

### Properties of Square Roots

$$\sqrt{a} \cdot \sqrt{b} = \sqrt{ab}$$

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

$$(\sqrt{a})^m = \sqrt{a^m}$$

$$\sqrt{ab} = \sqrt{|a|} \cdot \sqrt{|b|}$$

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{|a|}}{\sqrt{|b|}}$$

$$\sqrt{a^m} = (\sqrt{|a|})^m$$

$$\sqrt[n]{a} = \sqrt[n]{a^k} = \sqrt[n \cdot k]{a^k}$$

$$\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{a \cdot b}$$

$$\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$$

$$(\sqrt[n]{a})^m = \sqrt[n]{a^m}$$

$$\sqrt[n]{a} \sqrt[n]{b} = \sqrt[n]{a \cdot b}$$

$$\sqrt[n]{m \sqrt[n]{a}} = \sqrt[n]{m \cdot a}$$

### Laws of Exponents and Logarithms

Exponent Rules	Logarithm Rules
$a^m \cdot a^n = a^{m+n}$	$\log(mn) = \log m + \log n$
$\frac{a^m}{a^n} = a^{m-n}$	$\log\left(\frac{m}{n}\right) = \log m - \log n$
$(a^m)^n = a^{m \cdot n}$	$\log m^n = n \log m$

### Change of Base Formula

$$\log_b a = \frac{\log_c a}{\log_c b}$$

(OR)

$$\log_b a \cdot \log_c b = \log_c a$$

### Find an equation of a line that:

passes through two points  $y = mx + b$

that is parallel to one another isolate  $b$

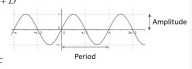
that is perpendicular to one another solve for  $x$

### Graphing Trigonometric Functions

$$y = A \sin[B(x - C)] + D$$

$|A|$  is the amplitude  
The period is  $\frac{2\pi}{B}$   
Phase (horizontal) shift is  $C$   
Vertical shift is  $D$

The same applies for the Cosine Function.  
For the Tangent Function, the period is  $\frac{\pi}{B}$

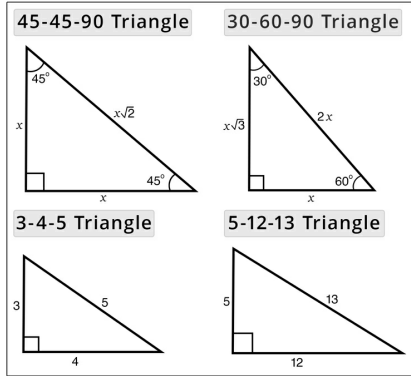


### Formulas

Distance Formula
$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

### Side Ratios

### Special Right Triangles



### Trigonometric Functions

Functions	Domain	Range
(i) sine	$\mathbb{R}$	$[-1, 1]$
(ii) cosine	$\mathbb{R}$	$[-1, 1]$
(iii) tangent	$\mathbb{R} - \{x : x = (2k+1)\frac{\pi}{2}, k \in \mathbb{Z}\}$	$\mathbb{R}$
(iv) cosecant	$\mathbb{R} - \{x : x = n\pi, n \in \mathbb{Z}\}$	$\mathbb{R} - [-1, 1]$
(v) secant	$\mathbb{R} - \{x : x = (2k+1)\frac{\pi}{2}, k \in \mathbb{Z}\}$	$\mathbb{R} - [-1, 1]$
(vi) cotangent	$\mathbb{R} - \{x : x = n\pi, n \in \mathbb{Z}\}$	$\mathbb{R}$

### Trig

Function	Domain	Range
$\sin^{-1}$	$[-\frac{\pi}{2}, \frac{\pi}{2}]$	$[-\frac{\pi}{2}, \frac{\pi}{2}]$
$\cos^{-1}$	$[0, \pi]$	$[0, \pi]$
$\tan^{-1}$	$\mathbb{R}$	$(-\frac{\pi}{2}, \frac{\pi}{2})$
$\csc^{-1}$	$\mathbb{R} - \{0\}$	$(-\frac{\pi}{2}, \frac{\pi}{2}) - \{0\}$
$\sec^{-1}$	$\mathbb{R} - \{-1, 1\}$	$[0, \pi] - \{\frac{\pi}{2}\}$
$\cot^{-1}$	$\mathbb{R}$	$(0, \pi)$

### Rational Root Theorem

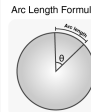
Possible Rational Roots:

$$f(x) = 2x^3 - 3x^2 - 11x + 6$$

$a_n: 1, 2, 3, 6$   
 $a_0: 1, 2$

### Arc Length

Arc Length Formula



$$\text{Arc Length} = 2\pi r \left(\frac{\theta}{360}\right)$$

### Sector Area

### Area of a Sector Formula

$$A = \frac{1}{2} r^2 \theta \quad \text{for } \theta \text{ in radians}$$

$$A = \frac{\theta}{360} \pi r^2 \quad \text{for } \theta \text{ in degrees}$$

### Rational Functions

Find an equation (in factored form) of a rational function,  $f$ , that satisfies the following conditions:

vertical asymptote:  $x = 4$   
Need factor in the denominator  $x - 4 = 0$

x-intercept:  $(-3, 0)$   $x + 3 = 0$   
Need factor in the numerator  $x + 3 = 0$

hole at  $x = -1$   $x + 1 = 0$   
Need same factor in numerator and denominator

horizontal asymptote:  $y = -\frac{2}{5}$   
Need degree of numerator and denominator to be the same and ratio of leading coefficients to be  $-\frac{2}{5}$

$$f(x) = \frac{-2(x+3)(x)}{5(x-4)(x+1)}$$

### Conversion

$$\text{Radians} = \left(\frac{\pi}{180^\circ}\right) \times \text{degrees}$$

$$\text{Degrees} = \left(\frac{180^\circ}{\pi}\right) \times \text{radians}$$

### Continuous Interest

Formula

$$P(t) = P_0 e^{rt}$$

$P(t)$  = value at time  $t$   
 $P_0$  = original principal sum  
 $r$  = nominal annual interest rate  
 $t$  = length of time the interest is applied

### Compound Interest

### Formula

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

$A$  = final amount  
 $P$  = initial principal balance  
 $r$  = interest rate  
 $n$  = number of times interest applied per time period  
 $t$  = number of time periods elapsed

### Reference Angle

Quadrant I given angle

Quadrant II  $180 - \text{given angle}$

Quadrant III given angle - 180

Quadrant IV  $360 - \text{given angle}$

### Trig Signs

### SIGNS OF TRIGONOMETRIC FUNCTIONS IN QUADRANTS

