

Abbreviations and Notations

- ▶ LSB: Least Significant Bit (right-most)
- ▶ MSB: Most Significant Bit (left-most)
- ▶ a, b (lower case): a single bit
- ▶ A, B (upper case): set of bits, e.g. A = {a_i}, i = [0, N-1]

Bit-wise operators

💡 Bool/Bit analogy (helps to remember effect of operators): 1 is TRUE, 0 is FALSE

⚠ While Bool operators (&&, ||, ! - no equivalence for ~) apply to simple TRUE/FALSE operands, bit-wise operators apply to **all** bits of their operands (see *Example* block)

- ▶ & (AND): both operands have 1s
- ▶ | (OR): either or both operands have 1s
- ▶ ^ (XOR, aka *exclusive OR*): either **but not both** operands have 1s
- ▶ ~(NOT, aka *complement*): 1 becomes 0; 0 becomes 1
- ▶ << (left-shift): a << n shifts all bits in a to the left by n positions and pads with 0s to the right.
- ▶ >> (right-shift): a >> n shifts all bits in a to the right by n positions and pads with 0s to the left

If a is an int, a << n and a >> n are equivalent to multiplying a dividing respectively by 2ⁿ

1-Bit Bit-wise Operators Summary

X	Y	X&Y	X Y	X^Y	~(X)
0	0	0	0	0	1
0	1	0	1	1	1
1	0	0	1	1	0
1	1	1	1	0	0

Source: <https://www.hackerearth.com/notes/bit-manipulation/>

Examples (using A = 1010; B = 1100)

- ▶ &: A&B = 1000
- ▶ |: A|B = 1110
- ▶ ^: A^B = 0110
- ▶ ~: ~A = 11110101 (the number of 1's depends on the type of A)
- ▶ <<: A << 2 = 0000

Usage

- ▶ Bit accessing: 1 << 5 = 100000
- TOREVIEW

Bit-wise Operators as Operations of Sets of Bits

- ▶ Using ALL_BIT = 32/64 1s on a 32/64-bit machines
- ▶ Union: A|B
- ▶ Intersection: A&B
- ▶ Subtraction: A&(~B)
- ▶ Negation: ALL_BITS^A

Two's Complement (TsC)

▶ Most common number system to encode pos. and neg. numbers in a binary number representation of negative integers. One's complement is the alternative but seemingly never used.

▶ In TsC, MSB used for int sign (- for 1, + for 0)

▶ Meaning 1: Mathematical operation on binary numbers (the *additive inverse* op.)

▶ Meaning 2: Binary signed number representation based on above mathematical operation, s.t. neg. numbers are represented by the TsC of the abs. value

▶ N-bit TsC range: $[-2^{N-1}, + (2^{N-1} - 1)]$

▶ Conversion from TsC representation

▶ Conversion to TsC representation

Source: https://en.wikipedia.org/wiki/Two%27s_complement

