Cheatography

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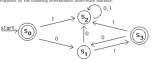
final

Final Exam 1

- 1. Prove or disprove that if A and B are sets then $A \cap (A \cup B) = A$

- Prove or disprove that if A and B are sets then A ∩ (A ∪ B) = A.
 Field the prime factorization of 16055.
 (i) Prove or disprove If a² = b² (and 5), where a and b are integers, then a² = b² (mod 5).
 (i) Prove or disprove If a² = b² (and 5), where a and b are integers, then a² = b² (mod 5).
 Use mathematical induction to prove that a² ≥ 2⁻¹ whence n is a positive integer.
 Suppose that a₁ = 0, a₂ = 5, and a_n = 2a_{n-1} + 3a_{n-2} for n ≥ 3. Prove that 5 divides a_n whenever n is a positive induced.
 How many the string of length 10 have a thesa too 0 in them?
 (i) How many functions are three from a set with three elements to a set with four elements?
 (i) How many functions are three from a set with three elements to a set with four elements?
 (i) How many gree outb²
 A door lock is opened by pushing a sequence of buttons. Each of the three terms in the combination is endered by pushing at their one buttons inframed evene of ways to ay on flight of stars if stars can be climber to "1 (Lamapte 15, 2.4 s is vaid combination.)
 Bern many positive infegers on the ensuit of the next of there down and you flight of stars if stars can be climber that fasting n = (x, y) | x y is an even integer) is an equivalence relation on the set of ruber.
 (i) Show many the relations P = ((x, y) | x y is an even integer) is an equivalence relation on the set of ruber.

- m₁ areas unas use reasons R = (1, Xy) (x = y is an even integer) is an equivalence relation on the set or al number.
 (b) What are the equivalence classes of 1 and ¹/₂ with respect to R?
 (b) Han are the forgurablence classes of 1 and ¹/₂ with respect to R?
 (c) How many vertices and how many edges are in this graph?
 (c) Is this graph hanor? Junify your areaver.
 (c) Both graph have an Eiber reioxil? Does it here an Eider path? Give reasons for your answers.
 (d) What is the chronatic number of this graph?
 Find a spanning tree for the graph K_{AA} using
 (a) a depth-fine search.
 (b) a the search.
 (b) at the search.
- 4. Find the sum-of-products expansion of the Boolean function f(x, y, z) that has the value 1 if and only if an odd number of the variables x, y, and z have the value 1.
 5. Find the set recognized by the following deterministic finite-state machine.



ped until a tail first a (a) What is the probability that exactly five flips are made?(b) What is the expected number of flips?

final2

Final Exam 2

- Prove or disprove that (A − B) = A ∪ B whenever A and B are sets.
 Prove or disprove that the fourth power of an odd positive integer always leaves a divided by 16.
- Prove or disprove that the fourth power of an odd positive integer always lowes a remainder of 1 when divided by 61.
 Use mathematical induction to prove that every postage of graster than 5 cents can be formed from 5 cent at 4 event stamps.
 Bor many the strings of fragch 10 have at least eight 1's in them?
 (a) flow many mixticians at there from a set with for dimensita to a set with eight densents?
 (b) flow many are ento?
 (b) flow many are ento?
 (c) and the positive integer gravest than 2 show that the relation?
 (c) and the positive integer gravest than 2. Show that the relation?
 (d) how many are ento?
 (e) boers the equivalence classes of this relation where m = 4.
 (e) how setup the equivalence classes of this relation where m = 4.
 (e) how setup the K₂₂ have an Elder circuit? If not, does it hare an Euler path?
 (f) how many many starks fragmention path?
 (f) how many many starks fragment thread theory thread theory the starks?
 (f) how many many endot fragment the version the starteners? This are path?
 (g) how the many many stark fragment multipost path?
 (h) construct a hary scark fragment multipost path?

