

Sketching Straight Lines

Using x & y intercepts | C cannot be equal to 0 Gradient - intercept method

$$ax + by = c \rightarrow \text{e.g } 2x - 5y = 10 \quad y = mx + c$$

y = 0 when solving x Horizontal Line
 $2x - 0 = 10$ gradient = 0

x = 5 y = c

x = 0 when solving y Vertical Line
 $2(0) - 5y = 10$ gradient = undefined

$-5y = 10$ x = a

y = 10/-5 a --> x-intercept

$$y = -2$$

Finding the equation of a straight line

Gradient + y-intercept	Gradient + a point (x1, y1)	2 points (x1, y1) (x2, y2)	Distance between 2 points
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Sub into equation	Sub into equation	1st find m	Sub into equation
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y = mx + c	y - y1 = m(x - x1)	m = y2 - y1 / x2 - x1	AB = $\sqrt{(x2 - x1)^2 + (y2 - y1)^2}$
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Example	Example	2nd sub into equation	Example
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c = 5 m = -1	m = 2 (2, -0.5)	y - y1 = m(x - x1)	A = (3, -5) B = (-2, 1)
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y = -1x + 5	y + 0.5 = 2(x - 2)	Example	AB = $\sqrt{(-2 - 3)^2 + (1 - -5)^2}$
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y + 0.5 = 2x - 4	(-1, 4), (5, 2)	AB = $\sqrt{(-5)^2 + 6^2}$
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y = 2x - 4.5	m = 2 - 4/3 - (-1)	AB = $\sqrt{25 + 36}$
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m = -2/4 --> -1/2	AB = $\sqrt{61}$
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$$y - 4 = -1/2(x - -1)$$

Finding the equation of a straight line (cont)

$$y - 4 = -1/2x - 1/2$$

$$y = -1/2x + 7/2$$

Middle point of a line

Middle point of a line	Paralell Lines	Perpendicular Lines
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Sub into equation - i.e / means divide	Sub into equation	Sub into equation
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M = (x1 + x2/2, y1 + y2/2)	m1 = m2	m1 x m2 = -1 or m2 = -1/m1
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Example	Example - 1st find m (gradient)	Example - 1st find m (gradient)
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(3, 5) (2, 7)	A (4, 13) B (2, 9)	A (-4, 9) B (2, -6)
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M = 3 + 2/2, 5 + 7/2	mAB = 9 - 13/2 - 4	mAB = -6 - 9/2 - (-4)
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M = (5/2, 12/2)	mAB = -4/-2	mAB = -15/6
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M = (5/2, 6)	mAB = 2	mAB = -5/2
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C (0, -10) D (15, 0)	C (-5, 8) D (10, 14)
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mCD = 0 - (-10)/15 - 0	mCD = 14 - 8/10 - (-5)
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mCD = 10/15	mCD = 6/15
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mCD = 2/3	mCD = 2/5
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$\therefore mAB \neq mCB$	2nd sub into m1 x m2 = -1
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\therefore not parralell	-5/2 x 2/5 = -1
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$$-10/10 = -1$$

$$\therefore AB \perp CD$$