

### Chapter 2: Motion along A Straight Line

s = speed                      t = time

Total Distance               $x_f + x_i$

#### One Dimensional Motion

Distance                      d = s·t

Displacement               $x_f - x_i$

Speed                           $(x_f + x_i) / (t_f + t_i)$

#### Not Constant Velocity

Average Velocity             $(x_f - x_i) / (t_f - t_i)$

x↑: v+                          a+: v↑

x↓: v-                          a-: v↓

x→: v=0                      a=0: v→

#### Instantaneous Acceleration

$(v_f - v_i) / (t_f - t_i)$

#### Constant Acceleration in 1D

$V_f = V_i + (a \cdot t)$

#### Constant Acceleration Final Distance

$X_f = 1/2(V_f - V_i) \cdot t$

$X_f = X_i + (V_i \cdot t) + 1/2(a \cdot t)$

$a = (V_f - V_i) / t$              $t = (V_f - V_i) / a$

$V_f = V_i \cdot a^2$

$V_f^2 = V_i^2 + 2 \cdot a (x_f - x_i)$

$G_y = -9.8 \text{ m/s}$

### Chapter 14: Periodic Motion

Angular Frequency         $w = 2\pi f$   
 $2\pi/T$

Frequency                     $f = 1 / T$

Period                         $T = 1 / f$

Restoring Force             $F_x = -kx$

#### Simple Harmonic Motion

k = Spring Constant      x = displacement

m = mass

### Chapter 14: Periodic Motion (cont)

Displacement as function of time     $x = A \cos(wt + \Theta)$

Velocity as function of time         $v = -wA \sin(wt + \Theta)$

Acceleration as function of time     $a = -w^2 A \cos(wt + \Theta)$

$x_{\max} = A$  [Amplitude]             $-x_{\max} = A$  [Amplitude]

$v_{\max} = wA$                            $-v_{\max} = wA$

$a_{\max} = w^2 A$                        $-a_{\max} = w^2 A$

Equation for Simple Harmonic Motion     $a \cdot x = - (k/m) x$

k = restoring force

Angular Frequency for SHM         $w = \sqrt{k/m}$

Frequency for SHM                   $f = w/2\pi$

$f = 1/2\pi \sqrt{k/m}$

Period for SHM                       $T = 1/f$

$T = 2\pi/w$

$T = 2\pi \sqrt{m/k}$

Total Mechanical Energy (Constant)     $E = 1/2 m v_x^2 + 1/2 k x^2$

$E = 1/2 k A^2$

### Chapter 6: Work and Kinetic Energy

1km = 1000m                      1 kg = 1000g

Dot Product                      P = Power

$A \cdot B = (A_i \cdot B_i) + (A_j \cdot B_j)$         t = s

Work = Force · distance

$W = F_x \cdot \text{distance}$

$W = F \cdot \cos\Theta \cdot \text{distance}$

$K_E: 1/2 \cdot m \cdot v^2$                       U = m·g·h

### Chapter 6: Work and Kinetic Energy (cont)

$W_{\text{total}} = K_{E_f} - K_{E_i}$

$W_x = F (\cos\Theta) \cdot s$  ||  $W_y = F (\sin\Theta) \cdot s$

#### Constant Speed

Friction (opposite) =  $\cos(180^\circ)$

$P = F \cdot v$                                   P = (W/t)

$P_{\text{av}} = \Delta W / \Delta t$  [Average Power]        if  $F \rightarrow$  &  $s \leftarrow = -W$

if  $F \downarrow$  &  $s \rightarrow = 0$                       if  $F \rightarrow$  &  $s \rightarrow = W$

#### Force Required to Stretch a spring

$F_x = k \cdot x$

### Chapter 13: Newton's Law of Gravitation

$G_E = 6.67 \cdot 10^{-11}$                       Earth Gravity Constant

$R_E = 6.38 \cdot 10^6 \text{ m}$                       Earth Radius

$M_E = 5.972 \cdot 10^{24} \text{ kg}$                       Mass of Earth

$g = 9.8 \text{ m/s}$ ;  $a_g = 9.8$                       r -  $R_E = h$

$F_g = (G_E \cdot m_1 \cdot m_2) / (r^2)$                        $F_g = m \cdot a$

$w = m \cdot g$                                    $s = r - R_E \cos\Theta$

Gravitation and Spherically Symmetric Bodies     $F_g = (G_E \cdot m_E \cdot m) / (r^2)$

Weight of the body at Earth's Surface         $w = F_g = (G_E \cdot m_E \cdot m) / (R_E^2)$

Acceleration due to Gravity             $g = (G_E \cdot m_E) / (R_E^2)$

Velocity of Earth                       $V_E = 4/3\pi R_E^2 = 1.08 \cdot 10^{21} \text{ m}^3$