- Bow many nonisomorphic unmoded trees are there with four vertices? Draw these trees.
 Construct a harry search tree from the versic of the scattere. This is powellawter found, using alphabetical order, inserting verds in the order they appear in the sentence.
 Find the same dependent expension for the Boolom function x + y + z.
 (a) Describe the bit strings that are in the regular set represented by 0*11(0 ∪ 1)??
 (b) Construct a nondeterministic finite-state automaton that recognizes this set.
 A thum tack is toosed until if real laoks with its point down, at which time no more tooses are made. On each toos, the probability that exactly five tooses are made?
 (a) What is the probability that exactly five tooses are made?
 (b) What is the explected number of tooses?

final 1 a

Final Exam 1 Solutions

- 1. Suppose that $x \in A$. Then $x \in A \cup B$, so $x \in A \cap (A \cup B)$. Conversely, suppose that $x \in A \cap (A \cup B)$. Then $x \in A$. Hence $A \cap (A \cup B) = A$.
- Then $x \in A$. Hence $A \cap (A \cup D) = A$. 2. We find that $2 \in A$ theore $A \cap (A \cup D) = A$. 2. We find that $2 \in A$ beam and divide 16755, but 3 does with 16575/3 = 5525. We see that 3 does not divide 5525, but 5 does with 5525/5 = 1105. We see that 5 divides 1105 with 1105/5 = 222. We see that atther 5 , n_{ee} that $a = b \pmod{5}$. However, 13 does with 22/13 = 17. Hence $16575 = 3 \cdot 5^2 3^2 \cdot 3^2 \cdot 13^2 \cdot 17$. 3. (a) Suppose that $a = b \pmod{5}$. How 5|a b|ba. Hence $a^{ab} = b^{ab} + b^{ab} + b^{ab} = a^{ab} + b^{ab} + b^{ab} + b^{ab} = a^{ab} + b^{ab} + b^{a} +$

- (b) We see that l⁺ = d⁺ (mod b), but l ≠ d + (mod b).
 A. The basis tep (does since l = 1 = 2ⁿ). For the inductive hypothesis assume that al ≥ 2ⁿ⁻¹. Then
 (n + 1)! = (n + 1) · n² ≥ (n + 1) · 2ⁿ⁻¹ ≥ 2 · 2ⁿ⁻¹ = 2ⁿ.
 The basis tep (a completed by nonline that a₁ = 10 and a₂ = 5 are both divisible by 5. For the inductive
 step assume that a₁ is divisible by 5 for every positive integer k with k ⊂ n, where n ≥ 3. It follows
 that a_n = 20n + 30n_n ≥ in divisible by 5, since the sum of two integer divisible by 5 is also divisible
 that a_n = 20n + 30n_n ≥ 1.

- by 5. The number of bit strings of length 10 with at least one 0 in them is the number of all bits strings of length 10 minus the number of bits strings of length 10 with no 0⁶ in them. This is 2¹⁰ − 1 = 1021 − 1 = 1023. 7. (a) There are 4 = 64 functions from as a with three dements to a set with or elements. (b) There are 4 − 3 − 2 = 24 concions from is not with three elements to a set with the or elements. (c) There are 4 − 3 − 2 = 0.1 concions from a set with there elements to a set with four elements. (c) There are 1 − 3 − 2 = 0.1 concions from a set with there elements to a set with four elements. (c) There are 0.1 concions from a set with there elements to a set with four elements. (c) A push of buttons in the conclusions is either the push of one of the five buttons or the simultaneous push of one of C(5,2) = 10 conditionations is either the push of one of the five buttons in the simultaneous push of one of C(5,2) = 0.1 conditionations of two of the five buttons. Hence there are 15 − 15 − 375 pushes the simultaneous for the door back.

final 2a

Final Exam 2 Solutions

- This set equality can be proved in several different ways. One method is to use set identities already known to hold. We find that $(\overline{A} \overline{B}) = (\overline{A} \cap \overline{B}) = \overline{A} \cup (\overline{B}) = \overline{A} \cup B$, where we have used De Morgan's laws and the double complementation law.

