

### Line

#### General equation

$$Ax + By + C = 0$$

#### Point slope equation

$$y - y_1 = m(x - x_1)$$

#### Slope of a straight line (m)

$$m = -A/B$$

$$m = (y_2 - y_1) / (x_2 - x_1)$$

$$m = \tan(\alpha)$$

### Positions relative to two lines

#### Equations

$$Ax + By + C = 0$$

$$A'x + B'y + C' = 0$$

#### Secant lines

$$A/A' \neq B/B'$$

#### Parallel lines

$$A/A' = B/B' \neq C/C'$$

#### Coincident lines

$$A/A' = B/B' = C/C'$$

### Parallel lines

#### Slope

$$m_1 = m_2$$

$$-A/B = -A'/B'$$

### Perpendicular lines

#### Slope

$$m_1 \cdot m_2 = -1$$

$$-A/B = B'/A'$$

### Points

#### Coordinates

$$P(x_1, y_1)$$

$$Q(x_2, y_2)$$

$$M(x_3, y_3)$$

#### Distance between two points (P and Q)

$$d = \sqrt{[(x_2 - x_1)^2 + (y_2 - y_1)^2]}$$

#### Midpoint (M)

$$x_3 = (x_1 + x_2) / 2$$

$$y_3 = (y_1 + y_2) / 2$$

#### Distance from a point (P) to a line

$$d = |(A \cdot x_1 + B \cdot y_1 + C) / \sqrt{a^2 + b^2}|$$

### Circumference

#### Ordinary equation

$$(x - a)^2 + (y - b)^2 = r^2$$

#### Elements

$$\text{Center: } C(a, b)$$

$$\text{Point: } P(x, y)$$

$$\text{Radius: } r$$

#### General equation

$$x^2 + y^2 + Ax + By + C = 0$$

If:

$$(A/2)^2 + (B/2)^2 - C > 0$$

$x$  and  $y$  don't multiply

$x^2$  and  $y^2$  have 1 as coefficient

#### Elements

$$A = -2a$$

$$B = -2b$$

$$C = a^2 + b^2 - r$$

### Ellipse

#### Equation

$$[(x - x_0)^2 / a^2] + [(y - y_0)^2 / b^2] = 1$$

$$\text{Center: } C(x_0, y_0)$$

$$\text{Horizontal radius: } a$$

$$\text{Vertical radius: } b$$

### Parabola

#### General equation

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

If:

$$A \neq 0 \vee B \neq 0$$

$$B^2 - 4AC = 0$$

#### Vertical Parabola Ordinary Equation

$$(x - x_0)^2 = 2p(y - y_0)$$

$$\text{Vertex: } V(x_0, y_0)$$

$$\text{Parameter: } p$$

#### Horizontal Parabola Ordinary Equation

$$(y - y_0)^2 = 2p(x - x_0)$$

$$\text{Vertex: } V(x_0, y_0)$$

$$\text{Parameter: } p$$

### Hyperbola

#### General equation

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

If:

$$A \neq 0 \wedge B \neq 0$$

$$A \cdot B < 0$$

#### Ordinary Equation (horizontal focal axis)

$$[(x - x_0)^2 / a^2] - [(y - y_0)^2 / b^2] = 1$$

#### Ordinary Equation (vertical focal axis)

$$[(y - y_0)^2 / b^2] - [(x - x_0)^2 / a^2] = 1$$

#### Equilateral Hyperbola Equation

$$a = b$$

#### Asymptotes

$$y = x$$

$$y = -x$$

#### Elements

$$\text{Center: } O(x_0, y_0)$$

Length of the semimajor axis of the hyperbola:  $a$

Length of the semi-minor axis of the hyperbola:  $b$

