicalities

Matrices are not good at animations as they are performance heavy use far too much storage, so quaternions should be used instead

We can decompose the transformation into rotation, translation, scale etc., using vectors for translation and scale and quaternions for rotation

### Spatial Partitioning

Spatial	is any scheme that divides the
Partit-	game world into smaller spaces
ioning	
	Needed for larger cools games

Needed for larger scale games

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### Spatial Partitioning (cont)

-	
Problems with Large Games	Complex games can contain millions of instances
	The majority of instances are likely to be far from the player
	We would like to cull these instances instead
Simple Culling Methods	Can cull entity instances against the viewing frustum. This is the volume of space visible from the camera, which is a cone with its head cut off.
	Check each instance against each of the 6 planes defining the frustum or more simply rejecting those beind the camera near clip plane
	Use bounding volumes and simple maths like boxes or spheres
Rationale for Spatial Partit- ioning	Culling instance one-by-one is not the best approach for very complex environments. There are too many instances to even consider in one frame.

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Spatial Pa	rtitioning (cont)	Spatial	Partitioning (cont)	Spatial Parti	tioning (cont)
	Need to reformulate problem and don't process non-visible instances at all		This can help in a variety of non- rendering situations. For example a game can be partit-		These sectors can also simplify lap processing which can include distance covered,
	Partitions can be seen as chunks of space and instead identify which partitions are invisible allowing use to accept		ioned into levels. Another example could be loading or releasing resources when moving between different partitions. Or having new		telemetrics or detecting whether you are going the wrong way around a race track.
	or reject large groups of instances at once.		pp or lighting effects or changing music etc.	Visibility/A- udibility	Paritions can be used to determine whether you can
Simple Example	Most space partitioning schemes use some form of	Game Logic	Space partitions can also help with game logic		hear sound past a concrete wall for example.
	graph to subdivide the world where each node represents a space. Shape of the spaces		For example a race track can be split up into sectors where only the current and neighbouring sectors	Potentially Visible Sets (PVS)	Each node in a space partition has a potentially visible set (PVS)
vary by scheme. The edges represent how the spaces are related or connected.	enable AI physics and rendering because AI race cars which are far away don't need physics etc.		These are the nodes that can in some be seen from that node. For example, you can		
	One example shows a very basic partition/graph demons- trating how areas in the sene are connected and how a group of instances can be reject by		because you can't see them.		see the living from the hallway because you can see through an open door. (Diagram shown in lecture slides)
	one check. (Refer to lecture slides for diagram)				PVS can be pre-calculated and stored with each node.
Level Division	Space partitions are not just for visibility checks				This indicates which other nodes to render whe in that node.
				Generating PVS	A PVS scheme is concep- tually simple

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Spatial	Partitioning (cont)	Spatial Pa	artitioning (cont)	Spatial	Partitioning (cont)
	However, generating the PVS for each node is non-trivial		So whilst efficent to execute, PVS systems are not ideally effective in node rejection.		Now we know the nodes connected through the visible portals are also visible
	Possible approaches include using brute force, which considers many different camera positions. This can be slow and result in possible	PVS Use	PVS system is not space partit- ioning scheme as such PVS can be added to any space	Refine ments	When a visible portal is found store its viewport dimensions (2D rectangle)
	rors. You can manually create /S. This can only be possible for mpler graphs and is error prone.		partition graph regardless of shceme used		Clip portals in the connected node against this smaller area. Reject
	Finally mathematical/geometric approaches can be used, which are complex and often have limita-		USed as a quick way to renduce the number of nodes under consideration		obscured nodes Watch out for multiple portals leading to same nodes. We don't
	tions	Portal Systems	A Portal system is a method that concetrates on the graph edges	Portal	want to render nodes twice. Cheao and simple implement
PVS Limita tions	imita geometry. For exampe if you have	Cyclonic	Spaces in such a system are connected through portals. A	Pros	Effective for indoor geometry
uono	then the door must be considered as open for PVS		portal is typically a natural opneing such as a door or		Portals can handle dynamic gemometry (unlike PVS)
	Potentially visible sets must be conservative. For example, a node		window Portals allow us to reject other		Each portal with 2 sides don't need to be in the same place.
	visible from only a tiny portion of the current node would need to be		nodes based on the camera view	Portal Cons	Can be tricky to know which node a partiuclar point is in
	entirely visible	Basic Portal usage	Identify which node the camera is in		
			Identify whether each of the node's portals are visible in the		