- used, so replace two 4-cent stamps with three 3-cent stamps to obtain postage of n + 1 cents. The number of bits trings of bengli 10 with a lost eight 11 with me equals the number with exactly eight 15 plan the number with exactly nine 15 plan the number with exactly into 15. These are $C(0, 6) = 10^{-10} (202) = 4$ s and s withing with exactly due 15. $C_{10}(0, 6) = 10^{-10}$ bits ariting with exactly due 15. $C_{10}(0, 6) = 10^{-10}$ bits ariting 40 mic ends of the string of bits arity of elements the exact $h = 10^{-1} 50^{-1}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting of length 10 even $h = 10^{-10}$ bits ariting 10 even $h = 10^{-10}$ bits arits ariting 10 even $h = 10^{-10}$ bits ariting 10 e
- (c) There are $3^4 C(3, 2)2^4 + C(3, 1)1^4 = 81 48 + 3 = 36$ onto functions from a set with four elements or a set with three elements.
- A symmetric relation is determined by specifying whether (i, j) and (j, j) belong to this relation for the pairs with i d j, and whether (i, i) bases to the station for all densats in the set. Since there are trained by specifying whether (i, j) and (j, j) belong to this relation for the pairs with i d j, and whether (i, i) bases to the pairs disc of all densats in the set. Since there are trained by the set of th
- (a) The graph K_{2,0} has two vertices of degree 5 and five vertices of degree 2. Hence it has an Euler path and no Euler circuit.
- (b) There is no Hamilton path in this graph since any path containing all five versits some of the vertices of degree 5 more than once.
- 9. There are two nonisomorphic unrooted trees with four vertices, as shown.





- ity of this is $(1/2)^5 =$
 - (b) The expected number of flips in a geometric distribution is 1/p = 2.



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of-products expansion is $f(x, y, z) = x y z + x \overline{y} \overline{z} + \overline{x} y \overline{z} + \overline{x} \overline{y} z$. ecognized is the set represented by $(01)^*$.

10. We construct the following binary search tre

discrete

start So ----

13. The n

The number of tosses follows a geometric distribution with parameter p =(a) The tack must land point up four times in a row and then point down, $(2/3)^4(1/3) = 16/243$.

(2/3) (1/3) = 10/243.
(b) The expected number of tosses in a geometric distribution is 1/p = 3.

this

• final

 \rightarrow (s₁) -

11. The Bodean function x + y + z has the value 1 unless x = y = z = 0, so it has the value 1 for the other seven combinations of the values of theor variable. Hence the sum-of-product expansion is 12. (a) The stringer is the seven theory has the begin value and thray number of 0's followed by too consecutive 11, is blowed by an arbitrary bit string.

• uour mathematics

(S2)

of $K_{3,4}$ is shown



(b) and due of Q(5,2) = 10 combination of two of the five battom. Hence there are 15–15–15 = 3375 possible combinations for the door bole.
 (c) Let a_n denote the number of ways to clink n ratius if stairs can be clinked one, two, or three at a time. Surgoest that n is a positive integra, n ≥ 4. A person can dish stairs by going up n = 1 stains and then clinking one stain, by going up n = 2 stains and then clinking one stain, by going up n = 3 taking and then clinking one stain, by going up n = 2 stains and then clinking one stain, by going up n = 3 taking and then clinking one stain, by going up n = 3 taking and then clinking one stain, by going up n = 3 taking and then clinking one stain, by going up n = 3 taking and then clinking one stain, by going up n = 3 taking and then clinking one stain, by going up n = 3 taking and then clinking the stain stain one, and a_i = 4 since we can clink the stain by the stain stain one, and a_i = 4 since we can clink the stain by the stain is the stain stain one, and a_i = 4 since we can clink the stain by one stain. To go the stain at the stain stain the two stains can be divided by the stain stain stains the stain stain stains the stain stain