#### Gravitational Potential Energy

$U = -(G_E \cdot m_E \cdot m) / (r)$

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### Chapter 13: Newton's Law of Gravitation (cont)

**Work Done by Gravity**  $W_{grav} = m \cdot g \cdot (r_1 - r_2)$

$$W_{grav} = G m_E \cdot m \cdot (r_1 - r_2) / (r_1 \cdot r_2)$$

$W_{grav} = G m_E \cdot m \cdot (r_1 - r_2) / (R_E^2)$  [if the body stays close to Earth]

**Speed of the Satellite**  $v = \sqrt{G \cdot m_E / r}$

**Period of Circular Orbit**  $T = (2\pi r / v)$

$$T = 2\pi r^{3/2} / \sqrt{G \cdot m_E} \quad T = 2\pi r \sqrt{r / G \cdot m_E}$$

**Point Mass Outside a Spherical Shell**  $U_i = - G m \cdot m_i / s$

**Apparent weight ; Earth's Rotation**

$w_0$  = true weight of object  $F$  = force exerted by spring scale

$F + w_0$  = net force on object  $w$  = apparent weight = opposite of  $F$

**centripetal acceleration**  $w_0 - F = (mv^2 / R_E)$

$$w = w_0 - (mv^2 / R_E)$$

**freefall acceleration**  $g = g_0 - (v^2 / R_E)$

**Black Holes**

$P$  = Density  $P = M / v$

$v = 4/3\pi R^3$   $c$  = speed of light in the vacuum

**Schwarzschild Radius**  $R_s = 2GM / c^2$

$$c = \sqrt{2GM / R_s}$$

### Chapter 7: Potential Energy, Energy Conservation

**Y-axis**

$E$  = Mechanical Energy

$$W_{grav} = F \cdot s = w(y_1 - y_2)$$

$$W_{grav} = (m \cdot g \cdot y_1) - (m \cdot g \cdot y_2)$$

$$W_{grav} = U_{grav,1} - U_{grav,2}$$

$$W_{grav} = -\Delta U_{grav}$$

**Conservation of Mechanical Energy**

$$K_f - K_i = U_{grav,1} - U_{grav,2}$$

$$K_i + U_{grav,1} = K_f + U_{grav,2}$$

$E = K + U_{grav} = \text{constant}$  (if gravity does work)

**When other forces than Gravity do work**

$$W_{other} + W_{grav} = K_f - K_i$$

**Elastic Potential Energy**

$$U_{el} = 1/2 k x^2$$

**Work Done a Spring**

$$W = 1/2 k x_2^2 - 1/2 k x_1^2$$

**If Elastic does work, total mechanical energy is stored**

$$K_i + U_{el,1} = K_f + U_{el,2}$$

**Situations with Both Gravitational and Elastic Potential Energy**

$$K_1 + U_1 + W_{other} = K_2 + U_2$$

**The work done by all forces other than the gravitational force or elastic force equals the change in total mechanical energy**  
 $E = K + U$  of the system

**The Law of Conservation of Energy**

$$\Delta U_{int} = -W_{other}$$

$$\Delta U_{int} = \text{internal energy}$$

**Force and Potential Energy**

$$F_x(x) = -dU(x) / dx$$

### Chapter 14: Periodic Motion (cont.)

**The Simple Pendulum (TSP)**  $L$  = pendulum length

**Angular Frequency TSP**  $w = \sqrt{k/m}$

$$w = \sqrt{mg / L / m}$$

$$w = \sqrt{g/L}$$

**Frequency TSP**  $f = w / 2\pi$

$$f = 1/2\pi \sqrt{g/L}$$

**Period TSP**  $T = 2\pi / w$

$$T = 1/f$$

$$T = 2\pi \sqrt{L/g}$$

**The Physical Pendulum (TPP)**

$L$  = angular momentum  $L = mvr$

$w$  = Angular Velocity  $w = \Delta\theta / \Delta t$

$$(I)_{inertia} = L / w$$

**Angular Frequency TPP**  $w = \sqrt{mgd / I}$

**Period TPP**  $T = 2\pi \sqrt{I / mgd}$

**Damped Oscillation**

$b$  = Damping Constant

**Displace of Damped**  $x = Ae^{-b(2m)t} \cos(\omega t + \theta)$

**Angular Frequency of Damped**  $w' = \sqrt{(k/m) - (b^2 / 4m^2)}$

**Force Oscillations and Resonance**

$F_{max}$  = Maximum Driving Force  $k$  = constant restoring force

$w_d$  = Driving Angular Frequency

$$A = F_{max} / \sqrt{(k - mw_d^2)^2 + b^2 w_d^2}$$

