

Basic Syntax

<code>null []</code>	return <i>True</i> if list is empty
<code>'H' `elem` "Hello"</code>	return <i>True</i> if H is in the string
<code>head [1,2,3]</code>	return 1
<code>tail [1,2,3]</code>	return [2,3]
<code>last [1,2,3]</code>	return 3
<code>init [1,2,3]</code>	return [1,2]
<code>:t</code>	return the type
<code>fst (5,2)</code>	return 5
<code>snd (5,2)</code>	return 2
<code>1:2:3:[]</code>	same as [1,2,3]
<code>length []</code>	give length of list
<code>reverse []</code>	reverse the list
<code>[] !! n</code>	gives the <i>nth</i> element
<code>filter test []</code>	return everything that passes the test
<code>[] ++ []</code>	list concatenation
<code>[] : []</code>	list concatenation
<code>drop n []</code>	delete the first <i>n</i> element from list
<code>take n []</code>	make a new list containing just the first <i>N</i> element
<code>splitAt n []</code>	split list into two lists at <i>nth</i> position
<code>zip [a..] [0..]</code>	combine two list into tuples [(a,0)..]
<code>map function []</code>	apply a function to all list elements

Terminology

Terminology (cont)

Type	Lower case, can be of any
Variable	type. e.g. <code>fst::(a,b)->a</code>
Typeclass	A sort of interface that defines some behavior. Basic type classes: Read, Show, Ord, Eq, Enum, Num. Num includes <i>Int</i> , <i>Integer</i> , <i>Float</i> , <i>Double</i> .
Higher-ordered Functions	A function that takes other functions as arguments or returns a function as result. Ex: <code>foldl</code> , <code>foldr</code> , <code>zipWith</code> , <code>flip</code> .
Module	A collection of related functions, types and typeclasses
Referential Transparency	An expression is called referentially transparent if it can be replaced with its corresponding value without changing the program's behavior.

substituting equals for equals, different from other programming languages

Type Signatures

In type signature, specific (*String*) and general (*a,b*) types can be mixed and matched.

<code>concat 3 :: String -> String</code>	Functional Use recursion instead of iteration
<code>const :: a -> b -> a</code>	Allows operations on functions
<code>allEqual :: (Eq a) => a -> a -> a -> Bool</code>	Lazy Don't do an operation unless you need the result.
<code>(.) :: (b -> c) -> (a -> b) -> a -> c</code>	

Type Signatures (cont)

Lambda function, lead with `\`, then arguments, then `->`, then the computation

Data Types

Haskell uses various data types, all of them starts by a capital letter:

- Int**: Integer number with fixed precision
- Integer**: Integer number with virtually no limits
- Float**: Floating number
- Bool**: Boolean. Takes two values: True or False.
- Char**: Character. Any character in the code is placed between quotes (').
- String**: Strings (In fact, a list of Chars).

Properties of Haskell

Pure	No side effects in functions and expressions
	No assignment operators such as <code>++</code> and <code>=+</code>
	<i>I/O is an exception</i>
	Promotes referential transparency
	Once <i>x</i> is assigned to a value, the value stays the same
	Functional Use recursion instead of iteration
	Allows operations on functions
	Lazy Don't do an operation unless you need the result.
	<code>(\x->1.0+x)^5</code>

Recursive Descent Parser

```
-- our parsers generally are of
type Parser [Ptree]
data Ptree = VAR String | ID
String | FCN String [Ptree]
deriving (Show, Eq, Read)
data Presult a = FAIL | OK a
String deriving (Show, Eq, Read)
type Parser a = String ->
Presult a
```

Polymorphic Types Families of types. For example, $(\text{forall } a)[a]$ is the family of types consisting of, for every type a , the type of lists of a . Lists of integers (e.g. $[1,2,3]$), lists of characters ($['a','b','c']$), even lists of lists of integers, etc., are all members of this family.



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Recursive Descent Parser (cont)

```
> -- As before, we use &> and |> as AND /
OR combinators on parsers
expr = variable |> fcnCall |> identifier
fcnCall = buildCall . (identifier &> skip "(" &>
arguments &> skip ")")
arguments = expr &> argTail |> empty
argTail = skip "," &> expr &> argTail |>
empty
identifier input = beginsWith ID Data.C-
har.isLower isTailChar (dropblank input)
variable input = beginsWith VAR Data.C-
har.isUpper isTailChar (dropblank input)
empty = OK [] -- empty string parser always
succeeds
```