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viewport

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	Need to know which node the camera is in to start the		Need to map between world space coords and grid indices	Quadtrees for	USe for frustum culling
	algorithm. e.g. what if a camera travels through a wall or teleports?	Conver- sions for	GridX = (int)(GridWidth * (WorldX - MinX) / (MaxX -	visibility culling	
	Portals are of little use for open	X dimension	MinX))		Viewing frustum is 6 planes
	areas	are (Y		Quality	Test if a node is visible
	Not easy to automatically generate portals from arbitrary	similar):	WorldX = Min +(float)GridX *	Quadtree Problem	Entities aren't points
	geometry		(MaxX - MinX) / GridWidth		May overlap a node boundar
Grids as Spatial	Can collect local entities for visibility culling like Al		2nd formular gives bottom-left of grid square		Entity needs to be in a larger parent node
Partitions	Can be used to map terrain (Height/influence maps)	Quadtrees / Qctrees	Quadtrees / Qctrees are hierarchical partition systems which use a tree structure to		Worst case: entities overlaps origin and does not fit in any node except root and will never be culled
	Can be extended to 3D		represent an area/volume of		Hot-spots like this all the way
Disadv- antages	May have many empty nodes, wasting memory, reducing		space. USe specific division scheme		around the boundaries of larger nodes.
to Grids as SP	cache efficency		Quadtrees are in 2D, Octrees in 3D	Solution	Loose Quadtrees
	Choice of partition size tricky -	Creating a	Root node is entire space		Have nodes overlap
	too small gives many empty odes, too large and culling etc.	Quadtree			Entities will then fit in original node area
	is ineffective		Divide into four equal quadrant		Few changes to algorithm - increase node size when
Mapping a Grid to	A grid is an integer indexed structure for a rectangle of		Repeat division with each quadrant		inserting entities and when doing frustum culling
the World	world space		Until some condition is met - max depth, empty node etc.		Removes hotspot problem
		Location in a Quadtree	Easy to find which node point is in		
			Can be optimised		
			Can use bitwise integer math		

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Spatial Parti	Spatial Partitioning (cont)		Spatial Partitioning (cont)		
Quadtrees for Collision	At the expense of larger nodes at the same level Saw intersection of viewing frustum with quadtree		Stop when max x elements in each partition. Partitions are small enough. tree reaches certain depth and choice depends on application		
Detection	Easy to find intersection of other primitives - sphere,	Locating a Point in a BSP	Given a point, each to find which partition it is in. Start at root of tree		
	cuboids, rays etc. Basis for collision detect-		Look at example in lecture slides		
	ion/ray casting/particle systems	BSP for solid/-	Can use the polygons in the scene as the division planes.		
	Can help if we add adjacency info to the tree	hollow spaces	Choose a polygon as a plane and polygons crossing the planes are split		
Binary Space Partit-	Hierarchical division of space and uses another tree structure. This one represents		BSP splits space into hollow/solid volumes		
ioning (BSP)	all space		All polygons/entities places in hollow ones		
	Partitions are separated by lines in 2D or planes in 3D	BSP / Brush	Traditional style of BSP used for FPS games		
	Recursively divide each partition into 2 smaller ones	modelling	In conjunction with PVS		
	Creates a binary tree		Can also be used to render		
Creating a BSP	Repeatedly divide space in 2		partitions in a strict back to fron order		

