

### Limits

**[2] Precise Definition of a Limit** Let  $f$  be a function defined on some open interval that contains the number  $a$ , except possibly at  $a$  itself. Then we say that the **limit of  $f(x)$  as  $x$  approaches  $a$  is  $L$** , and we write

$$\lim_{x \rightarrow a} f(x) = L$$

if for every number  $\epsilon > 0$  there is a number  $\delta > 0$  such that

$$\text{if } 0 < |x - a| < \delta \quad \text{then} \quad |f(x) - L| < \epsilon$$

### One Sided Limits

Show that the side you are evaluating exists

If it is defined @ value plug it in

### First/ Second Derivative Tests

First	Second
1. Take derivative and find c.v.	1. Take and find c.v.
2. Use a sign chart	2. Use a sign chart
+ is inc. / - is dec.	+ is CC up / - is CC down
shows extrema	shows inflection points
* test <b>endpoints</b>	*if checking extrema sign is the opposite

### Area Between Curves

$$A = \int_a^b (f(x) - g(x)) dx$$

$$A = \int_a^b (\text{top} - \text{bottom}) dx$$

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### Derivative of an Integral

$$\frac{d}{dx} \int_{g(x)}^{f(x)} f(t) dt = f(h(x)) h'(x) - f(g(x)) g'(x)$$

### Limit Definition of Derivatives

$$\frac{dy}{dx} = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$m = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

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### Power Rule

$$\frac{d}{dx} x^n = n \cdot x^{n-1}$$

### Product/Quotient Rule

$$\text{Product Rule: } \frac{d}{dx} [f(x)g(x)] = f(x)g'(x) + g(x)f'(x)$$

$$\text{Quotient Rule: } \frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

### Chain Rule

$$\frac{d}{dx} [f(g(x))] = f'(g(x)) \cdot g'(x)$$

$$\frac{d}{dt} [f(g(t))] = f'(g(t)) \cdot g'(t)$$

### Intermediate Value Theorem

IF  $f$  is a function that is continuous over the interval  $[a, b]$  and  $m$  is some number between  $f(a)$  and  $f(b)$ , THEN there exists a number  $c$  between  $a$  and  $b$  such that  $f(c) = m$ .

### Mean Value Theorem

Let  $f$  be continuous on  $[a, b]$  and differentiable on  $(a, b)$ . Then there exists a point  $c$  in  $(a, b)$  such that

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

### Rolle's Theorem

IF:

- $[a, b]$  is continuous
- $(a, b)$  is differentiable
- $f(a) = f(b)$

THEN:  $f'(c) = 0$

### Newton Raphson Method

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

### Related Rates

1. Draw a picture and label
2. Use formula for area/volume of shape
3. Take derivative of formula
4. Plug in values to each formula as needed

\*One variable will **NOT** have a rate of change (ex. ladder)



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