UTILITY ROUTINES

```
-- Parse a string but don't save it as a parse
tree
skip :: String -> Parser [a]
skip want input =
    let found = take (length want) input
        remainder = dropblank (drop (length
want) input)
    in
        if want == found then OK [] remainder
        else FAIL
-- Build a singleton list of a function call
parse tree from a list with
-- an identifier followed by list of arguments
buildCall :: Presult [Ptree] -> Presult [Ptree]
buildCall FAIL = FAIL
buildCall (OK [] _) = FAIL
buildCall (OK (ID fcn : args) remainder) =
OK [FCN fcn args] remainder
-- Build a singleton list of a parse tree given
the kind of tree we want
-- and the kinds of head and tail characters
we want
beginsWith :: (String -> Ptree) -> (Char ->
Bool) -> (Char -> Bool) -> Parser [Ptree]
```

Recursive Descent Parser (cont)

```
> beginsWith _ _ _ "" = FAIL
beginsWith builder isHead isTail (c:cs)
    | isHead c = let tail = Data.List.takeWhile
isTail cs
    in OK [builder (c:tail)] (dropblank
(drop (length tail) cs))
    | otherwise = FAIL
-- Remove spaces (and tabs and newlines)
from head of string.
--
dropblank :: String -> String
dropblank = Data.List.dropWhile Data.C-
har.isSpace
-- kind of character that makes up 2nd - end
character of an id or var
--
isTailChar :: Char -> Bool
isTailChar c = Data.Char.isAlphaNum c || c
== '_'
-- Concatenation and alternation operators
on parsers
-- (|>) is an OR/Alternation operator for
parsers.
--
infixr 2 |>
(|>) :: Parser a -> Parser a -> Parser a
(p1 |> p2) input =
    case p1 input of
        m1 @ (OK _ _) -> m1 -- if p1
succeeds, just return what it did
        FAIL -> p2 input
-- (&>) is an AND/Concatenation operator
for parsers
infixr 3 &>
(&>) :: Parser [a] -> Parser [a] -> Parser [a]
(p1 &> p2) input =
    case p1 input of
        FAIL -> FAIL -- p1 fails? we fail
        OK ptrees1 remain1 ->
```

Recursive Descent Parser (cont)

```
> case p2 remain1 of -- run p2 on
remaining input
    FAIL -> FAIL -- p2 fails? we fail
    OK ptrees2 remain2 -> -- both
succeeded
    OK (ptrees1 ++ ptrees2)
remain2
```

Tree

```
data Tree a = Leaf a | Branch a (T
treeEq :: (Eq a) => Tree a -> Tree
treeEq (Leaf x) (Leaf y) = x == y
treeEq (Branch x1 l1 r1) (Branch x
treeEq _ _ = False
treeShow
treeShow :: Show a => Tree a -> [C
treeShow (Leaf x) = " (Leaf " ++ s
treeShow (Branch x left right) = "
"
```

Preorder via standard recursion

```
preorder :: Tree a -> [a]
preorder (Leaf x) = [x]
preorder (Branch x left right) = x
Tail-recursive traversal
preorder' :: Tree a -> [a] -> [a]
preorder' (Leaf x) xs = x : xs
preorder' (Branch r left right) xs
```

Function Syntax

```
addFour w x y z =
    let a = w + x
        b = y + a
    in z + b
-----
addFour w x y z =
    z + b
```



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Pattern Matching (cont)

```
data Pattern a = P a | POr (Pattern a) (Pattern a) | PAnd (Pattern a) (Pattern a) deriving Show

match pattern [] = (False, [])
match (P x) (y : ys) = if x == y
  then (True, ys) else (False, y : ys)
match (POr pat1 pat2) xs = case m
  atch pat1 xs of
    (True, leftover) -> (True, leftover)
    (False, _) -> match pat2 xs
match (PAnd pat1 pat2) xs = case
  match pat1 xs of
    (False, _) -> (False, xs)
    (True, leftover) -> case match pat2
  leftover of
    (False, _) -> (False, xs)
    (True, leftover2) -> (True, leftover2)
```