### Spatial Partitioning (cont)

	moc You cut o hollo	ds itself to a unique form of 3D lelling called brush modelling. start with a entirely solid world, out primitives, entities paces in owed out areas. This is like ing out the level.
BSP Pros and Cons		P trees are a well established nique
	+Us traci	ed for rendering/collision/ray ing
	+Ca	n be generated automatically
	+Fu	lly Classify space
		ed good algorithm to choose ling planes
		low/solid BSP generates extra gons due to splitting
Deferre	d Re	ndering
Forwar Render	~	Name for the method of rendering we have used in all material so far

rward ndering	Name for the method of rendering we have used in all material so far
	Render geometry and light effects on the geometry in single pass
	Cost = numObjects x NumLights - Get's very expensive

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Deferred Rendering (cont)		Deferred F	Rendering (cont)	Deferred Rendering (cont)
	Forward rendering can be effective but need a slow uber- shader or lots of shaders and		Large g-buffer results in major performance drain - memory access is slow	+Better batching performance +G-buffer data can eb reused for Post-P- rocessing
	batch problems Doesn't work well with lots of lights in one place		So data compression in the g- buffer is common ie store x and y of normal together with a single bit for direction	-Huge g-buffer can be a slow down -G-Buffer compression to counter this reduces material flexibility
Deferred Rendering	Decouples geometry from lighting	Lighting Volumes	G-buffer is not displayed	-Transparant obkects don't work, must be rendered separately
	Splits the rendering process into 2 stages Cost = NumObject + NumLights - Much cheaper	volumes	Render actual scene by going through each light and rendering it's effect on the geometry	-MSAA becomes very diffcult due to g- buffer -Not actually particularly useful in some
G-Buffer	Render geometry to g-buffer, which is several textures holding geometry and surface data		Point light lights up a sphere around itself. Render the sphere around the point light. For each pixel find if it is actually lit up.	scenes(daylight) More advanced techniques are getting ver complex Optimisation for Games
	Example: Texture1: Diffuse Colour Texture2: WorldP- osition Texture3: WorldNormal		USe data in g-buffer to calculate amount of light. Do this for every light and accumulate = rendered scene	Optimisation Tradeoffs Reducing memory use can decrease spee
	Pixel shader can render to several render targets at the		Same concept for spotlights	Increased speed might be at the expense of memory
	same time, so can build three textures all in one pass with a special pixel shader		Don't need high-poly spheres or cones Examples shown in lecture	When not to optimise Never optimise code unless you are sure that is affects performance
	MRT = Multiple Render Target	Deferred	+Lights become cheap to	Optimisations usually harm readability/mai
	Data in g-buffer is anything we need to calculate lit version of the scene	- Pros and Cons	render	ntainability of code Can reduce functionality
			+No need for complex partit-	Can make architecture less flexible Performance Analysis
			ioning +Shaders become simpler - less of them	Generally, 90% of processor time is spent on just 10% of code
				Need to identify the 10% to optimise effect

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of code during run-time

Tools can be used to analyse performance

ively

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#### **Optimisation for Games (cont)**

Performance Analysis Tools

-Simple timing functions

-Profiler - Reports on time spent in different functions

-Specialist tools like VTune, PTU, PerfKit, PerfHUD etc.

#### **Compiler Optimisations**

Compilers can perform some optimisations Optimisations can be enabled using release mode in visual stuido.

#### **Basic Language Optimisations**

-Loop Untrolling - Does not loop through indices, just duplicated lines of code instead

-Remove constant calculations by using a variable outside a loop for example

-Change ording of conditions, like OR for example. Put simple condition first

-Pass by reference not copy

-Use early return within functions whenever possible

-Inline functions - stores functions in cache but can be ignored by compiler

-Break code into smaller steps. For example, don't have calculations inside if statements. Does not directly lead to optimisations but can help compiler optimise.

-Try programming in assembly, although it would be very complex and compliers would probably do a better job.

