

### Taylor Series

$$1/1-x \quad 1+x+x^2+x^3+\dots \quad \sum x^n$$

$$\sin(x) \quad x^1-x^3/3!+x^5/5!-\dots \quad \sum (-1)^n x^{2n+1}/(2n+1)!$$

$$e^x \quad 1+x+x^2/2!+x^3/3!+\dots \quad \sum x^n/n!$$

$$\cos(x) \quad 1-x^2/2!+x^4/4!-\dots \quad \sum (-1)^n x^{2n}/(2n)!$$

centered around 0  
(1/1-x only valid for  $-1 < x < 1$ .)

### Trig Sub's

$$\sqrt{x^2+a^2} \quad x = a \tan(\theta)$$

$$\sqrt{a^2-x^2} \quad x = a \sin(\theta)$$

$$\sqrt{x^2-a^2} \quad x = a \sec(\theta)$$

$$b-ax^2 \quad x = \sqrt{b/a} \sin(\theta)$$

$$ax^2+b \quad x = \sqrt{b/a} \tan(\theta)$$

$$ax^2-b \quad x = \sqrt{b/a} \sec(\theta)$$

### Convergence|Divergence test

$N^{\text{th}}$  term test for divergence  
 $\lim_{n \rightarrow \infty} a_n \neq 0$   $\sum a_n$  diverges

P-Test  
 converge  $p > 1$   
 diverge  $p \leq 1$

Limit Comparison  
 $L = \lim_{n \rightarrow \infty} (a_n/b_n)$   
 $L \neq 0$  series both converge|diverge

Ratio test  
 $r = \lim_{n \rightarrow \infty} |a_{n+1}/a_n|$   
 $r < 1$  converge  
 $r > 1$  diverge

Alternating series test  
 $\lim_{n \rightarrow \infty} a_n = 0$   
 $\sum (-1)^n a_n$  converges

### Common Integrals

$$\int \sin(x) dx \quad -\cos(x) + C$$

$$\int \cos(x) dx \quad \sin(x) + C$$

$$\int \tan(x) dx \quad -\ln|\cos(x)| + C$$

$$\int \sec(x) dx \quad \ln|\sec(x) + \tan(x)| + C$$

$$\int \csc(x) dx \quad -\ln|\csc(x) + \cot(x)| + C$$

$$\int \cot(x) dx \quad \ln|\sin(x)| + C$$

$$\int \sec^2(x) dx \quad \tan(x) + C$$

$$\int e^{f(x)} dx \quad e^{f(x)}/f'(x) + C$$

$$\int (1/x) dx \quad \ln|x| + C$$

$$\int (1/x^n) dx \quad (x^{n+1}/(n+1)) + C$$

$$\int dx/\sqrt{a-x^2} \quad \arcsin(x/\sqrt{a}) + C$$

$$\int dx/x^2+a \quad (1/\sqrt{a}) \arctan(x/\sqrt{a}) + C$$

### Important Derivatives

$$d/dx \arctan f(x) \quad f'(x)/(x^2+1)$$

$$d/dx \sec(\theta) \quad \sec(\theta)\tan(\theta)$$

### Power Series

$$\text{general form} \quad \sum a_n(x-a)^n$$

$a_n$  = sequence of coeff.

$$\text{center} \quad x=a$$

$$\text{radius of convergence} \quad R = \lim_{n \rightarrow \infty} |a_n/a_{n+1}|$$

$$\text{endpoints} \quad x=a+R \text{ and } x=a-R \text{ in series}$$

### Parametric Curves

Horizontal Tangents when  $dy/dx=0$   $t=?$  (x)

### Equations for Parabola

$$y=a(x-h)^2+k$$

$$\text{Directrix} \quad y=k-(1/4a)$$

$$\text{Focus} \quad (h, k+1/4a)$$

$$x=a(y-k)^2+h$$

$$\text{Directrix} \quad x=h-(1/4a)$$

$$\text{Focus} \quad (h+1/4a, k)$$

### Equations for Ellipses

$$(x-h)^2/a^2 + (y-k)^2/b^2 = 1 \quad c = \sqrt{|a^2-b^2|}$$

$$\text{eccentricity} \quad c/(\max a|b)$$

foci (on major axis) when  $x = \text{center}$  and  $y = \text{center}$

$y =$  horizontal axis

$x =$  vertical axis

### Trig Identities

$$\sec^2(\theta) \quad \tan^2(\theta)+1$$

$$\sin^2(\theta) \quad 1-\cos^2(\theta)$$

$$\tan^2(\theta) \quad \sec^2(\theta)-1$$

$$\cos^2(\theta) \quad [1+\cos(2\theta)]/2$$

$$\sin^2(\theta) \quad [1-\cos(2\theta)]/2$$

$$\text{double angle } \cos^2(\theta) \quad (1+\cos(2\theta))/2$$

$$\text{double angle } \sin^2(\theta) \quad (1-\cos(2\theta))/2$$

### Polar Coordinates & Area

$$\text{Area} \quad \int 1/2 (f(x))^2 dx$$

One petal of  $r = \sin(n\theta)$  interval  $[0, \pi/n]$

One petal of  $r = \cos(n\theta)$   $[-\pi/2n, \pi/2n]$

Polar  $\rightarrow$  Cartesian  $x = r\cos(\theta)$   $y = r\sin(\theta)$

Cartesian  $\rightarrow$  Polar  $\tan(\theta) = y/x$   $x^2+y^2 = r^2$