| Differentiation |  |
| :---: | :---: |
| gradient of a line | $\begin{aligned} & m=\text { rise } / \text { run }=(y 2- \\ & y 1) /(x 2-x 1) \end{aligned}$ |
| as lim approaches 0 | $\begin{aligned} & m=(\lim h \rightarrow 0) f(x+h)- \\ & f(x) / h \end{aligned}$ |
| first derivative | $\mathrm{f}^{\prime}(\mathrm{x})=\mathrm{df} / \mathrm{dx}$ |
| second derivative | $f^{\prime \prime}(x)=d^{2} f / d x^{2}$ |
| third derivative | $f^{\prime \prime \prime}(x)=d^{3} f / d x^{3}$ |
| $d / d x x^{n}=n x^{n-1}$ | $d / d x \ln (x)-1 / x$ |
| $d / d x e^{x}=e^{x}$ | $\mathrm{d} / \mathrm{dx} \sin (\mathrm{x})=\cos (\mathrm{x})$ |
| $d / d x \cos (x)=-\sin (x)$ |  |
| product rule | $y=u v$ |
|  | $y^{\prime} u v^{\prime}+$ vu' |
| chain rule | $y=y(u(x))$ |
|  | $d y / d x=d y / d u . d u / d x$ |
| quotient rule | $y=u / v$ |
|  | $y^{\prime}=u^{\prime} v-u v^{\prime} / v^{2}$ |
| rewrite gradient <br> scalar product r where k is a sca derivative of a s $u^{\prime}(x)+v^{\prime}(x)$ | line: $m=f(x+h)-f(x) / h$ $d / d x(k u(x))=k u^{\prime}(x)$ <br> $\mathrm{m}: \mathrm{dx} \cdot(u(x)+v(x))=$ |
| Vectors |  |
| $\sin (\theta)=$ opposite/hypotenuse |  |
| $\cos (\theta)=$ adjacent/hypotenuse |  |
| $\tan (\theta 0=$ opposite/adjacent |  |
| $\mathrm{a}^{2}+\mathrm{b}^{2}=\mathrm{c}^{2}$ |  |

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| Matrices |
| :--- |
| $\mathrm{C}=\mathrm{A}+\mathrm{B} \quad$ addition/subtraction |
| $B=k A \quad k$ is scalar, $A$ is $m \cdot n$ matrix |
| $C=A B \quad$ if $\mathrm{A}=m \cdot n, \mathrm{~B}=n \cdot k$ |
| Trig Functions |
| $\mathrm{y}=\mathrm{a} \sin (\mathrm{bx}+\mathrm{c})+\mathrm{d}$ $\mathrm{y}=\mathrm{a} \cos (\mathrm{bx}+\mathrm{c})+\mathrm{d}$ <br> exponential $\mathrm{y}=\mathrm{e}^{\mathrm{x}}$ <br> function values x can <br> assume <br> domain values y can <br> assume <br> range  |

amplitude $=\mathrm{a}$
period $=2 \pi / b$
horizontal shift $=-\mathrm{c} / \mathrm{b}$
vertical shift $=\mathrm{d}$
$\sin (x)$ starts at $0, \cos (x)$ starts at one

Expon - e = eulers's constant.
domain/range : _ (> or <) _

## Logarithmic Differentiation

$\ln (a b)=\ln (a)+\ln (b)$
$\ln (a / b)=\ln (a)-\ln (b)$
$\ln \left(\mathrm{a}^{\mathrm{b}}\right)=\mathrm{b} x \ln (\mathrm{a})$
$\ln (\mathrm{e})=1$
$e^{\ln (x)}=x$

## Area Between Curves

$\int f(x) d x-\int g(x) d x \quad f(x)=$ upper function $g(x 0=$ lower function

Volume of $\quad V=\pi \int y^{2} d x$
Revolution
Integrating $\quad f^{\prime}(x)=x / x^{2}-1$
Ration
Functions

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| Integrals |  |
| :---: | :---: |
| $\int \sin (x) d x$ | $-\cos (x)+C$ |
| $\int \cos (\mathrm{x}) \mathrm{dx}$ | $\sin (x)+C$ |
| $\int e^{\wedge} x d x$ | $e^{x}+C$ |
| $\int 1 / x d x$ | $\ln (\mathrm{x})+\mathrm{C}$ |
| $\int x^{n} d x$ | $x^{n+1} / n+1+C$ |
| $\int \ln (\mathrm{x}) \mathrm{dx}$ | $x \ln (\mathrm{x})-\mathrm{x}+\mathrm{C}$ |
| scalar rule | $\int k u(x) d x=k \int u(x) d x$ |
| integral of a sum | $\begin{aligned} & \int(u(x)+v(x)) d x=\int u(x) d x \\ & +\int v(x) d x \end{aligned}$ |
| derivative of intergral | $\mathrm{d} / \mathrm{dx} \int \mathrm{u}(\mathrm{x}) \mathrm{d} \mathrm{x}=\mathrm{u}(\mathrm{x})$ |
| integral of derivative | $\int u^{\prime}(x) d x=u(x)+C$ |

