

Basic Trigonometric Integrals

$\int \sin(x)dx$	$-\cos(x)+C$
$\int \cos(x)dx$	$\sin(x)+C$
$\int \sec^2(x)dx$	$\tan(x)+C$
$\int \sec(x)\tan(x)dx$	$\sec(x)+C$
$\int \csc^2(x)dx$	$-\cot(x)+C$
$\int \csc(x)\cot(x)dx$	$-\csc(x)+C$

Common Trigonometric Integrals

$\int \sin(2x)dx$	$-\frac{1}{2}\cos(2x)+C$
$\int \cos(2x)dx$	$\frac{1}{2}\sin(2x)+C = \sin(x)\cos(x)+C$
$\int \tan(x)dx$	$\ln \sec(x) +C$
$\int \sec(x)dx$	$\ln \sec(x)+\tan(x) +C$
$\int \sec^3(x)dx$	$\frac{1}{2}(\sec(x)\tan(x)+\ln \sec(x)+\tan(x))+C$
$\int \csc(x)dx$	$-\ln \csc(x)+\cot(x) +C$
$\int \csc^3(x)dx$	$-\frac{1}{2}(\csc(x)\cot(x)+\ln \csc(x)+\cot(x))+C$
$\int 1/(1+x^2)dx$	$\arctan(x)+C$
$\int 1/(a^2+x^2)dx$	$(1/a)\arctan(x/a)+C$

Secant and Cosecant Integral Forms

Secant	$\int \sec(x)dx = \ln \sec(x)+\tan(-x) +C$
Integral 1	
Secant	$\int \sec(x)dx = -\ln \sec(x)-\tan(-x) +C$
Integral 2	
Secant	$\int \sec(x)dx = \frac{1}{2}\ln (\sin(x)+1)/(\sin(x)-1) +C$
Integral 3	
Secant	$\int \sec(x)dx = \ln \tan(x/-2+\pi/4) +C$
Integral 4	

Secant and Cosecant Integral Forms (cont)

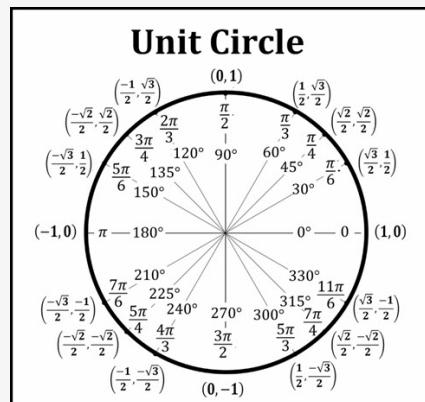
Cosecant	$\int \csc(x)dx = \ln \csc(x)-\cot(-x) +C$
Integral 1	
Cosecant	$\int \csc(x)dx = -\ln \csc(x)+\cot(-x) +C$
Integral 2	
Cosecant	$\int \csc(x)dx = \frac{1}{2}\ln (\cos(x)-1)/(\cos(x)+1) +C$
Integral 3	
Cosecant	$\int \csc(x)dx = \ln \tan(x/2) +C$
Integral 4	

Pythagorean Identities

Sine-Cosine Pythagorean	$\sin^2(x)+\cos^2(x)=1$
Sine Pythagorean	$\sin^2(x)=1-\cos^2(x)$
Cosine Pythagorean	$\cos^2(x)=1-\sin^2(x)$
Secant Pythagorean	$\tan^2(x)+1=\sec^2(x)$
Tangent Pythagorean	$\tan^2(x)=\sec^2(x)-1$
Secant-Tangent	$\sec^2(x)-\tan^2(x)=1$
Pythagorean	
Cosecant Pythagorean	$1+\cot^2(x)=\csc^2(x)$
Cotangent Pythagorean	$\cot^2(x)=\csc^2(x)-1$
Cosecant-Cotangent Pythagorean	$\csc^2(x)-\cot^2(x)=1$

The last two triplets of Pythagorean identities are obtained by dividing all the terms of the original identity by $\sin^2(x)$ or $\cos^2(x)$

Sine and Cosine Unit Circle



Powers of Trigonometric Functions

<https://cheatography.com/crossant/cheatsheets/integral-cases-for-trigonometric-powers/>