#### **Data Structure Choices**

-Static structures like fixed arrays might improe performance over dynamic ones

-Only choose data structures that suit your needs, nothing more

#### Algorithmic Improvements

-Can multiple by 0.5 rather than dividing by 2

-Reduce nesting of loops - don't go deeper than 3



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### Optimisation for Games (cont)

Alpha Sorting and Soft Particles
-Remove code completely!
-Pre-calculate formulae using look-up tables
-Reduce maths operations
-Cluster similar cases into one
-Sort data into more convenient orders
-Reduce range of loop counters

Alpha Sorting Problems	Attractive blending technique but cuases sorting issues
	Problem is depth buffer ignores transparancy
	Avoid problem by drawing polygons back to front.
Run-time Depth Sorting	If all polygons face camera ie particle system then you can sort polygons based on camera-space z distance
	Issues arise with this based on example shown on slides with the lines
	To solve this assume polygons don't intersect
	Then given 2 polygons one of them will be entirely on one side of the plane of the other
	Identify this polygon and see if it is on the side nearer the camera or not

### Alpha Sorting and Soft Particles (cont)

	First step is to get a face normal for each polygon
	Join either point of polygn 2 to eachh of the points polygon 1. Calculate dot products of these with normal of polygon 2. Results all +ve : poly 1 is nearer. Results all -ve: poly 1 further. Results mixed: poly1 is split by place of poly 2. So repeat test the other way around. If split both ways then the polygons are intersecting. Refer to slides for diagrams etc.
Run- time sorting practi- calities	Must ensure this sorting is efficient as possible. so sort pointer to polygon not polygon data itself
	In practice, another technique alpha-to-coverage is often used as an alternative.
Hard Flat particles	Alpha blending is as useful as other blending methods once the polygons are sorted
	However all blending methods exhibit hard edges if they intersect other polygons

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Alpha Sorting and Soft Particles (cont)	
	Particuarly large particles like smoke indoors
Soft Particles	To improve further we can compare depth of particle with depth already in buffer and then fade pixels out when the distance is small Adjust alpha toward 0
Depth- Soft Particles	This method can be combined with the depth particles idea presented earlier
	We must do some detailed work with depth buffer but almost completely removes hard edges where alpha particles intersect solid objects.
Further Possib- ilities	Can explore volumetric particles - consider the volume of particle that camera is looking through.
Linear Dy Physics	namics and Particle based
Particle	Data: Position, velocity,

System Basics

### Linear Dynamics and Particle based Physics (cont)

Fliysics (	
	Particle velocity must change or it will only movie in a straight line. Change in velocity is called acceleration. Acceleration caused by forces on particle. Gravity is common force.
Particle Update	F=ma
	Use above formula to update particle each frame
	Diagram shown in lecture slides
Aprox. in this update	This ibasic physics of forces, acclerations and velocities doesn't just apply to particles. Starting point for modeling physics too.
	Problem: Approach is only an approx. we only update things once per frame. Assumes vecocity was constant over entire time period of rame. This is wrong - forces/acceleration will change gradually throughout frame. Whereas our simple approach changes the velocity isntantly to a new value each frame.

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possibly mass

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# Linear Dynamics and Particle based Physics (cont)

Initial Value	Example of this is when you have a particle following an orbit around an object. Over time the particle will move further away from the object it is orbitting. This is down to approximations and is wrong. Updating particle pos is an example of an initial value
problems	problem. We know the value of an equation at an initial point in time. Want ot calculate value at some furutre point in time.
	In this case we know pos and velocity from this frmae. Want to know position and velcity for next frame. The simple but flawed method just shown is one way of solving an initial value problem. Will present others with better accuracy.
Formal Definition	Function which changes over time: p(t)
	Initial position/veclocity: p0 (where t = 0)
	Time period: h
	Value next frame: p(t0 + h)
	Need derivatives: p'(t), p"(t)

