

Complex Numbers

Polar Form $z = r \operatorname{cis} \theta$

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Modulus $|z| = \sqrt{a^2 + b^2}$

$$z = a + bi$$

Inverses

$a + b = b + a = 0$ Additive inverse of -5 is 5

$a \cdot b = b \cdot a = 1$ Multiplicative inverse of -1 is -1

Complex Conjugate z^*

Flip the sign of the imaginary number to get the conjugate (original $a + bi$) (complex con $a - bi$)

Eulers Identity $e^{i\pi} + 1 = 0$

Eulers equation ($e^{ix} = \cos x + i \sin x$)

Basis and Dimension

Linear independence

No linear combination of the remaining vectors

Basis

a set of vectors that span a vector space and are linearly independent

Factor out variables $a(1 \ 2 \ 3 \ 1)$

Number of independent vectors that form a basis

Dimension of $V = \dim(V)$

dimension of \mathbb{R}^n is n . $\dim(\mathbb{R}^3) = 3$

Rank

number of pivots after rref

Nullity

non pivot rows after rref

tuple

1 column list of numbers

Dimension of nullspace

rref and solve

Row Reduction

Augmented Matrix

Represents the whole system (line at end)

RREF

Leading 1 then zero under and next leading one beside, only zeros at bottom)

Augmented RREF

rref with complete system

Gauss-Jordan (elementary row operations)

$$R_2 = R_3 \dots R_1 = R_1 - R_3 \dots R_2 = R_1 - A(R_3)$$

Determinant

$$\det(A) = ad - bc$$

row reduce

Cofactor Expansion

Remove row A(31) row 3 column 1 you are left with 2×2 ... then it factors (A31) (2×2 matrix)

$$\det(A) = A_{31}(ad - bc) + A_{32}(ad - bc) + A_{33}(ad - bc)$$

Vectorspace

Subspace

set of vectors in W is a subset of the set of vectors in V

Spanning sets

All the matrices that form the same matrix set after

Linear Transformations

Kernel

rref and solve ($1a + 0b + 3/10c = 0$ $a = -3/10$)

$\operatorname{Ker}(T) = N(A)$ null space of A

Surjection (onto)

all outputs could be from 1 input

Injection (one-to-one)

different inputs different outputs

Bijection (both)

both injective and surjective

Linear Transformations (cont)

Change of Basis

$$t = a, b, c, d \quad v = e, f, g, h \dots v \text{ to } t \quad (e, g) = e(ac) + g(bd) \dots (f, h) = f(a, c) + h(b, d)$$

Matrix Multiplication

Identity Matrix

$$10 \ 01 \dots 100 \ 010 \ 001$$

Elementary matrix is matrix after a elementary row operation

Inverse & Matrix Algebra

$MA = I_n$

Left inverse

$AN = I_n$

Right inverse

Inverse of a product

inverse all the matrices in set

Invertible matrices

RREF to invert the matrix

Transpose $A^t = A_{11} \ A_{12} \ A_{21} \ A_{22}$

Switch places $A_{12} \rightarrow A_{21}$

Eigenstuff

Eigenvalue $\lambda I - A$ (solve for λ)

$$\lambda - (a) - b, -c, \lambda - (d) \text{ then } \det(\lambda - a) = (\lambda - a)(\lambda - d) - (-b)(-c)$$

Eigenvector

sub in λ to matrix $\lambda - (a) - b, -c, \lambda - (d)$ and rref and solve for x 's

Multiplicities

eigenspace λ

Diagonalization

can be diagonalized if multiplicities are equal. Needs more than 1 linearly independent eigenvalues

Need to know	
i	$\sqrt{-1}$
i^2	-1
multiply $3 \times 1 \times 1 \times 3$	$a_{11} \times b_{11}$
De MOIVRE	$z^n = r^n \text{cis}(n\theta)$
cis	$\cos \theta + i \sin \theta$ or $\cos \theta + (\sqrt{-1}) \sin \theta$
$\det(A)$	ad-bc
\mathbb{R}^n	
$\text{range}(T) + \text{nullity}(T) = n$ (in $m \times n$)	
m	row
n	column



By **ajani18ka**

cheatography.com/ajani18ka/

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