Integrals of Common Functions

| $\int \sin (n x) d x$ | $-1 / n \cos (n x)+C$ |
| :--- | :--- |
| $\int \cos (n x) d x$ | $1 / n \sin (n x)=C$ |
| $\int e^{n x} d x$ | $1 / n e^{n x}+C$ |
| $\int \ln (n x) d x$ | $1 / n \ln (n x)+C$ |

## Integration by Substitution

$\int y(u(x)) u^{\prime}(x) d x \quad \int y(u) d u$

## Integration by Parts

$\int u v^{\prime} d x=u v-\int u ' v d x$
$\int x^{n} d x=x^{n+1} / n+1+C$ only applies when $n$ does NOT equal -1

## when $\mathrm{n}=-1, \int 1 / \mathrm{xdx}$ applies

Indefinite Integral: no numbers at top of bottom.

Definite Integral: solve for a number that represents the areas under the curve from $\mathrm{x}=\mathrm{a}$ to $\mathrm{x}=\mathrm{b}$
no integration constant in this situation

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| rules |  |
| :---: | :---: |
| product rule: $x$ multiplied together in different forms eg. $y=e^{2} e^{x}$ |  |
| chain rule: <br> inner function $u(x)$ <br> outer function: $\mathrm{y}(\mathrm{u})$ |  |
| looking for function within a function eg. $y=\ln (\sin (x))$. <br> let $u$ equal the inner function |  |
| quotient: x in both the numerator and denominator eg. $y=e^{x} x^{2}$ |  |
| remember $1 / a^{n}=a^{-n}$ |  |
| Functions \& Algebraic Structure |  |
| y-intercept: where crosses y | solve for $y$ when $x$ $=0$ |
| roots: where crosses X | solve for x when y $=0$ |
| linear functions | $y=m x+c$ |
| quadratic functions | $y=a x^{2}+b x+c$ |
| turning point | $x=-b / 2 \cdot a$ |
| roots of quadratic | use quadratic formula |
| $2 \pi=360^{\circ}$ | $\begin{aligned} & \text { radians = degrees } \\ & \pi / 180 \end{aligned}$ |

Function - can have only one output, y, or each unique input, $x$.
Relation - can have more than one output, $y$, for each unique input, $x$.
may be be more than one root for a function. roots can also be called $x$-intercepts and zeros
linear: $m x=$ gradient/slope $C=y$-intercept
quadratic: pos a = 'happy face', neg a = 'sad face'


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## Explicit/Implicit

Explicit: dependent variable is written explicitly in terms of the independent.
eg. $y=3 x+5$

Implicit: dependent variable is not isolated
to one side of equation
eg. $3 x+5-y=0$

Explicit differentiation: when starting with implicit from that is rearrangeable, rearrange then do.

Implicit differentiation: relies on the chain rule. No rearranging required

## Differential Equations

## First Order Separable

$f(x) \quad$ put all $x$ to one side and $y$ to other
$d x=$
g(y)
dy

## Power \& Log Rules

$a^{b} \cdot a^{c}=a^{b+c}$
$a^{b} / a^{c}=a^{b-c}$
$\ln \left(a^{b}\right)=b \ln (a)$
$\ln (e)=1$
$e^{\ln (x)}=x$

Decay
dN/dt $\quad N=$ amount of substance, $t=$ time
$=-\lambda \mathrm{N}$ and $\lambda$ is decay constant

## Newton's Law of Cooling

$\mathrm{dT} / \mathrm{dt} \quad \mathrm{T}=\mathrm{Temp}$ of object, Ta is ambient = - temp, t is time a k is heat transfer k(T- constant
Ta)

$$
\begin{aligned}
& \text { *Motion Problems } \\
& \begin{array}{l}
\mathrm{v}= \\
\mathrm{s}=\text { position, } \mathrm{v}=\text { velocity, } \mathrm{a}= \\
\mathrm{ds} / \mathrm{dt} \\
\text { acceleration, } \mathrm{t}=\text { time }
\end{array}
\end{aligned}
$$

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## Differential Equations (cont)

$\mathrm{a}=\mathrm{dv} / \mathrm{dt}$
A differential equation is just a mathematical equation that involves derivatives.
can have more than one solution

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