Quotient and Reciprocal Identities

$$\text{Tangent Quotient} \quad \tan(x) = \sin(x)/\cos(x)$$

$$\text{Cotangent Quotient} \quad \cot(x) = \cos(x)/\sin(x)$$

$$\text{Sine Reciprocal} \quad \sin(x) = 1/\csc(x)$$

$$\text{Cosine Reciprocal} \quad \cos(x) = 1/\sec(x)$$

$$\text{Tangent Reciprocal} \quad \tan(x) = 1/\cot(x)$$

$$\text{Cosecant Reciprocal} \quad \csc(x) = 1/\sin(x)$$

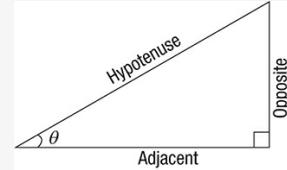
$$\text{Secant Reciprocal} \quad \sec(x) = 1/\cos(x)$$

$$\text{Cotangent Reciprocal} \quad \cot(x) = 1/\tan(x)$$

Sum and Difference Identities

$$\begin{aligned} \sin(x+y) &= \sin(x)\cos(y) + \cos(x)\sin(y) \\ \sin(x-y) &= \sin(x)\cos(y) - \cos(x)\sin(y) \\ \cos(x+y) &= \cos(x)\cos(y) - \sin(x)\sin(y) \\ \cos(x-y) &= \cos(x)\cos(y) + \sin(x)\sin(y) \end{aligned}$$

Right-Triangle Trigonometric Relations



$$\begin{aligned} \sin \theta &= \frac{\text{opposite}}{\text{hypotenuse}} & \csc \theta &= \frac{\text{hypotenuse}}{\text{opposite}} \\ \cos \theta &= \frac{\text{adjacent}}{\text{hypotenuse}} & \sec \theta &= \frac{\text{hypotenuse}}{\text{adjacent}} \\ \tan \theta &= \frac{\text{opposite}}{\text{adjacent}} & \cot \theta &= \frac{\text{adjacent}}{\text{opposite}} \end{aligned}$$

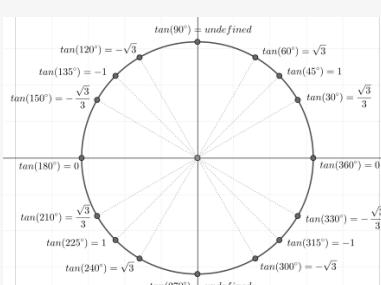
Trigonometric Substitutions

a^2-x^2	Let $x=\sin(\theta)$	$dx=\cos(\theta)d\theta$
x^2-a^2	Let $x=\sec(\theta)$	$dx=\sec^2(\theta)d\theta$
x^2+a^2	Let $x=\tan(\theta)$	$dx=\sec^2(\theta)d\theta$
$a^2-b^2x^2$	Let $x=(a/b)\cos(\theta)$	$dx=(a/b)\cos(\theta)d\theta$
$b^2x^2-a^2$	Let $x=(a/b)\sec(\theta)$	$dx=(a/b)\sec(\theta)\tan(\theta)d\theta$
$b^2x^2+a^2$	Let $x=(a/b)\tan(\theta)$	$dx=(a/b)\sec^2(\theta)d\theta$

Trigonometric substitutions are typically used under radicals, however, they are not required to be

For definite integrals, you will need to set x equal to its respective bounds, and solve for θ in order to properly change the bounds of integration with respect to θ

Tangent Unit Circle



Half-Angle and Double-Angle Identities

Sine Half-Angle	$\sin(x/2)=\sqrt{\frac{1}{2}(1-\cos(x))}$
Cosine Half-Angle	$\cos(x/2)=\sqrt{\frac{1}{2}(1+\cos(x))}$
Sine Power-Reducing using	$\sin^2(x)=\frac{1}{2}(1-\cos(2x))$
Cosine Power-Reducing using	$\cos^2(x)=\frac{1}{2}(1+\cos(2x))$
Sine Double-Angle	$\sin(2x)=2\sin(x)-\cos(x)$
Cosine Double-Angle 1	$\cos(2x)=\cos^2(x)-\sin^2(x)$
Cosine Double-Angle 2	$\cos(2x)=2\cos^2(x)-1$
Cosine Double-Angle 3	$\cos(2x)=1-2\sin^2(x)$
Sine Power-Reducing and Cosine Power-Reducing identities are variations of the Half-Angle identities	

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