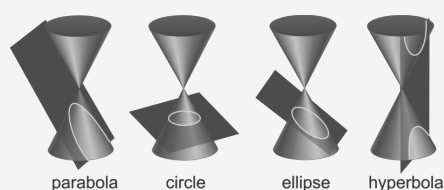


Parabolas with vertex (h,k)

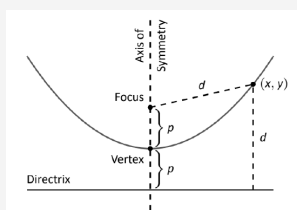
| | |
|--------------------|-------------------------|
| Opening up/down | $(x-h)^2 = \pm 4p(y-k)$ |
| Vertical Focus | $(h, k+p)$ |
| Directrix | $y=k-p$ |
| Opening right/left | $(y-k)^2 = \pm 4p(x-h)$ |
| Horizontal Focus | $(h+p, k)$ |
| Directrix | $x=h-p$ |

Any point on a parabola is equidistant from the parabola's focus and directrix

Conic Cross-Sections Diagram



Parabola opening upwards



Circles/Ellipses with center (h,k)

| | |
|-----------------|---------------------------------|
| Circle | $(x-h)^2 + (y-k)^2 = r^2$ |
| Circle Focus | (h, k) |
| Circle Vertices | None |
| Wide Ellipse | $(x-h)^2/a^2 + (y-k)^2/b^2 = 1$ |
| Wide Foci | $(h \pm c, k)$ |
| Wide Vertices | $(h \pm a, k \pm b)$ |
| Tall Ellipse | $(x-h)^2/b^2 + (y-k)^2/a^2 = 1$ |
| Tall Foci | $(h, k \pm c)$ |

Circles/Ellipses with center (h,k) (cont)

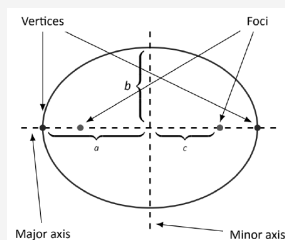
Tall Vertices $(h \pm b, k \pm a)$

$c^2 = a^2 - b^2$ and $a > b > 0$

Formulas for foci generate two different points (+c and -c), and formulas for vertices generate four different vertices: (h+a, k) (h-a, k) (h, k+b) and (h, k-b)

Distances between a focal point to any point on the ellipse, plus the distance of the other focal point to that same point on the ellipse, gives a sum of distances that is constant for any point on the ellipse

Wide Ellipse



Hyperbolas with center (h,k)

| | |
|-------------------------------|---------------------------------|
| Branches opening horizontally | $(x-h)^2/a^2 - (y-k)^2/b^2 = 1$ |
| Horizontal Foci | $(h \pm c, k)$ |
| Horizontal Vertices | $(h \pm a, k)$ |
| Asymptotes | $y-k = \pm (b/a)(x-h)$ |
| Branches opening vertically | $(y-k)^2/a^2 - (x-h)^2/b^2 = 1$ |
| Vertical Foci | $(h, k \pm c)$ |
| Vertical Vertices | $(h, k \pm a)$ |

Hyperbolas with center (h,k) (cont)

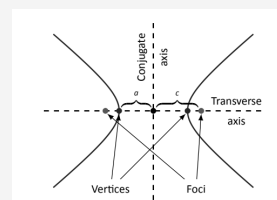
Asymptotes $y-k = \pm (a/b)(x-h)$

$c^2 = a^2 + b^2$ and $a, b \neq 0$

Formulas for foci generate two different points (+c and -c), formulas for vertices generate two different points (+a and -a), and formulas for asymptotes generate two different asymptotes (+a/b and -a/b) or +b/a and -b/a)

Distance of a focal point to a point on either hyperbola branch, minus distance of the other focal point to that same point on that same hyperbola branch, gives a value whose magnitude is constant for any point on either hyperbola branch

Horizontal Hyperbola



Horizontal Hyperbola Asymptotes