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Linear Dynamics and Particle based Physics (cont)			Linear Dy Physics (
	1st derivative of pos = velocity. 2nd = acceleration		
Euler's Method	Taylor series is a represenation of a function based on the deriva- tives at a single point (int time)		
	$\begin{split} p(t+h) &= p(t) + hp'(t) + h^2/2p''(t) + \\ h^3/3!p'''(t) + \ldots + h^n/n!p^{(n)} + \ldots \end{split}$		
	Arranged here to suit our problem		Mid- point
	p is pos, p' velocity, p" accele- ration, p'" acceleration of accele- ration		Method
	As h is smaller aprrox is more accurate		
	IT is an infinite series - cannot be completly calculated		
	Eulers Method uses just the 1st two terms in the series and assumes the rest are small		Basic Verlet Method
	enough to ignore. Translation into games terms:		
	posNextFrame = currentPos + frameTime * currentVelocity		
	veclocityNextFrame = currentVe- locity + frameTime * currentAccel		

# Linear Dynamics and Particle based Physics (cont)

	This is exactly the method presented earlier for updating particles in a particle system. Not ideal, terms are ignored (not always small). Still widely acceptable when accuracy isn't required.
Mid- point Method	Problem with Euler's method is that velocity and acceleration are taken at the start of the frame.
	The mid-point method takes them half way through the frame.
	This has better accuracy than Euler's method but not perfect as half-way values are themselves approx.
Basic Verlet Method	Less reliant on velocity
	Can be resrictive because of that
	OK for particle systems if only concerned with position
	Most basic method: uses pos from the current and previous frame and uses current accele- ration
	formula: $y(t+h) = 2y(5) - y(t-h) + h^2y''(t)$

# Linear Dynamics and Particle based Physics (cont)

	posNextFrame = 2 * currentPos - posLastFrame + (frame time) <sup>2</sup> * currentAccel- eration Has similar accuracy to mid- point method
Particle Physics - Springs	Forces involved: Gravity, spring compression and spring stretch
	Considers particle mass
Spring Forces	Force exerted by spring is from Hooke's Law: F = -kx
	x = displacement for spring's equilibrium pos
	k = spring coefficent (stiff- ness)
Practical- ities	Real life systems slow down with friction
	Instead of friction we will damp the motion
	Damping force: Fd = -cv
	v = velocity
	c = damping coefficent - works against current velocity range: 0-1
Uses	Can model rope, cloth and jelly-like objects
Different Connectors	Can use new connetor type such as elastic, rods and string

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Linear Dynamics and Particle based Physics (cont)		Advanced Graphics: Scene Post-Proc- essing (cont)		Advanced Graphics: Scene Post-Proc- essing (cont)	
	Key difference introduced: Some types behave differ- ently when stretched and compressed, some are constrained, some don't exert forces at some times.		After frame rendering the back buffer is copied to the front buffer This is a form of double-buffering		Alternatively can copy to front buffer immediately May see tearing
Constraints		Swap method s/c- hains	Methods to get the back buffer content to the front buffer involve a simlpe copy were the back buffer is discarded or te 2 buffers are swapped which is useful if we want to keep the last frame	Altern- ative Render Targets	Not necessary to render to a back buffer
Constraints	Rods and strings have constraints. Rods must always be same length and			Targets	We can render to a texture or to a specially created render target
Mathem-	string cannot be longer than original length Each constraint can be		Can have more than one back buffer. This is known as triple-bu- ffering		Can create explicit render targets or render to multiple render targets
Approaches rating then fixed length	between particles such as:		Improved concurrency with GPU Multiple back buffers must use the swap method which is called a swap chain	Scene Post-P- roc- essing	Assume we render the entire scene to an intermediate texture
	p is particle pos and L is fixed length of connecter Several constraints we have	VSync or Not	Copy/swap is fast operation		Can then copy it to back buffer to be presented to the viewport but we can also perform additional
	several equations Known as a system of linear equations		monitor's vertical sync If you do this though the FPS will		image processing during this copy
Solving Constraints	Of the various mathematical solutions most have a similar repeated iterative approach.		be tied to monitor refresh rate		The copy process is effectively another rendering pass so the look of the scene is altered through pixel shader
A	Examples shown in slides				This is full-screen post-proc- essing
essing	aphics: Scene Post-Proc-			Multiple Passes	Can post-process in multiple passes
Front/back	Visible viewport can be called			/	

front buffer A 2nd off-screen back buffer is the usual render target

buffers

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Render Targets

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### Advanced Graphics: Scene Post-Processing (cont)

The textures used do not have to all be the same size so that you can scale down and back up for blur for example

Can make complex sequences of post processing like bloom.