Regex Examples

Natural numbers with no leading zeros except just 0

`0 | [1-9] \d*`

Floating point numbers w/o leading zeros

`(0 | [1-9] \d*.\d* | . \d+)?([eE][+-]?[0-9]+)`

Hex numbers allowing leading zeros

`0x[0-9a-fA-F]*`

Strings with an even #a's or number of b's divisible by 2

`(b*ab*a)*b*((a*ba*ba*b)*a*`

Match regular expressions using backtracking

Match regular expressions using backtracking (cont)

```
> match Rend str = FAIL
match Rany "" = FAIL
match Rany (c : cs) = OK [c] cs
match (Rch ch1) "" = FAIL
match (Rch ch1) (str @ (ch2 : left))
  | ch1 == ch2 = OK [ch1] left
  | otherwise = FAIL
match (Ror exp1 exp2) str =
  case match exp1 str of
    FAIL -> match exp2 str
    result1 @ (OK match1 remain1) ->
      case match exp2 str of
        FAIL -> result1
        result2 @ (OK match2 remain2) -
>
      if length match1 >= length
match2
match (Rand exp1 exp2) str =
  case match exp1 str of
    FAIL -> FAIL
    ok @ (OK match1 remain1) ->
      extend match1 (match exp2
remain1)
match (Ropt exp) str = match (Ror exp
Rnull) str
match (Rstar exp) str =
  case match exp str of
    FAIL -> OK "" str
    OK match1 remain1 ->
      if match1 == "" then OK "" str
      else
        extend match1 (match (Ror
(Rstar exp) Rnull) remain1)
extend match1 (OK match2 remain2) = OK
(match1 ++ match2) remain2
extend match1 FAIL = FAIL
-- mkAnd string = the exp that matches
each character of the string in sequence.
--
mkAnd (c : "") = Rch c
mkAnd (c : cs) = Rand (Rch c) (mkAnd cs)
```

Match regular expressions using backtracking (cont)

```
> --
mkOr (c : "") = Rch c
mkOr (c : cs) = Ror (Rch c) (mkOr cs)
```

More Examples

```
(Find out whether a list is a
palindrome)
isPali ndr ome'' :: (Eq a) =>
[a] -> Bool
isPali ndr ome'' xs = foldl
(\acc (a,b) -> if a == b then
acc else False) True input where
input = zip xs (reverse xs)
(Eliminate consec utive
duplicates of list elements)
compress :: Eq a => [a] -> [a]
compress = map head . group
(Count the leaves of a binary
tree)
countL eaves Empty = 0
countL eaves (Branch _ Empty
Empty) = 1
countL eaves (Branch _ left
right) = countL eaves left +
countL eaves right
(User- Defined Polymo rphic
Lists)
(a) Define the function foldList
which acts on user-d efined
lists just as foldr acts on
native lists.
foldList :: (a -> b -> b) -> b -
> List a -> b
foldList f init Nil = init
foldList f init (Cons x xs) = f
x (foldList f init xs)
(b) Define the function sumList
which adds up the entries in an
argument of type (List Int).
sumList :: (List Int) -> Int
sumList = foldList (+) 0
```

```

data RegExp = Rnull
              | Rend
              | Rany
              | Rch
Char
              | Ror
RegExp RegExp
              | Rand
RegExp RegExp
              | Ropt
RegExp
              | Rstar
RegExp
              der -
iving (Eq, Show)
data Mresult = FAIL | OK String
String deriving (Eq, Show)
match :: RegExp -> String ->
Mresult
match Rnull str = OK " " str
match Rend " " = OK " " " "

```

```

data ParseT = STR String | LIST
[ParseT] deriving (Show, Eq,
Read)
data PResult = FAIL | OK
[ParseT] String deriving (Show,
Eq, Read)
type Parser = String -> PResult

```



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Lecture 11 (cont)

```
> type TreeBuilder = [ParseT] -> ParseT --
LIST, for these trees
-- Note use of &> as AND and |> as OR
list = parse LIST (skip "(" &> list &> sublist
&> skip ")")
    |> skip "[" &> list &> sublist &>
skip "]"
    |> identifier)
sublist = (skip ",") &> list &> sublist |> empty
identifier = literal "x"
empty = OK [] -- empty string parser always
succeeds
-- expr = expr &> literal "+" &> identifier |>
empty
-----
-- UTILITY ROUTINES
-- Parse a string and make it a parse tree
literal :: String -> Parser
literal want input =
    let found = take (length want) input
        remainder = dropblank (drop (length
want) input)
    in
        if want == found then OK [STR want]
remainder
        else FAIL
-- Parse a string but don't save it as a parse
tree
skip want input =
    case literal want input of
        FAIL -> FAIL
        OK _ remain -> OK [] remain
-- Remove spaces from head of string
dropblank = Data.List.dropWhile Data.C-
har.isSpace
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Lecture 11 (cont)

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(&>) :: Parser -> Parser -> Parser
(p1 &> p2) input =
    case p1 input of
        FAIL -> FAIL -- p1 fails? we fail
        OK ptrees1 remain1 ->
            case p2 remain1 of -- run p2 on
remaining input
                FAIL -> FAIL -- p2 fails? we fail
                OK ptrees2 remain2 -> -- both
succeeded
                    OK (ptrees1 ++ ptrees2)
remain2
-----
-- Building a parse tree from list of found
parse trees
parse :: TreeBuilder -> Parser -> Parser
parse builder parser input =
    case parser input of
        FAIL -> FAIL
        (OK [] remain) -> OK [] remain
        (OK trees remain) -> OK [builder trees]
remain
```



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