Don't need to talk any more about Post Processing - Should be confident from assignment

### Water Rendering

Visual Aspects of Water	Reflection, refraction, fresnel effect, kught extinction, surface deformation, foam/spray/c- austics and underwater effects
Reflection	Water behaves to some degree like a mirror
	Perfectly still water presents a perfect reflection
	Surface deformation presents practical difficulties as the normals vary
Reflection Practical- ities	Can be dynamic, movement in scene is reflected
	Or static - Just skybox reflected

Water Rendering (cont)

Static case - Cube mapping works effectively, reflect ray from camera off the surface normal and into a cube, hlsl support for cube-mapping makes this simple, works without difficulty with varying normals

Dynamic reflections - cube mapping not effective so reflect the camera in the plane of the water, render the scene from this reflected camera into a texture, draw the water surface mapped with this reflection texture

Varying normal can be simulated by offsetting which part of the reflection texture sampled

Not a fully robust solution. Reflections might come from parts of the scene that were not rendered in the reflection texture. Approach only works perfectly for completely flat water

### Water Rendering (cont)

	Alternative approach is to use ray-tracing or similar
Self-Refl- ection	If the water surface is choppy enough it may reflect other parts of the water
	Reflection and refraction require multi-pass approaches to do properly however don't need to do it properly in most cases
	Static cube mapping: Lower half of cube map not really needed so draw the upper half reflected
	Dynamic reflected camera: render the water in the reflection texture using static cube mapping
Refraction	Where light crosses the interface between 2 different materials it bends
	Amount of bend is given by Snell's Law
	Depends on: Angle of incidence, refractive indexes, vacuum has a refractive index of 1, clean water is 1.33
	n1sin(theta1) = n2sin(theta2)

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Water Rendering (cont)		Water Rendering (cont)		Water Rendering (cont)	
Refraction in Water	When looking into water, light coming from under the water is bent and the scene at the water surface appears shifted and distorted		In practice: Create 2 textures, render sabove water scene(ref- lected) to 1 and the below water scene to the other. Clip each of these scenes at the water surface		F gives the proportion of reflected light coming from the surface, the remainder comes from refraction. e.g. if F = 0.3 at a point on the surface. Point emits 30% reflected light and
	Amount of shift/distortion depends on: angle at which we view the surface, variations in the surface shape - waves ripples, both of these vary per pixel		Render water surface blending reflection and refraction textures		70% refracted light Fresnel formula calculated in
			Blending amount depends on viewing angle		pixel shader giving a blending ratio for the reflection and refraction textures
Refraction - Practical- ities	Refraction typically rendered in the manner of a post processing effect - similar to distorted glass	Fresnel Effect	To do with viewing angle and blending of textures	Light Extinction	Light attenuates in water as well as air
			Effect depends on the material involved		The effect in water is much stronger though
	Process - Underwater parts of scene rendered to texture, water surface is rendered and this texture is applied,		$F = F0 + (1 - F0)(1 - N \cdot C)^{5}$ $F0 = ((n1 - n2)/(n1+n2))^{2}$	Practical- ities	Effects refracted light only
			n1, n2 are the refractive indexes of the material		Need to know how far light has travelled
	distortion is applied to UVs Fully robust system would be complex		N = surface normal C = Normal to the camera		
Combining reflection and Refraction	Both involve rendering scene to texture				

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#### Water Rendering (cont)

Several approaches can be used: e.g. render water surface only to texture, store only its world space distance from camera, when renedering refraction texture subract the distace of each underwater pixel from the water surface distance at the same point. Gives distance the light travels through water to surface. Linearly belend RGB components based on this distance and the extinction distances given. Water surface distance texture created in the 1st step can aslso be used to do the above/below water clipping

For surface normals you can animate normal maps to get a wave or ripple effect etc.

Refer to lecture for more detail

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